

**TS EAMCET Mathematics Previous Questions with Key – Test 5**

1) If  $f: [0, \infty) \rightarrow [0, \infty)$  is defined by  $f(x) = \frac{x}{1+x}$ , then  $f$  is

- 1) neither one-one nor onto
- 2) one-one but not onto
- 3) onto but not one-one
- 4) both one-one and onto

2) The range of the function  $f(x) = -\sqrt{-x^2 - 6x - 5}$  is

- 1)  $[-2, 0]$
- 2)  $[0, 2]$
- 3)  $(-\infty, -2]$
- 4)  $[-2, 2]$

3) If  $A = \begin{bmatrix} 1 & 1 \\ 0 & 1 \end{bmatrix}$  and  $I = \begin{bmatrix} 1 & 0 \\ 0 & 1 \end{bmatrix}$ , then for all  $n \in \mathbb{N}$

- 1)  $A^n = nA$
- 2)  $A^n = nA + (n-1)I$
- 3)  $A^n = (n-1)A - nI$
- 4)  $A^n = nA - (n-1)I$

4)The rank of the matrix  $\begin{bmatrix} 3 & 2 & 1 & -4 \\ 2 & 3 & 0 & -1 \\ 1 & -6 & 3 & -8 \end{bmatrix}$  is

1)1

2)2

3)3

4)4

5)Let, A, B, C be  $3 \times 3$  non – singular matrices and I be the identity matrix of order three. If  $ABA = BA^2 B$  and  $A^3 = I$ , then  $AB^4 - B^4A =$

1) $O_{3 \times 3}$

2) $\frac{I}{2}$

3)I

4)2I

6)If the system of equations

$$x + y + 2z = 3$$

$$x + 2y + 3z = 4$$

$$x + cy + 2cz = 5$$

1)c=1

2)c = 3

3)c  $\in$  R

4)c  $\neq$  1

7) If  $z = x + iy$  is a complex number satisfying  $\left| \frac{z-2i}{z+2i} \right| = 2$  and the locus of  $z$  is a circle then its radius is

1)  $\frac{5}{3}$

2)  $\sqrt{\frac{71}{9}}$

3)  $\frac{8}{3}$

4)  $\frac{1}{3}$

8) If  $(x - iy)^{\frac{1}{3}} = a + ib$ , then  $\frac{ax - by}{a - b} =$

1)  $a^3 - b^3$

2)  $a^3 + a^2b + ab^2 + b^3$

3)  $a^3 + 3a^2b + 3ab^2 + b^3$

4)  $a^4 - b^4$

9) If  $z = x + iy$  is a complex number and  $|1 + iz| = |1 - iz|$ , then

1)  $\text{Re}(z) > 0$

2)  $|z| = 1$

3)  $z = \bar{z}$

4)  $z = -\bar{z}$

10) The sum of the least positive arguments of the distinct cube roots of the complex number  $(1-i\sqrt{3})$  is

1)  $\frac{5\pi}{3}$

2)  $\frac{17\pi}{3}$

3)  $\frac{23\pi}{3}$

4)  $\frac{11\pi}{3}$

11) Let  $R-(\alpha, \beta)$  be the range of  $\frac{x+3}{(x-1)(x+2)}$ . Then the sum of the intercepts of the line  $\alpha x +$

$\beta y + 1 = 0$

1) -8

2) 10

3) 8

4) -10

12) If  $\alpha, \beta$  are the roots of the equation  $x^2 + 5x + 2 = 0$  then  $\left(\frac{\alpha}{2+5\alpha}\right)^2 + \left(\frac{\beta}{2+5\beta}\right)^2 =$

1)  $\frac{4}{21}$

2)  $\frac{19}{4}$

3)  $\frac{21}{4}$

4)  $\frac{4}{19}$

13) If the roots of  $x^4 - 10x^3 + 37x^2 - 60x + 36 = 0$  are  $\alpha, \alpha, \beta, \beta$  ( $\alpha < \beta$ ), then  $2\alpha + 3\beta - 2\alpha\beta$  =

1) 1

2) 0

3) -1

4) 4

14) The polynomial equation of degree 5 whose roots are the translates of the roots of  $x^5 - 2x^4 + 3x^3 - 4x^2 + 5x - 6 = 0$  by -2 is

1)  $x^5 - 8x^4 + 27x^3 + 46x^2 + 41x + 12 = 0$

2)  $x^5 + 8x^4 + 27x^3 + 46x^2 + 41x + 12 = 0$

3)  $x^5 + 6x^4 + 28x^3 + 46x^2 + 41x + 12 = 0$

4)  $x^5 + 8x^4 + 28x^3 + 46x^2 + 41x + 12 = 0$

15) The number of natural numbers less than 1000 in which no digit is repeated is

1) 729

2) 738

3) 792

4) 836

16) The coefficient of  $x^3$  in the expansion of  $\frac{1-2x}{(2x+1)(2-x)}$  is

1)  $-\frac{509}{80}$

2)  $\frac{509}{80}$

3)  $-\frac{103}{16}$

4)  $\frac{103}{16}$

17) If the coefficient of  $r^{\text{th}}$ ,  $(r + 1)^{\text{th}}$  and  $(r + 2)^{\text{th}}$  terms in the expansion of  $(1 + x)^n$  are respectively in the ratio 2 : 4 : 5, then  $(r, n) =$

1) (2, 7)

2) (3, 8)

3) (3, 9)

4) (4, 9)

18) If  $n$  is a positive integer greater than 1 then,

$$3({}^n C_0) - 8({}^n C_1) + 13({}^n C_2) - 18({}^n C_3) + \dots \text{ Upto } (n + 1) \text{ terms} =$$

1) -5

2)  $\frac{2^{n+1} - 1}{n}$

3)  $\frac{2^n - 1}{2}$

4) 0

19)  $\frac{3x - 2}{(x + 1)^2(x + 3)} = \frac{A}{x + 1} + \frac{B}{(x + 1)^2} + \frac{C}{x + 3}$ , then  $A + B + C =$

1)  $\frac{11}{4}$

2)  $\frac{5}{2}$

3)  $-\frac{5}{2}$

4)  $-\frac{11}{4}$

20) If  $\sin \theta + \sin^2 \theta = 1$  and  $\cos^{12} \theta + a \cos^{10} \theta + b \cos^8 \theta + c \cos^6 \theta + d = 0$  then

1)  $ab = cd$

2)  $ac = bd$

3)  $ab + cd = 0$

4)  $ac + bd = 0$

21)  $\cos 20^\circ \cos 40^\circ \cos 60^\circ \cos 80^\circ =$

1)  $\frac{3}{8}$

2)  $\frac{1}{8}$

3)  $\frac{\sqrt{3}}{8}$

4)  $\frac{1}{16}$

22) If  $A + B + C = \frac{\pi}{4}$ , then  $4 \cos \frac{A}{2} \cos \frac{C}{2} - \cos \frac{\pi}{8} =$

1)  $\cos\left(\frac{\pi}{4} - A\right) + \cos\left(\frac{\pi}{4} - B\right) + \cos\left(\frac{\pi}{4} - C\right)$

2)  $\cos\left(\frac{\pi}{8} - A\right) + \cos\left(\frac{\pi}{8} - B\right) + \cos\left(\frac{\pi}{8} - C\right)$

3)  $\sin\left(\frac{\pi}{4} - A\right) + \sin\left(\frac{\pi}{4} - B\right) + \sin\left(\frac{\pi}{4} - C\right)$

4)  $\sin\left(\frac{\pi}{8} - A\right) + \sin\left(\frac{\pi}{8} - B\right) + \sin\left(\frac{\pi}{8} - C\right)$

23) Let  $A = \{x \in \mathbb{R} / |\sqrt{3} \cos x - \sin x| \geq 2, 0 \leq x \leq 2\pi\}$ . If  $x_1 \in A, x_2 \in A$  then  $\frac{x_1}{x_2} =$

1)  $\frac{5}{23}$

2)  $\frac{11}{17}$

3)  $\frac{5}{11}$

4)  $\frac{11}{23}$

24) All the value of  $x$  satisfying the equation  $2 \tan^{-1} 2x = \sin^{-1} \left( \frac{4x}{1+4x^2} \right)$  lie in the interval

1)  $[-\frac{1}{2}, \frac{1}{2}]$

2)  $[-1, 1]$

3)  $[\frac{1}{2}, \infty)$

4)  $(-\infty, -\frac{1}{2}]$

25)  $\sinh^{-1} 2 + \cosh^{-1} 2 - \tanh^{-1} \frac{2}{3} + \coth^{-1} (-2) =$

1)  $\log \left( \frac{4+2\sqrt{3}+2\sqrt{5}+\sqrt{15}}{\sqrt{15}} \right)$

2)  $\log \left( \frac{4+2\sqrt{3}+\sqrt{5}+\sqrt{15}}{\sqrt{15}} \right)$

3)  $\log \left( \frac{(2+\sqrt{3})(2+\sqrt{5})\sqrt{5}}{\sqrt{3}} \right)$

4)  $\log \left( \frac{(2+\sqrt{3})(2+\sqrt{5})\sqrt{3}}{\sqrt{5}} \right)$

26) The greatest angle of the triangle whose side are  $x^2 + x + 1$ ,  $2x + 1$  and  $x^2 - 1$  is

1)  $75^\circ$

2)  $90^\circ$

3)  $105^\circ$

4)  $120^\circ$



27) In a  $\Delta ABC$ , if  $a : b : c = 4 : 5 : 6$ , then the ratio of the radius of its circumcircle to that of its incircle

1)  $16 : 7$

2)  $12 : 7$

3)  $15 : 8$

4)  $16 : 9$

28) In a  $\Delta ABC$ , the midpoint of  $BC$  is  $D$ . If  $AD$  is perpendicular to  $AC$ , then  $\cos A \cos C =$

1)  $\frac{1}{3} \frac{c^2 + a^2}{ab}$

2)  $\frac{2(c^2 + a^2)}{ab}$

3)  $\frac{2(c^2 - a^2)}{3ac}$

4)  $\frac{3(a^2 + b^2)}{2bc}$

29) The position vectors of three points  $A$ ,  $B$  and  $C$  are  $(1, 3, x)$ ,  $(3, 5, 8)$  and  $(y, -1, -6)$  respectively. If  $A$ ,  $B$  and  $C$  are collinear, then  $(x, y) =$

1)  $\left(\frac{2}{3}, -3\right)$

2)  $\left(\frac{10}{3}, 3\right)$

3)  $\left(\frac{10}{3}, -3\right)$

4)  $\left(-3, \frac{10}{3}\right)$

30) A line  $L$  passes through the points  $\bar{i} + 2\bar{j} + \bar{k}$  and  $-2\bar{i} + 3\bar{k}$ . A plane  $P$  passes through the origin and the points  $4\bar{k}, 2\bar{i} + \bar{j}$ . The point where the line  $L$  meets the plane  $P$  is

1)  $-\bar{i} - \bar{j} + 3\bar{k}$

2)  $-8\bar{i} - 4\bar{j} + 7\bar{k}$

3)  $8\bar{i} + 4\bar{j} + \bar{k}$

4)  $3\bar{i} + \bar{j} + 2\bar{k}$

31) If P, Q, R are the mid points of the sides AB, BC and CA of  $\Delta ABC$  respectively, then

$$\overline{PC} - \overline{BQ} =$$

1)  $\overline{CP}$

2)  $\overline{PQ}$

3)  $\overline{BR}$

4)  $\overline{AR}$

32) Let  $\vec{a} = \vec{i} + \vec{j}$ ,  $\vec{b} = \vec{j} + \vec{k}$  and  $\vec{c} = \vec{i} + \vec{k}$ . If  $\vec{d}$  is a unit vector such that  $\vec{a} \cdot \vec{d} = 0$  and  $\vec{b} \cdot (\vec{c} \times \vec{d}) = 0$ , then  $\vec{d} =$

1)  $\pm \frac{1}{\sqrt{2}}(\vec{i} + \vec{j})$

2)  $\pm \frac{1}{\sqrt{2}}(\vec{i} - \vec{j})$

3)  $\frac{1}{\sqrt{2}}\vec{i} + \frac{1}{\sqrt{2}}\vec{j} + \frac{1}{\sqrt{3}}\vec{k}$

4)  $\pm \left( \frac{1}{\sqrt{2}}\vec{j} + \frac{1}{\sqrt{2}}\vec{k} \right)$

33) If  $\vec{a} = \vec{i} + \vec{j}$  and  $\vec{b} = 3\vec{i} - 2\vec{j}$ , then the vector  $\vec{r}$  satisfying the equations  $\vec{r} \times \vec{a} = \vec{b} \times \vec{a}$  and  $\vec{r} \times \vec{b} = \vec{a} \times \vec{b}$  is

1)  $-\vec{i} + \vec{j} - 2\vec{k}$

2)  $-\vec{i} - 4\vec{j} - 2\vec{k}$

3)  $4\vec{i} - \vec{j}$

4)  $4\vec{i} - \vec{j}$

34)The shortest distance between the lines  $\vec{r} = (3t-4)\vec{i} - 2t\vec{j} - (1+3t)\vec{k}$  and  $\vec{r} = (6+s)\vec{i} + (2-2s)\vec{j} + 2(1+s)\vec{k}$  is

- 1)3
- 2)6
- 3)9
- 4)12

35)Let  $\sigma_1, \sigma_2$  be the standard deviations of two distributions  $D_1$  and  $D_2$  respectively and  $D_1$  be more consistent than  $D_2$ . If the means of  $D_1$  and  $D_2$  are same, then the percentage increase in the standard deviation of  $D_2$  over the standard deviation of  $D_1$  is

- 1)  $\frac{\sigma_1 - \sigma_2}{\sigma_2} \times 100$
- 2)  $\frac{\sigma_1 - \sigma_2}{\sigma_1} \times 100$
- 3)  $\frac{\sigma_2 - \sigma_1}{\sigma_2} \times 100$
- 4)  $\frac{\sigma_2 - \sigma_1}{\sigma_1} \times 100$

36)Consider the following distribution

$x_i$ :	2	4	6	8	10
$f_i$ :	1	2	3	2	1

The sum of the mean deviation from the mean and the mean deviation from the median of this distribution is

- 1)6
- 2) $\frac{16}{9}$
- 3)54
- 4) $\frac{32}{9}$

37) Ten persons with badges numbered 1 to 10 are in a room. If three of them are asked to leave the room, Then the probability to have the person with the smallest badge number as 5 among the three persons that left the room, is

- 1)  $\frac{3}{10}$       2)  $\frac{1}{6}$       3)  $\frac{1}{12}$       4)  $\frac{2}{5}$

38) A bag P contains 3 blue and 5 red balls. Another bag Q contains 4 blue and 6 red balls. A ball is drawn at random from one of the bags and is found to be red. The probability that is from bag Q is

- 1)  $\frac{24}{49}$       2)  $\frac{28}{49}$       3)  $\frac{36}{49}$       4)  $\frac{42}{49}$

39) Match the items List-I that of List-II:

A bag contains 4 red, 2 white and 5 blue balls. Three balls are drawn at a time randomly from the bag.

List-I

List-II

a) Probability of getting 1 red, 1 white and 1 blue ball

ii)  $\frac{3}{44}$

b) Probability of getting 2 white and 1 blue ball

ii)  $\frac{21}{55}$

c) Probability of getting 2 red and 1 white ball

iii)  $\frac{38}{55}$

d) Probability that none of the balls is white

iv)  $\frac{3}{11}$

v)  $\frac{9}{110}$

The correct answer is

1)a-v-b-ii, c-iii, d-iv

2)a-iv, b-i, c-v, d-ii

3)a-iv, b-i, c-v, d-iii

4)a-v, b-iii, c-iv, d-i

40)In a game of throwing 3 coins, a player will loose R.s. 5 for each head and gain Rs. 10 for each tail. If a random variable  $X : S \rightarrow R$  is defined as  $X(a) = \text{net gain } (a \in S)$ , then the mean of the random variable is (in rupees)

1)  $\frac{15}{2}$

2)  $-\frac{15}{2}$

3)15

4)25

41)A person fails 4 times in a game when he plays 9 times. If he plays 15 times, the probability of having success at most one is

1)  $\frac{65}{9} \left(\frac{5}{9}\right)^{14}$

2)  $\frac{65}{9} \left(\frac{5}{9}\right)^{15}$

3)  $\frac{79}{9} \left(\frac{4}{9}\right)^{14}$

4)  $\frac{79}{9} \left(\frac{4}{9}\right)^{15}$

42)If  $A = (-1, 2)$  and  $B = (1, -2)$  are two points and P is a variable point such that the area of  $\Delta PAB$  is always one, then the equation of the locus of P is

1)  $4x^2 + 4xy + y^2 = 1$

2)  $x^2 + 10xy + 25y^2 - 34x - 170y = 0$

3)  $x^2 - 6xy + 9y^2 - 22x - 66y - 23 = 0$

4)  $16x^2 + 24xy + 9y^2 - 62x + 34y + 46 = 0$

43)The point (4, 1) undergoes the following transformations successively:

i)Reflection about the line  $y = x$

ii)Translation through a distance 2 unit in the direction of positive X-axis

iii)Rotation through and angle  $\frac{\pi}{4}$  about origin in the anticlockwise direction

Then the final position of the point is

1)  $\left(\frac{7}{\sqrt{2}}, \frac{1}{\sqrt{2}}\right)$

2)  $(\sqrt{2}, 7\sqrt{2})$

3)  $(-\sqrt{2}, 7\sqrt{2})$

4)  $\left(\frac{1}{\sqrt{2}}, -\frac{7}{\sqrt{2}}\right)$

44)The image of the point (2, 4) with respect to the straight line  $2x + 3y - 6 = 0$  is

1)  $\left(-\frac{14}{13}, -\frac{8}{13}\right)$

2)  $\left(\frac{14}{13}, \frac{8}{13}\right)$

3)  $\left(-\frac{2}{13}, -\frac{4}{13}\right)$

4)  $\left(-\frac{2}{7}, -\frac{8}{7}\right)$

45)The equation of the base of an equilateral triangle is  $12x + 5y - 65 = 0$ . If one of its vertices is (2, 3), then the length of the side is

1)  $\frac{14}{13}$

2)  $\frac{2}{\sqrt{3}}$

3)  $\frac{4}{\sqrt{3}}$

4)  $\frac{2}{13}$

46) A triangle is formed by Y – axis, the straight line L passing through the points (3, 0),  $\left(1, \frac{4}{3}\right)$  and the straight line perpendicular to the line L and passing through the point (8, 1).

Then the area of that triangle (in square units) is

1) 16

2) 21

3) 36

4) 39

47) For  $c \neq 0$ ,  $c \neq 1$  if the straight lines  $x + y = 1$ ,  $2x - y = c$  and  $bx + 2by = c$  have one common point, then

1)  $c < 1 \Rightarrow b \in \left(-3, \frac{3}{4}\right)$

2)  $c < 1 \Rightarrow b \in \left(-\frac{3}{4}, 3\right)$

3)  $c < 1 \Rightarrow b \in \left(-3, \frac{3}{2}\right)$

4)  $c < 1 \Rightarrow b \in \left(-\frac{3}{4}, \frac{3}{4}\right)$

48) If the lines represented by  $x^2 - 2hxy - y^2 = 0$  are rotated about (0, 0) through an angle  $\alpha$  one in clockwise direction and the other in the counter clockwise direction, then the combined equation of the bisectors of the angle between the lines thus obtained is

1)  $x^2 - y^2 + hxy = 0$

2)  $x^2 - 2hxy + y^2 = 0$

3)  $hx^2 - hy^2 + 2xy = 0$

4)  $hx^2 - hy^2 + xy = 0$

49) The normal  $S = 0$  at  $P(1, 3)$  is  $x + 2y = 7$  and it has another normal at  $Q(3, 5)$  which is the polar of the point  $A(7, -\frac{1}{2})$  with respect to the circle  $x^2 + y^2 - 4x + 6y - 12 = 0$ . Then the equation of the circle  $S = 0$  is

1)  $x^2 + y^2 - 10x - 2y + 6 = 0$

2)  $x^2 + y^2 - 5x - 2y + 1 = 0$

3)  $x^2 + y^2 - 8x + 2y - 8 = 0$

4)  $x^2 + y^2 - 7x + 3y - 12 = 0$

50) If  $x + ky - 4 = 0$  and  $x + y - 5 = 0$  are conjugate lines respect to the circle  $(x - 1)^2 + (y - 1)^2 = 3$ , then  $k =$

1) 1

2) 2

3) 3

4) 4

51) The length of the chord intercepted by the circle  $x^2 + y^2 + 2x + 4y - 20 = 0$  on the line  $3x + 4y - 6 = 0$  is

1)  $5\sqrt{21}$

2)  $\frac{4}{5}\sqrt{21}$

3)  $\frac{8}{5}\sqrt{21}$

4)  $5\sqrt{2}$



52) Let Q be a point on the circle B:  $x^2 + y^2 = a^2$  and (h, k) be a fixed point. If the locus of the point which divides the join of P and Q in the ratio p : q is a circle C, then the centre of C is

1)  $\left(\frac{p+q}{p}, \frac{p+q}{q}\right)$

2)  $\left(\frac{hp+kq}{p}, \frac{hp+kq}{q}\right)$

3)  $\left(\frac{hq}{p}, \frac{kq}{q}\right)$

4)  $\left(\frac{hq}{p+q}, \frac{kq}{p+q}\right)$

53) A circle C passes through (2a, 0) and the line  $2x = a$  is the radical axis of the circle C and the circle  $x^2 + y^2 = a^2$ , then

1) centre of C is (-a, 0) and C passes through (0, 0) and (-a, -a)

2) circle C is  $x^2 + y^2 - 2ax - 2ay = 0$

3) centre of C is (a, 0) and C passes through (0, 0) and (a, a)

4) centre of C is (0, -a) and C passes through (-a, -a) and (0, 0)

54) If two distinct chords drawn from the point A(4, 4) on the parabola  $y^2 = 4x$  are bisected by the line  $y = ax$ , then the interval in which a lies is

1)  $\left(\frac{1}{2} - \frac{1}{\sqrt{2}}, \frac{1}{2} + \frac{1}{\sqrt{2}}\right)$

2)  $\left(-\frac{\sqrt{3}}{2}, \frac{1}{2}\right)$

3)  $\left(\frac{1+\sqrt{2}}{2}, \frac{5+\sqrt{2}}{2}\right)$

4) (2,  $\infty$ )

55)The locus of the midpoint of the line segment joining the focus to a moving point on the parabola  $y^2 = 4ax$  is a conic. The equation of the directrix of the conic is

1)  $y = a$

2)  $x = a$

3)  $y = 0$

4)  $x = 0$

56)For the ellipse  $4x^2 + y^2 - 8x + 2y + 1 = 0$ , the focus and the equation of the directrix are respectively

1)  $\left(-1 - \frac{4}{\sqrt{3}}, 1\right), y + \sqrt{3} + 1 = 0$

2)  $(-1 - \sqrt{3}, 1), \sqrt{3}y + \sqrt{3} + 4 = 0$

3)  $\left(1, -1 - \frac{4}{\sqrt{3}}\right), y + \sqrt{3} + 1 = 0$

4)  $(1, -1 - \sqrt{3}), \sqrt{3}y + \sqrt{3} + 4 = 0$

57)If  $3x + y + p = 0$  ( $p > 0$ ) is a tangent to the ellipse  $x^2 + 3y^2 = 3$  and  $16x + qy + 14 = 0$  ( $q > 0$ ) is a normal to the ellipse  $x^2 + 8y^2 = 33$  then  $p + q =$

1) 8

2) 5

3) 9

4) 6

58)The locus of the mid points of the chords of the circle  $x^2 + y^2 = 16$  which are tangents to the hyperbola  $9x^2 - 16y^2 = 144$  is

1)  $12x^2 - 8y^2 = x^2 + y^2$

2)  $9x^2 + 12y^2 = (x^2 + y^2)$

3)  $16x^2 - 8y^2 = (x^2 + y^2)$

4)  $16x^2 - 6y^2 = x^2 + y^2$

59) If the line segment joining the points P (2, 4, 1) and Q (3, 8, 1) is divided by the plane  $3x - ky - 6z = 0$  externally in the ratio 4 : 5 then  $k =$

1) -1

2) 1

3) 2

4) 3

60) If the direction cosines of two lines satisfy the equations  $1 + m + n = 0$  and  $2lm + 2ln - mn = 0$ , then the acute angle between those two lines is

1)  $\frac{\pi}{4}$

2)  $\frac{\pi}{3}$

3)  $\frac{\pi}{6}$

4)  $\frac{2\pi}{5}$

61) The perpendicular distance of the point (1, -1, 2) from the plane  $x + 2y + z = 4$ , is

1)  $\sqrt{17}$

2)  $\sqrt{6}$

3)  $\sqrt{\frac{3}{2}}$

4)  $\sqrt{\frac{2}{3}}$

62) If  $f(x)$  satisfies  $97 f(x) + m f\left(\frac{1}{x}\right) = 0$ , where  $f(x) = \lim_{n \rightarrow \infty} n \left( n^{1/n} - 1 \right)$ ,  $x > 0$ , then the value of  $m$  is

1)  $\frac{1}{97}$

2) 97

3) 0

4) 1

63) If  $f(x) = \begin{cases} \frac{\sqrt{1+ax} - \sqrt{1-ax}}{x}, & -1 \leq x < 0 \\ \frac{x^2+2}{x-2}, & 0 \leq x \leq 1 \end{cases}$

is continuous on  $[-1, 1]$ , then  $a =$

1) 1

2) -2

3) 1

4) 2

64) The function that is not differentiable at  $x = 1$  is

1)  $f_1(x) = |x|, -\infty < x < \infty$

2)  $f_2(x) = \begin{cases} 1 + \sin(x-1), & -\infty < x \leq 1 \\ x, & x \geq 1 \end{cases}$

3)  $f_3(x) = \begin{cases} x^2 + 7x - 7, & -\infty < x \leq 1 \\ \frac{3x-1}{2}, & x \geq 1 \end{cases}$

4)  $f_4(x) = \begin{cases} |x-1| + |x-2|, & -\infty < x \leq 1 \\ 1+x-x^3, & x \geq 1 \end{cases}$

65) Match the items of List-I with those of List-II

List-I

List-II

a)  $\frac{d}{dx} \left( \tan^{-1} \left( \sqrt{\frac{1-\cos x}{1+\cos x}} \right) \right)$

i)  $\log \left( x\sqrt{1+x^2} \right)$

b)  $\frac{d}{dx} \left( \frac{3+|x-1|}{3x+4} \right)$

ii)  $-\frac{4x}{(1+x^2)^2}$

c)  $\sinh^{-1}x$

iii)  $1/2$

b)  $\frac{d^2}{dx^2} \left( \cos^{-1} \left( \frac{1-x^2}{1+x^2} \right) \right)$

iv)  $\frac{1}{\sqrt{1+x^2}}$

v) not differentiable at  $x = 1$

1) a-iii, b-v, c-iv, d-ii

2) a-iv, b-v, c-ii, d-iii

3) a-i, b-iii, c-iv, d-v

4) a-iii, b-v, c-I, d-ii

66) If  $y = 2 \cos (2 \log x) + 3 \sin (2 \log x)$ , then  $x^2 y'' + xy' + 2y = 0$

1)  $-2y$

2)  $2y$

3)  $0$

4)  $4$

67) Consider the following statements

A is relative error in the area of a square when the relative error in its side is 0.4

B is relative error in the volume of a sphere when the relative error in its radius is 0.3

C is relative error in the surface area of a closed cylinder whose height is equal radius, when the relative error in its height is 0.2

D is approximate error in  $y = x^2 + x - 3$  when  $x = 2$  and  $\delta x = 0.1$

The ascending order of the values of errors in these statements is

1) B, C, A, D

2) A, C, B, D

3) C, D, A, B

4) D, A, C, B

68) If the curves  $\frac{x^2}{4} + \frac{y^2}{9} = 1$  and  $\frac{x^2}{16} - \frac{y^2}{k} = 1$  cut each other orthogonally, then  $k =$

1) 144

2) -9

3) 25

4) -21

69) The value  $c$  of the Lagrange's mean value theorem for the function  $f(x) = x(x-1)(x-2)$  in the interval  $[0, \frac{1}{2}]$  is

1)  $1 - \frac{\sqrt{7}}{2\sqrt{3}}$

2)  $1 - \frac{\sqrt{7}}{\sqrt{3}}$

3)  $\frac{1}{3}$

4)  $\frac{1}{6}$

70) If Q is the point on the parabola  $y^2 = 4x$  that is nearest to the point P(2, 0), then PQ =

- 1)1                      2)2                      3)3                      4)4

71) If  $\int \sin^{-1}\left(\frac{\sqrt{x}}{a+x}\right) dx = A(x) + \text{constant}$ , then  $A(x) =$

- 1)  $a \tan^{-1} \sqrt{\frac{x}{a}} + ax$                       2)  $\frac{1}{\sqrt{a+x}} \tan^{-1} \sqrt{\frac{x}{a}} - \sqrt{ax}$   
3)  $(a+x) \tan^{-1} \sqrt{x} + a\sqrt{x}$                       4)  $(a+x) \tan^{-1} \sqrt{\frac{x}{a}} - \sqrt{ax}$

72)  $\int \frac{\cos 2x \cdot \sin 4x}{\cos^4 x (1 + \cos^2 2x)} dx = +$

- 1)  $\log \left[ \frac{1 + \cos^2 2x}{1 + \cos 2x} \right] - \tan^2 x + c$                       2)  $\log \left( \frac{1 + \cos^2 2x}{1 + \cos 2x} \right) + \tan^2 x + c$   
3)  $\log \left( \frac{1 + \cos 2x}{1 + \cos^2 2x} \right) + \sec^2 x + c$                       4)  $\log \left( \frac{(1 + \cos 2x)^2}{1 + \cos^2 2x} \right) + \sec^2 x + c$

73)  $\int (\log x)^3 x^4 dx =$

- 1)  $\frac{x^5}{625} [125p^3 - 75p^2 + 30p - 6] + c$  (where  $p = \log x$ )  
2)  $\frac{x^5}{625} [125p^3 - 25p^2 + 30p - 5] + c$  (where  $p = \log x$ )  
3)  $\frac{x^5}{625} [125p^3 - 60p^2 - 25p + 5] + c$  (where  $p = \log x$ )  
4)  $\frac{x^5}{625} [625p^3 - 75p^2 + 30p + 6] + c$  (where  $p = \log x$ )

74) If  $\int \frac{\sqrt{x}}{\sqrt{x} - \sqrt[3]{x}} dx = x + Ex^{5/6} + Dx^{2/3} + Cx^{1/2} + Bx^{1/3} + Ax^{1/6} + \log(\sqrt[6]{x} - 1)^6 + k$ ,

then  $A + B + C + D + E$

1)  $\frac{137}{10}$

2)  $\frac{129}{10}$

3)  $\frac{119}{10}$

4)  $\frac{117}{10}$

75)  $\int_0^{\frac{1}{2}} |\sin 4\pi x| dx =$

1)  $\pi - 1$

2)  $\frac{2}{\pi}$

3)  $\frac{1}{\pi}$

4) 0

76) If  $f(n) = \frac{1}{n} [(n+1)(n+2)(n+3)\dots(2n)]^{\frac{1}{n}}$ , then  $\lim_{n \rightarrow \infty} f(n) =$

1)  $\frac{4}{e}$

2)  $\log\left(\frac{4}{e}\right)$

3)  $\frac{2}{e}$

4)  $\log\left(\frac{2}{e}\right)$

77) The area of the region bounded by  $y = |x|$  and  $y = 1 - |x|$  is

1)  $\frac{1}{4}$

2)  $\frac{1}{2}$

3)  $\frac{3}{2}$

4) 1

78) Consider the following differential equations

$D_1 : y = 4 \frac{dy}{dx} + 3x \frac{dx}{dy}$

$D_2 : \frac{d^2y}{dx^2} = \left( 3 + \left( \frac{dy}{dx} \right)^2 \right)^{4/3}$

$D_3 : \left[ 1 + \left( \frac{dy}{dx} \right) \right]^2 = \left( \frac{dy}{dx} \right)^2$

The ratio of the sum of the orders of  $D_1$ ,  $D_2$ , and  $D_3$  to the sum of their degrees is



1) 1 : 2

2) 1 : 1

3) 2 : 3

4) 3 : 2

79) The general solution of the differential equation  $\frac{dy}{dx} = 1 + x + y + xy$  is

1)  $\log(1+x) = y + \frac{x^2}{2} + k$

2)  $y = x + \frac{x^2}{2} + k$

3)  $\log(1+y) = \frac{x^3}{3} + k$

4)  $y = ke^{x + \frac{x^2}{2}} - 1$

80) The general solution of the differential equation  $(1 - y^2)dx = (\tan^{-1}y - x)dy$  is

1)  $x \tan^{-1}y = e^{(\tan^{-1}y)} + k$

2)  $x \tan^{-1}y = e^{\tan^{-1}y} - 1 + k$

3)  $xe^{\tan^{-1}y} = (\tan^{-1}y - y - e^y) + k$

4)  $x = (\tan^{-1}y - y - 1) + ke^{-\tan^{-1}y}$

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1	2	41	3
2	1	42	1
3	4	43	1
4	2	44	1
5	1	45	3
6	1	46	4
7	3	47	1
8	2	48	3
9	3	49	1
10	4	50	1
11	2	51	3
12	3	52	4
13	1	53	3
14	2	54	1
15	2	55	4
16	3	56	4
17	2	57	1
18	4	58	3
19	3	59	2
20	4	60	2
21	4	61	3
22	2	62	2
23	3	63	1
24	1	64	3
25	1	65	4
26	4	66	1
27	1	67	3
28	3	68	4
29	3	69	1
30	2	70	2
31	2	&	4
32	2	72	4
33	4	73	1
34	3	74	1
35	4	75	3
36	4	76	1
37	3	77	2
38	1	78	3
39	2	79	4
40	1	80	4