

### AP EAMCET Mathematics Previous Questions with Key – Test 10

**1) Among the following functions defined on R into R, the constant functions is**

1)  $\frac{3}{5+4\sin 3x}$

2)  $\frac{1}{2-\cos 3x}$

3)  $\cos^2 x + \cos^2\left(x + \frac{\pi}{3}\right) + \sin x \cdot \sin\left(x + \frac{\pi}{3}\right)$

4)  $\frac{15}{3\sin x + 4\cos x + 10}$

**2) The function  $f:[0, \infty) \rightarrow [0, \infty)$  defined by  $f(x) = \frac{x}{1+x}$  is**

- 1) One-one and onto
- 2) One-one but not onto
- 3) Onto but not one-one
- 4) Neither one-one nor onto

**3) For all  $n \in \mathbb{N}$ ,  $1 + \frac{1}{\sqrt{2}} + \frac{1}{\sqrt{3}} + \dots + \frac{1}{\sqrt{n}}$  is**

1)  $> n$       2)  $< \sqrt{n}$       3)  $\leq \sqrt{n}$       4)  $\geq \sqrt{n}$

**4) If** 
$$\begin{vmatrix} x^2 + x & x + 1 & x - 2 \\ 2x^2 + 3x - 1 & 3x & 3x - 3 \\ x^2 + 2x + 3 & 2x - 1 & 2x - 1 \end{vmatrix} = x A + B$$
, where A and B are determinants of order 3 not involving x, then  $|A| =$

1) 27      2) 24      3) 19      4) -8

**5) The system of equations  $x + y + z = 5$ ,  $x + 2y + az = 9$ ,  $x + 2y + z = b$  is inconsistent if**

- 1)  $a = 1, b = 9$
- 2)  $a = 1, b \neq 9$
- 3)  $a \neq 1, b = 9$
- 4)  $a \neq 1, b \neq 9$

6) If  $A = \begin{bmatrix} \cos \frac{2\pi}{33} & \sin \frac{2\pi}{33} \\ -\sin \frac{2\pi}{33} & \cos \frac{2\pi}{33} \end{bmatrix}$ , then  $A^{2017} =$

- 1) A      2)  $A^2$       3)  $A^4$       4)  $\begin{bmatrix} 1 & 0 \\ 0 & 1 \end{bmatrix}$

7) If  $(x + iy)^{1/3} = 5 + 3i$ , then  $3x + 5y =$

- 1) 480      2) 152      3) 990      4) 960

8) If  $z = \left(\frac{\sqrt{3}+i}{2}\right)^5 + \left(\frac{\sqrt{3}-i}{2}\right)^5$ , then

- 1)  $\operatorname{Re}(z) > 0, \operatorname{Im}(z) < 0$       2)  $\operatorname{Re}(z) > 0, \operatorname{Im}(z) > 0$   
 3)  $\operatorname{Re}(z) = 0$       4)  $\operatorname{Im}(z) = 0$

9) Match the items of List-I with those of List-II

List-I (Complex number)

i)  $\sqrt{3} - i$

ii)  $\sqrt{3} + i$

iii)  $-\sqrt{3} + i$

iv)  $-\sqrt{3} - i$

List-II (Polar form)

a)  $2\operatorname{cis}\frac{\pi}{6}$

b)  $2\operatorname{cis}\frac{5\pi}{6}$

c)  $2\operatorname{cis}\left(\frac{-5\pi}{6}\right)$

d)  $2\operatorname{cis}\left(-\frac{\pi}{6}\right)$

e)  $2\operatorname{cis}\frac{9\pi}{6}$

1) i-d, ii-b, iii-a, iv-e

2) i-d, ii-a, iii-b, iv-c

3) i-b, ii-d, iii-a, iv-c

4) i-b, ii-c, iii-a, iv-d

10) If  $(1 + x)^n = p_0 + p_1x + p_2x^2 + \dots + p_nx^n$ , then  $p_0 + p_3 + p_6 + \dots =$

1)  $\frac{1}{3} \left[ 2^{n-1} + \cos \frac{n\pi}{3} \right]$

2)  $\frac{2}{3} \left[ 2^{n-1} + \cos \frac{n\pi}{3} \right]$

3)  $\frac{1}{3} \left[ 2^{n-2} + \sin \frac{n\pi}{3} \right]$

4)  $\frac{2}{3} \left[ 2^{n-2} + \sin \frac{n\pi}{6} \right]$

11) The solution set contained in  $R^+$  of the inequation  $3^x + 3^{1-x} - 4 < 0$  is

1) (1, 3)

2) (0, 1)

3) (0, 1]

4) (0, 2)

12) The maximum value of the expression  $\frac{x^2+x+1}{2x^2-x+1}$ , for  $x \in R$ , is

1)  $\frac{7+2\sqrt{7}}{7}$

2)  $\frac{7-2\sqrt{7}}{7}$

3)  $\frac{7}{3}$

4)  $\frac{14+2\sqrt{7}}{7}$

13) If the equation  $x^5 - 3x^4 - 5x^3 + 2yx^2 - 32x + 12 = 0$  has repeated roots, then the prime number that divides then non-repeated root of this equation is

1) 7

2) 5

3) 3

4) 2

14) If  $\alpha, \beta$  are the roots of  $x^2 - 3x + a = 0$  and  $\gamma, \delta$  are the roots of  $x^2 - 12x + b = 0$  and  $\alpha, \beta, \gamma, \delta$  in that order form a geometric progression in increasing order with common ratio  $r > 1$ , then  $a + b =$

- 1) 16
- 2) 28
- 3) 34
- 4) 42

15) The number of subsets of  $\{1, 2, 3, \dots, 9\}$  containing at least one odd number is

- 1) 324
- 2) 396
- 3) 512
- 4) 496

16) Suppose  $t_n$  is the number of triangles formed using the vertices of a regular polygon of  $n$  sides. If  $t_{n+1} = t_n + 28$ , then  $n =$

- 1) 11
- 2) 9
- 3) 8
- 4) 7

17) The number of integers greater than 3000 that can be formed by any number of digits from 0, 1, 2, 3, 4, 5 without repetition in each number is

- 1) 1630
- 2) 1380
- 3) 1260
- 4) 1200

18) If  $|x|$  is so small that all terms containing  $x^2$  and higher powers of  $x$  can be neglected, then

approximate value of  $\frac{(3-5x)^{\frac{1}{2}}}{(5-3x)^2}$ , when  $x = \frac{1}{\sqrt{363}}$ , is

- 1)  $\frac{\sqrt{3}}{25}$
- 2)  $\frac{1+30\sqrt{3}}{75}$
- 3)  $\frac{1-30\sqrt{3}}{75}$
- 4)  $\frac{1+30\sqrt{3}}{750}$

19) If the first three terms in the binomial expansion of  $(1 + bx)^n$  in ascending powers of  $x$  are 1,  $6x^2$  respectively then  $b + n =$

1)  $\frac{28}{3}$

2)  $\frac{15}{2}$

3)  $\frac{29}{3}$

4)  $\frac{17}{3}$

20) If  $\frac{x^4}{(x-1)(x-2)(x-3)} = Ax + B \cdot \frac{1}{(x-1)} + C \cdot \frac{1}{(x-2)} + D \cdot \frac{1}{(x-3)} + E$ , then  $A + B + C + D + E = 0$

1)-12

2)6

3)8

4)32

21) If  $\cos\alpha + \cos\beta = a$ ,  $\sin\alpha + \sin\beta = b$  and  $\alpha - \beta = 2\theta$ , then  $\frac{\cos 3\theta}{\cos \theta} =$

1) $a^2 + b^2 - 2$

2) $a^2 + b^2 - 3$

3) $3^2 - a^2 - b^2$

4) $\frac{a^2 + b^2}{4}$

22)  $\cos^3\theta + \cos^3(120^\circ + \theta) + \cos^3(\theta - 120^\circ) =$

1) $\frac{\sqrt{3}}{2}\cos\theta$

2) $\frac{3}{4}\sec^3\theta$

3) $\frac{3}{2}\tan^3\theta$

4) $\frac{3}{4}\cos 3\theta$

23) The general solution of the trigonometric equation  $(\sqrt{3} - 1)\sin\theta + (\sqrt{3} + 1)\cos\theta = 2$  is

- 1)  $2n\pi \frac{\pi}{4} + \frac{\pi}{12}$
- 2)  $n\pi + (-1)^n \frac{\pi}{4} + \frac{\pi}{12}$
- 3)  $2n\pi \pm \frac{\pi}{4} - \frac{\pi}{12}$
- 4)  $n\pi + (-1)^n \frac{\pi}{4} - \frac{\pi}{12}$

24) Suppose  $S_a(x) = \text{Sec}^{-1}\left(\frac{x}{a}\right) + \text{Sec}^{-1}(a)$  for  $a \neq 0$ . If  $S_a(x) = S_b(x)$  for  $a \neq b$  then  $x =$

- 1) 1
- 2)  $\pm ab$
- 3)  $ab$
- 4)  $-ab$

25) If  $\sin x \cosh y = \cos\theta$  and  $\cos x \sinh y = \sin\theta$ , then  $\sinh^2 y =$

- 1)  $\cosh^2 x$
- 2)  $\cos^2 x$
- 3)  $\sin^2 x$
- 4)  $\sinh^2 x$

26) In  $\Delta ABC$ , if  $a = 2(\sqrt{3} + 1)$ ,  $B = 45^\circ$ ,  $C = 60^\circ$ , then the area (in sq. units) of that triangle is

- 1)  $2\sqrt{3}$
- 2) 6
- 3)  $6+2\sqrt{3}$
- 4)  $6-2\sqrt{3}$

27) The equation  $x^2 - 2\sqrt{3}x + 2 = 0$  represents two sides of a triangle. If the angle between them is  $\frac{\pi}{3}$ , then the perimeter of that triangle is

- 1)  $2\sqrt{3} + 6$
- 2)  $2\sqrt{3} + \sqrt{6}$
- 3)  $3\sqrt{2} + 6$
- 4)  $3\sqrt{2} + \sqrt{6}$

28) In  $\Delta ABC$ , if  $b = 2$ ,  $c = \sqrt{3}$ ,  $\angle A = 30^\circ$ , then its inradius  $r =$

1)  $\sqrt{3} - 1$

2)  $\sqrt{3} + 1$

3)  $\frac{\sqrt{3}+1}{2}$

4)  $\frac{\sqrt{3}-1}{2}$

29) If  $M$  is the foot of the perpendicular drawn from  $P(1, 2, -1)$  to the plane passing through the point  $A(3, -2, 1)$  and perpendicular to the vector  $4\bar{i} + 7\bar{j} - 4\bar{k}$ , then the length of  $PM$ , in proper units, is

1)  $\frac{24}{9}$

2)  $\frac{26}{9}$

3)  $\frac{28}{9}$

4)  $\frac{32}{9}$

30) The Cartesian equation of the line passing through the point  $\bar{i} - 2\bar{j} + \bar{k}$  and parallel to the vector  $\bar{i} + \bar{j} + 3\bar{k}$  is

1)  $(x - 1) = (y + 2) = (z - 1)$

2)  $\frac{(x-1)}{3} = \frac{(y+2)}{1} = \frac{(z-1)}{2}$

3)  $\frac{(x-1)}{3} = \frac{(y+2)}{1} = \frac{(z-1)}{3}$

4)  $\frac{(x+1)}{3} = \frac{(y-2)}{1} = \frac{(z+1)}{3}$

31) A vector of magnitude  $\sqrt{51}$  which makes equal angles with the vectors

$\bar{a} = \frac{1}{3}(\bar{i} - 2\bar{j} + 2\bar{k})$ ,  $\bar{b} = \frac{1}{5}(-4\bar{i} - 3\bar{k})$  and  $\bar{c} = \bar{j}$ , is

1)  $5\bar{i} - \bar{j} + 5\bar{k}$

2)  $-5\bar{i} - \bar{j} - 5\bar{k}$

3)  $-5\bar{i} + \bar{j} + 5\bar{k}$

4)  $\bar{i} - \bar{j} + 7\bar{k}$

32) A unit vector orthogonal to the vector  $3\bar{i} + 4\bar{j} + 5\bar{k}$  and coplanar with the vectors  $\bar{i} + \bar{j} + \bar{k}$  and  $\bar{i} - \bar{j} + \bar{k}$  is

1)  $\frac{1}{5}(4\bar{i} - 3\bar{j})$

2)  $\frac{1}{\sqrt{11}}(3\bar{i} - \bar{j} - \bar{k})$

3)  $\frac{1}{3}(2\bar{i} + \bar{j} - 2\bar{k})$

4)  $\frac{1}{\sqrt{6}}(\bar{i} - 2\bar{j} + \bar{k})$

33) Let  $\bar{a}$  and  $\bar{b}$  be two non-collinear unit vectors. If  $\bar{u} = \bar{a} - (\bar{a} \cdot \bar{b})\bar{b}$  and  $\bar{v} = \bar{a} \times \bar{b}$ , then  $|\bar{v}| =$

1)  $|\bar{u}|$

2)  $|\bar{a}|$

3)  $|\bar{b}|$

4)  $|\bar{a}||\bar{b}|$

34) The shortest distance between the line passing through the point  $\bar{i} + 2\bar{j} + 3\bar{k}$  and parallel to the vector  $2\bar{i} + 3\bar{j} + 4\bar{k}$  and the line passing through the point  $2\bar{i} + 4\bar{j} + 5\bar{k}$  and parallel to the vector  $3\bar{i} + 4\bar{j} + 5\bar{k}$ , is

1) 9

2)  $\frac{1}{\sqrt{6}}$

3) 1

4)  $\sqrt{6}$

35) The standard deviation of the following distribution is

Class interval	0-10	10-20	20-30	30-40
Frequency	1	3	4	2

1) 9

2) 8

3) 7

4) 6

36) a, a + d, a + 2d, ...., a + 2nd from their mean is equal to

- 1)  $\frac{(n+1)d}{2n+1}$
- 2)  $\frac{n(n+1)d}{2n+1}$
- 3)  $\frac{(n+1)|d|}{2n}$
- 4)  $\frac{n(n+1)|d|}{2n+1}$

37) If 5 red roses and 5 white roses of different sizes are used in preparing a garland, the probability that red and white roses come alternately is

- 1)  $\frac{1}{252}$
- 2)  $\frac{1}{126}$
- 3)  $\frac{1}{63}$
- 4)  $\frac{5}{126}$

38) There are eight different coloured balls and 8 bags having the same colours as that of the balls. If one ball is placed at random in each one of the bags, then the probability that 5 of the balls are placed in the respective coloured bags, is

- 1)  $\frac{1}{120}$
- 2)  $\frac{1}{160}$
- 3)  $\frac{1}{180}$
- 4)  $\frac{1}{360}$

39) If the probability function of a random variable X is given by  $P(X = k) = \frac{3^{ck}}{k!}$  for  $k = 1, 2, 3, \dots$  (where c is a constant), then c =

- 1)  $\frac{1}{2}\log_3(\log_e 2)$
- 2)  $\frac{1}{2}\log_2(\log_e 3)$
- 3)  $\log_3(\log_e 2)$
- 4)  $\log_2(\log_e 3)$

40) If X is a Poisson variate with mean 2, then  $P\left(X > \frac{3}{2}\right) =$

- 1)  $\frac{e^2 - 1}{2}$
- 2)  $\frac{e^2 - 1}{e}$
- 3)  $\frac{e^2 - 3}{e^2}$
- 4)  $\frac{e^2 - 1}{e^2}$

41) The locus of the point P such that the area of the  $\Delta PAB$  is 7, where A (4, 5) and B(-2, 3) are given points, is

- 1) a straight line
- 2) a pair of parallel lines
- 3) a circle
- 4) an ellipse

42) If the point P(4, 1) undergoes a reflection in the line  $x - y = 0$ , then a translation through a distance of 2 units along the positive X-axis and finally projected on the X-axis, then the coordinates of P in the final position, is

- 1) (3, 4)
- 2) (3, 0)
- 3) (1, 0)
- 4) (4, 3)

43) A straight line L cuts both the lines  $5x - y - 4 = 0$  and  $3x + 4y - 4 = 0$ . The segment of L between the two lines is bisected at the point (1, 5). The equation of L is

- 1)  $63x - 32y + 62 = 0$
- 2)  $36 - 53y - 72 = 0$
- 3)  $38x - 65y - 45 = 0$
- 4)  $8x - 35y + 92 = 0$

44) If the line  $(2x + 3y + 4) + \lambda(6x - y + 12) = 0$  is perpendicular to the line  $7x + 5y = 2$ , then  $\lambda =$

- 1)  $\frac{-27}{39}$
- 2)  $\frac{-29}{37}$
- 3)  $\frac{-27}{37}$
- 4)  $\frac{-28}{37}$

45) If P(-1, 0), Q(0, 0) and R(3,  $3\sqrt{3}$ ) are three points, then the equation of the bisector of the  $\angle PQR$  is

- 1)  $x + \sqrt{3}y = 0$
- 2)  $\sqrt{3}x + y = 0$
- 3)  $x + \frac{\sqrt{3}}{2}y = 0$
- 4)  $\frac{\sqrt{3}}{2}x + y = 0$

46) The product of the perpendicular distances drawn from the origin to the pair of straight lines  $6x^2 - 5xy - 6y^2 + x + 5y - 1 = 0$  is

- 1) 1
- 2)  $\frac{1}{12}$
- 3)  $\frac{1}{13}$
- 4) 13

47) If the slope of one of the lines represented by  $2x^2 + 3xy + ky^2 = 0$  is 2, then the angle between the pair of lines is

1)  $\frac{\pi}{2}$

2)  $\frac{\pi}{3}$

3)  $\frac{\pi}{6}$

4)  $\frac{\pi}{4}$

48) The angle between the lines joining the origin to the points of intersection of  $x + 2y + 1 = 0$  and  $2x^2 - 2xy + 3y^2 + 2x - y - 1 = 0$  is

1)  $\frac{\pi}{4}$

2)  $\frac{\pi}{3}$

3)  $\frac{\pi}{2}$

4)  $\frac{\pi}{6}$

49) The power of the point (-3, 7) with respect to a circle, with centre (3, 7) and radius 2, is

1) 49

2)  $\sqrt{32}$

3) 32

4) 7

50) The equation of the circle with (1, 1) as centre and which cuts a chord of length  $4\sqrt{2}$  units on the line  $x + y + 1 = 0$  is

1)  $x^2 + y^2 - 2x - 2y - 21 = 0$

2)  $2x^2 + y^2 - 4x - 4y - 21 = 0$

3)  $x^2 + y^2 - 2x - 2y - 10 = 0$

4)  $2x^2 + y^2 - 4x - 4y - 25 = 0$

51) The area of the triangle (in sq.units) formed by the tangents drawn from P(4, 4) to the circle  $S \equiv x^2 + y^2 - 2x - 2y - 7 = 0$  and the chord of contact of P with respect to  $S = 0$  is

- 1) 4.5
- 2) 8.1
- 3) 6.75
- 4) 1.5

52) The pole of the line  $x + y + 2 = 0$  with respect to the circle  $x^2 + y^2 - 4x + 6y - 12 = 0$  is

- 1) (23, 28)
- 2) (-23, 28)
- 3) (23, -28)
- 4) (-23, -28)

53) The angle between the circles  $x^2 + y^2 + 4x - 14y + 28 = 0$  and  $x^2 + y^2 - 12x - 6y - 4 = 0$  is

- 1)  $60^\circ$
- 2)  $\cos^{-1} \frac{3}{35}$
- 3)  $45^\circ$
- 4)  $\cos^{-1} \left( \frac{2}{\sqrt{5}} \right)$

54) The length of the common chord of the circles  $x^2 + y^2 + 3x + 5y + 4 = 0$  and  $x^2 + y^2 + 5x + 3y + 4 = 0$

- 1) 1
- 2) 2
- 3) 3
- 4) 4

55) The angle subtended by the normal chord at the point (9, 9) on the parabola  $y^2 = 9x$ , at the focus of the parabola is

- 1)  $45^\circ$
- 2)  $60^\circ$
- 3)  $90^\circ$
- 4)  $135^\circ$

56) If the vertex of a parabola is (4, 3) and its directrix is  $3x + 2y - 7 = 0$ , then the equation of latus rectum of the parabola is

- 1)  $3x + 2y - 18 = 0$
- 2)  $2x + 2y - 29 = 0$
- 3)  $3x + 2y - 8 = 0$
- 4)  $3x + 2y - 31 = 0$

57) The equation of a common tangent to the circle  $x^2 + y^2 = 16$  and to the ellipse  $\frac{x^2}{49} + \frac{y^2}{4} = 1$  is

- 1)  $y = x + \sqrt{45}$
- 2)  $y = x + \sqrt{53}$
- 3)  $\sqrt{11}y = 2x + 4$
- 4)  $\sqrt{11}y = 2x + 4\sqrt{15}$

58) The equation of the ellipse with  $x + y + 2 = 0$  as its directrix, one of its focus at (1, -1) and having eccentricity  $\frac{2}{3}$  is

- 1)  $7x^2 + 7y^2 + 4xy + 26x + 26y + 10 = 0$
- 2)  $7x^2 + 7y^2 - 4xy - 26x - 26y - 10 = 0$
- 3)  $7x^2 + 7y^2 - 4xy + 26x + 26y - 10 = 0$
- 4)  $7x^2 + 7y^2 + 4xy - 26x - 26y + 10 = 0$

59) Let C be the centre of the hyperbola  $\frac{x^2}{a^2} - \frac{y^2}{b^2} = 1$  and P be a point on it. If the tangent at P to the hyperbola meets the straight lines  $bx - ay = 0$  and  $bx + ay = 0$  respectively in Q and R, then  $CQ \cdot CR =$

- 1)  $a^2 - b^2$
- 2)  $a^2 + b^2$
- 3)  $\frac{1}{a^2} - \frac{1}{b^2}$
- 4)  $\frac{1}{a^2} + \frac{1}{b^2}$

60) If  $A = (5, 4, 2)$ ,  $B = (6, 2, -1)$ ,  $C = (8, -2, -7)$ , then the harmonic conjugate of  $A$  with respect to  $B$  and  $C$  is

- 1)  $(7, 0, -3)$
- 2)  $\left(\frac{13}{2}, -1, \frac{-5}{2}\right)$
- 3)  $\left(\frac{13}{2}, 1, \frac{-5}{2}\right)$
- 4)  $\left(\frac{11}{2}, 3, \frac{1}{2}\right)$

61) If the line joining  $(2, 3, -1)$  and  $(3, 5, -3)$  is perpendicular to the line joining  $A(1, 2, 3)$  and  $B(\alpha, \beta, \gamma)$  then a possible point for  $B$  is

- 1)  $(-3, 5, 7)$
- 2)  $(3, -5, 7)$
- 3)  $(3, 5, -7)$
- 4)  $(3, 5, 7)$

62) If a plane passes through  $(1, -2, 1)$  and is perpendicular to the planes  $2x - 2y + z = 0$  and  $x - y + 2z = 4$ , then the distance of that plane from the point  $(1, 2, 2)$  is

- 1)  $\sqrt{2}$
- 2) 2
- 3)  $2\sqrt{2}$
- 4) 4

63) If  $\Delta(x) = \begin{vmatrix} e^x & -1 \\ \sin x - 1 & 1 \end{vmatrix}$ , then  $\lim_{x \rightarrow 0} \frac{\Delta(x)}{x} =$

- 1) 1
- 2) 2
- 3) -1
- 4) 3

64) If  $f(x) = \begin{cases} \frac{\cos ax - \cos bx}{x^2}, & x \neq 0 \\ \frac{1}{2}(a^2 - b^2), & x = 0 \end{cases}$

Where a, b are real and distinct constants, then

- 1)f is discontinuous at  $x = 0$
- 2)f is continuous at  $x = 0$
- 3)  $\lim_{x \rightarrow 0} f(x)$  does not exist
- 4) $f(0)$  is not defined

65) If  $ay^4 = (x + b)^5$ , then  $\frac{y\left(\frac{d^2y}{dx^2}\right)}{\left(\frac{dy}{dx}\right)^2} =$

1) 5

2) -5

3)  $\frac{1}{5}$

4)  $-\frac{1}{5}$

66)  $x^3 + y^3 = 3xy \Rightarrow \frac{dy}{dx} =$

1)  $\frac{y-x^2}{y^2-x}$

2)  $\frac{y+x^2}{y^2+x}$

3)  $\frac{y-x^2}{y^2+x}$

4)  $\frac{y+x^2}{y^2-x}$

67) If  $y = \tan^{-1}\left(\frac{2x}{1-x^2}\right)$ ,  $|x| < 1$ , then  $\left(\frac{dy}{dx}\right)_{x=\frac{1}{2}} =$

1)  $\frac{1}{5}$

2)  $\frac{2}{5}$

3)  $\frac{4}{5}$

4)  $\frac{8}{5}$

68) The length of the normal to the curve  $x = a(\theta + \sin\theta)$ ,  $y = a(1 - \cos\theta)$  at  $\theta = \frac{\pi}{2}$  is

1)  $a^2$

2)  $a\sqrt{2}$

3)  $2a$

4)  $a$

69) Each edge of a cube is expanding at the rate of 1 cm/sec. Then the rate (in cc/sec.) of change in its volume, when each of its edge is of length 5 cm is

1) 25

2) 75

3) 125

4) 175

70) Lagrange's mean value theorem is not applicable in  $[0, 1]$  to the function

1)  $f(x) = \begin{cases} \frac{1}{2} - x, & x < \frac{1}{2} \\ (\frac{1}{2} - x)^2, & x \geq \frac{1}{2} \end{cases}$

2)  $f(x) = \begin{cases} \frac{\sin x}{x}, & x \neq 0 \\ 1, & x = 0 \end{cases}$

3)  $f(x) = |x|$

4)  $f(x) = |x|$

71) The shortest distance between the line  $y-x=1$  and the curve  $x=y^2$  is

1)  $\frac{2\sqrt{3}}{8}$

2)  $\frac{3\sqrt{2}}{5}$

3)  $\frac{\sqrt{3}}{4}$

4)  $\frac{3\sqrt{2}}{8}$

72)  $\int \frac{e^x - 1}{e^x + 1} dx =$

1)  $2\log_e(1+e^x) + x + c$

2)  $2\log_e(1+e^x) - x + c$

3)  $\log_e(1+e^x) + x + c$

4)  $\log_e(1+e^x) - x + c$

73)  $\int \cos^{-1}(2x^2 - 1) dx$

1)  $2(x\sin^{-1}x + \sqrt{1-x^2}) + c$

2)  $2(x\cos^{-1}x + \sqrt{1-x^2}) + c$

3)  $2(x\cos^{-1}x - \sqrt{1-x^2}) + c$

4)  $2(x\sin^{-1}x - \sqrt{1-x^2}) + c$

74)  $\int \frac{dx}{x(x^2+1)^3} =$

1)  $\frac{1}{2(x^2+1)} + \frac{1}{4(x^2+1)^2} + \log\sqrt{\frac{x^2}{x^2+1}} + c$

2)  $\frac{1}{x^2+1} + \frac{1}{2(x^2+1)^2} + \log\sqrt{\frac{x}{x^2+1}} + c$

3)  $\frac{1}{2(x^2+1)} + \frac{1}{4(x^2+1)^3} + \log\sqrt{\frac{x}{x+1}} + c$

4)  $\frac{2}{x^2+1} - \frac{1}{4(x^2+1)^2} - \log\sqrt{\frac{x}{x+1}} + c$

75)  $\int x^5 e^{-2x} dx =$

1)  $e^{-2x} \left[ \frac{x^5}{2} - \frac{5x^4}{2^2} + \frac{20x^3}{2^3} - \frac{60x^2}{2^4} + \frac{120x}{2^5} - \frac{120}{2^6} \right] + c$

2)  $-e^{-2x} \left[ \frac{x^5}{2} + \frac{5x^4}{4} + \frac{5x^3}{2} + \frac{15x^2}{4} + \frac{15x}{4} + \frac{15}{8} \right] + c$

3)  $-e^{-2x} \left[ \frac{x^5}{2} - \frac{5x^4}{2^2} + \frac{20x^3}{2^3} - \frac{60x^2}{2^4} + \frac{120x}{2^5} - \frac{120}{2^6} \right] + c$

4)  $e^{-2x} \left[ \frac{x^5}{2} + \frac{5x^4}{4} + \frac{5x^3}{2} + \frac{15x^2}{4} + \frac{15x}{4} + \frac{15}{8} \right] + c$

76)  $\lim_{n \rightarrow \infty} \left[ \frac{\sqrt{n^2 - 1^2}}{n^2} + \frac{\sqrt{n^2 - 2^2}}{n^2} + \frac{\sqrt{n^2 - 3^2}}{n^2} + \dots \text{to } n \text{ terms} \right] =$

1)  $\frac{\pi}{4}$       2)  $\frac{\pi}{2}$       3)  $\frac{\pi}{3}$       4)  $\frac{2\pi}{3}$

77) If  $\int_3^5 \sqrt{8x - x^2 - 15} dx = P$ , then  $\sin P + \cosec P =$

- 1)  $\frac{5}{2}$   
2) 0  
3) 1  
4) 2

78) The area (in sq. units) bounded by the curve  $x^2 + 2x + y - 3 = 0$ , the X-axis and the tangent at the point where the curve meets the Y-axis is

- 1)  $\frac{7}{10}$   
2)  $\frac{7}{12}$   
3)  $\frac{62}{11}$   
4)  $\frac{5}{11}$

79) The differential equation having the general solution  $y = c(x-c)^2$  (c is an arbitrary constant) is

- 1)  $(y')^2 = 4y^2 (x - y' - 2y)$
- 2)  $(y')^3 = 4y (x - y' - 2y)$
- 3)  $(y')^3 = y(x^2 y' - y)$
- 4)  $(y')^3 = 2y(x - y' + 2y)$

80) The solution of the differential equation  $(x+1)\frac{dy}{dx} - xy = 1$ , satisfying  $y(0) = 1$  is

- 1)  $\frac{1}{(1+x)}(e^x + 1) = y$
- 2)  $\log_e(1+x) + \frac{1}{2} = y$
- 3)  $\left(e^x - \frac{1}{2}\right) \frac{1}{x} = y$
- 4)  $\frac{1}{(1+x)}(2e^x - 1) = y$

APEAMCET-2018 -- Engineering Stream			
Final Key			
Date: 24-04-18 AN (Shift 2)			
1	3	41	1
2	2	42	1
3	3	43	3
4	1	44	1
5	1	45	1
6	2	46	3
7	2	47	3
8	2	48	3
9	1	49	1
10	3	50	3
11	3	51	1
12	4	52	2
13	1	53	2
14	3	54	1
15	3	55	3
16	3	56	1
17	2	57	1
18	3	58	4
19	2	59	2
20	1	60	4
21	2	61	2
22	4	62	4
23	3	63	2
24	1	64	4
25	1	65	4
26	2	66	3
27	3	67	1
28	2	68	3
29	3	69	3
30	3	70	3
31	2	71	3
32	4	72	3
33	1	73	4
34	3	74	1
35	3	75	1
36	3	76	4
37	1	77	3
38	2	78	4
39	4	79	4
40	1	80	4