## 6. UNITARY METHOD

Unitary method is the basic area of arithmetic.

## Direct Proportion

Two quantities are said to be directly proportional, if on the increase in one the other increases proportionally or on the decrease in one the other decreases proportionally,
e.g., More the numbers of articles, More is the cost.

More the number of workers, More is the work done.
Less the number of articles, Less is the cost.
Less the number of workers, Less is the work done.

## Indirect Proportion

Two quantities are said to be indirectly proportional, if on the increase in one the other decreases proportionally or on the decrease in one the other increases proportionally.
e.g., More the number of workers, less is the number of days required to finish a work. More the speed, less is the time taken to cover a certain distance.

Less the number of workers, more is the number of days required to finish a work. Less the speed, more is the time taken to cover a certain distance.

## Chain Rule

When a series of variables are connected with one another, that we know how much of the first kind is equivalent to a given quantity of second, how much of the second is equivalent to a given quantity of the third and so on. The rule by which we can find how much of the last kind is equivalent to a given quantity of the first kind is called the Chain Rule.
Example 1: If 12 apples cost Rs.216, what is the cost of 3 dozen apples?
Solution: Let the required cost be Rs. $\boldsymbol{x}$. Also, 3 dozen apples $=36$ apples
more apples- more cost (Direct Proportion);

| Apples | Cost |
| :--- | :---: |
| 12 | 216 |
| 36 | X |
| $12 \times \boldsymbol{x}=36 \times 216 \Rightarrow \boldsymbol{x}$ | $=\frac{\mathbf{3 6 2 1 6}}{\mathbf{1 2}}=$ Rs. 648 |

Example 2: A man completes $\frac{3}{5}$ of a job in 18 days. At this rate, how many more days will it take him to finish the job?
Solution: Let the number of days still required to finish the job be x days. Remaining Work $=\left(1-\frac{3}{5}\right)$ $=\frac{2}{5}$
Less work- Less hours (Direct Proportion).


Example 3: A wheel that has 5 cogs is meshed with a larger wheel of 15 cogs. When the smaller wheel has made 27 revolutions, find the number of revolution made by the larger wheel.
Solution:: Let the required number of revolutions made by larger wheel be x .
More cogs-Less revolutions (Indirect Proportion)

| Cogs | Revolutions made |
| :---: | :---: |
| 5 | 27 |
| 15 | x |
| $\Rightarrow 15 \times \boldsymbol{x}=5 \times 27 \Rightarrow$ | $\mathrm{x}=\frac{5 \times 27}{15}=9$ revolutions |

Example 4: If the wages for 8 men for 24 days be Rs.3040, then find the wages of 6 men for 18 days.
Solution: . Let the required wages be Rs. $x$.
Less men, Less wages (Direct Proportion)
Less days, Less wages (Direct Proportion)
Men Days Wages in Rs.
$8 \quad 24 \quad 3040$
$6 \quad 18$ x
$\Rightarrow \mathrm{x}=\frac{6}{8} \times \frac{18}{24} \times 3040=$ Rs. 1710
Example 5: If a man walks a certain distance in 20 days when he rests 10 h each day, how long will it take him to walk three times as far, if he walks twice as fast and rests 12 h each day?
Solution: In the first case the man walks (24-10)hr $=14 \mathrm{~h}$ each day. Let the distance travelled be d and the speed be s.
In the second case the man walks (24-12) $\mathrm{hr}=12 \mathrm{hr}$ each day. The distance travelled is $3 d$ and the speed is 2 s . Let the required number of days be x .
More distance-More days (Direct Proportion)
More speed-Less days (Indirect Proportion)
Less hours-More days (Indirect Proportion)

| Distance | Speed | Hours | Days |
| :---: | :---: | :--- | :--- |
| d | s | 14 | 20 |
| 3 d | 2 s | 12 | x |

$$
\mathrm{X}=\frac{3 d}{d} \times \frac{s}{2 s} \times \frac{14}{12} \times 20=35 \text { days }
$$

Example 6: A contractor undertakes to complete a road 420 m long in 140 days and employ 28 men for the work. After 70 days he finds that only 140 m of the road is made. How many men should the contractor employ more so that the work may be completed in time?
Solution: In the second case in (140-70) days i.e., 70 days the length of the road to be construct (420-140) m i.e., 280 m .
Let the number of men employed be $x$.
More length of road-More men (Direct Proportion)
Days Length of road in meters Men
$70 \quad 140 \quad 28$
70280 x

$$
\mathrm{X}=\frac{\mathbf{2 8 0}}{\mathbf{1 4 0}} \times \mathbf{2 8}=56 \mathrm{men}
$$

Additional men required $=56-28=28$ men

## EXERCISE

1. Cost of 24 pens is Rs. 96. Find the cost of 16 such pens,
(a) Rs. 66
(b) Rs. 64
(c) Rs. 62
(d) Rs. 68
2. A bus travels 240 km in 3 h . How long will it take to travel 360 km ?
(a) 5 h
(b) 4 h
(c) $4 \frac{1}{2} \boldsymbol{h}$
(d) $5 \frac{\mathbf{1}}{\mathbf{2}} \boldsymbol{h}$
3. The temperature dropped $18^{\circ} \mathrm{C}$ in the last 24 days. If the rate of temperature drop remains constant, then how many degrees will the temperature drop in the next 32 days?
(a) $24 \frac{1^{0}}{2} \mathrm{C}$
(b) $22^{\circ} \mathrm{C}$
(c) $22 \frac{1^{0}}{2} \mathrm{C}$
(d) $24^{\circ} \mathrm{C}$
4. Cost of 8 dozen bananas is Rs.180. How many bananas can be purchased for Rs. 30 ?
(a) 16 bananas
(b) 24 bananas
(c) 14 bananas
(d) 22 bananas
5. 20 men can reap a field in 20 days. When should 5 men leave the work, if the whole field is to be reaped in 24 days after they leave the work?
(a) 2 days
(b) 4 days
(c) 3 days
(d) 5 days
6. A rope makes 125 rounds of a cylinder with base radius 15 cm . How many times can it go round a cylinder with base radius 25 cm ?
(a) 100
(b) 75
(c) 80
(d) 65
7. 6 men finish one-fourth work in 2 days. The number of additional men required for finishing the same work in 2 days is
(a) 18 men
(b) 24 men
(c) 28 men
(d) 14 men
8. A certain number of men complete a piece of work in 45 days. If there were 5 men more, the work could be finished in 9 days less. How many men were originally there?
(a) 30
(b) 15
(c) 25
(d) 20
9. 10 workers can make 15 boxes in 6 days, how many boxes will 12 workers make in 3 days.
(a) 10
(b) 9
(c) 6
(d) 8
10. If 25 binders bind 25 books in 25 days. How many binders can bind 10 books in 10 days?
(a) 25
(b) 10
(c) 15
(d) 20
11. If 8 men working 9 h a day can reap a field in 24 days, in how many days will 12 men reap the field, working 6 h a day?
(a) 24 days
(b) 20 days
(c) 28 days
(d) 16 days
12. If 5 men take 21 days of 8 h each to do a piece of work. How many days of 6 h each would 14 women take, if 2 women do as much work as a man?
(a) 20 days
(b) 16 days
(c) 18 days
(d) 22 days
13. If the cost of ' $m$ ' articles is -n the cost of $P$ articles is
(a) Rs. $\frac{p \boldsymbol{n}}{m}$
(b) Rs. $\frac{p m}{n}$
(c) Rs. pmn
(d) Rs. $\frac{m n}{p}$

## SOLUTIONS

1. Let the required cost be Rs. x. Then,

Less pens, Less cost (Direct

| Pens | Cost in Rs. |
| :---: | :---: |
| 24 | 96 |
| 16 | $\boldsymbol{x}$ |

Proportion)

16
14. The work done by $(m+3)$ men in $(m-2)$ days and work done by $(\mathrm{m}-2)$ men in ( m +5 ) days are in the ratio $4: 5$. Find the value of $m$ ?
(a) 5
(b) 6
(c) 4
(d) 8
15. If 36 men take 9 days to earn rs 9000 . How many men will earn rs 6000 in 6 days?
(a) 42
(b) 36
(c) 45
(d) 39
16. A contractor undertakes to complete the repairing of a rail track 480 m long in 60 days and employs 60 men for the work. After 30 days he finds that only 160 m of the rail track is repaired. How many more men Should he employ to complete the work in time?
(a) 60 men
(b) 64 men
(c) 68 men
(d) 62 men
17. If 8 men or 12 women can do a piece of work in 52 days. In how many days can 12 men and 8 women do the same piece of work?
(a) 28 days
(b) 24 days
(c) 25 days
(d) 30 days
18. A camp of 3000 soldiers has provision for 60 days. After 15 days how many soldiers must leave so that the provision may last for 75 days?
(a) 1200
(b) 1400
(c) 1300
(d) 1500

| ANSWER KEY |  |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | b | 5 | a | 9 | b | 13 | a | 17 | b |
| 2 | c | 6 | b | 10 | a | 14 | a | 18 | a |
| 3 | d | 7 | a | 11 | a | 15 | b |  |  |
| 4 | a | 8 | d | 12 | a | 16 | a |  |  |

$x=\frac{16}{24} \times 96=$ Rs. 64
2. Let the required number of hours be $x$.

More distance, More hours (Direct
Proportion)
Distance (in km) Hours 240

```
                                    Hours
                                3
```

$$
\stackrel{360}{\Rightarrow x=\frac{360}{240} \times 3=\frac{9}{2}=4 \frac{1}{2} h}
$$

3. Let the required drop in temperature be $x$. More days, More drop in temperature (Direct Proportion)

| Days <br> 24 | Drop in temperature |
| :--- | :---: |
| 32 | 18 |
| $\Rightarrow \boldsymbol{x}=\frac{\mathbf{3 2}}{\mathbf{2 4}} \times \mathbf{1 8}=\mathbf{2 4}{ }^{\circ} \mathbf{C}$ |  |

4. 8 dozens $=8 \times 12=96$ bananas

Let the required number of bananas that can be bought be $x$.
Less price, Less bananas (Direct proportion)

$$
\begin{array}{ll}
\text { Cost in Rs. } & \text { Bananas } \\
180 & 96 \\
30 & \boldsymbol{x} \\
\Rightarrow \boldsymbol{x}=\frac{\mathbf{3 0}}{\mathbf{1 8 0}} \times \mathbf{9 6}=\mathbf{1 6} \text { bananas }
\end{array}
$$

5. 20 men can reap a field in 20 days.
$\Rightarrow 1$ man can reap that field in $(20 \times 20)$ days $=400$ days
Let 5 men leave the field after $x$ days, so that the remaining 15 men can complete the work field in 24 days.

$$
\begin{aligned}
& 20 x+15 \times 24=400 \\
& \Rightarrow x=2 \text { days }
\end{aligned}
$$

$\therefore 5$ men must leave the work after 2 days.
6. Let the required number of rounds be $x$.

More radius, Less rounds(Inverse Proportion)
Radius in cm

| 15 |
| :--- |
| 25 |
| $\Rightarrow \boldsymbol{x}=\frac{\mathbf{1 5} \times \mathbf{1 2 5}}{\mathbf{2 5}}=\mathbf{7 5}$ rounds | Round

$\boldsymbol{x}$
7. Time taken by 6 men to finish the whole work $=8$ days
Let the number of men required be $x$.
Less days, More men (Inverse Proportion)

| Days | Men |
| :--- | :---: |
| 8 | 6 |
| 2 | $\boldsymbol{x}$ |
| $\Rightarrow \boldsymbol{x}=\frac{\mathbf{8 \times 6}}{\mathbf{2}}=\mathbf{2 4}$ men |  |

The additional men required $=24-6$ men $=$ 18 men
8. Let there be originally $x$ men.

Then, $(x+5)$ men can finish the work in (45-9) days ie, 36 days
More days, Less men (Inverse Proportion)

$$
\begin{array}{lc}
\text { Days } & \text { Men } \\
36 & (x+5) \\
45 & x \\
\Rightarrow x=\frac{\mathbf{3 6}(x+5)}{\mathbf{4 5}} \Rightarrow x=\mathbf{2 0} \text { men }
\end{array}
$$

9. Let the number of boxes made be $x$.

More workers, More boxes (Direct
Proportion)
Less days, Less boxes (Direct Proportion)
Workers
Days Boxes
10
6 15
12
3
$\Rightarrow x=\frac{12}{10} \times \frac{3}{6} \times 15=9$ boxes
10. Let the number of binders required be $x$.

Less books, Less binders (Direct Variation)

Less days, More binders (Indirect Variation)

| Books | Days | Binders |
| :---: | :---: | :---: |
| 25 | 25 | 25 |
| 10 | 10 | $\boldsymbol{x}$ |
| $\Rightarrow \boldsymbol{x}=\frac{\mathbf{1 0}}{\mathbf{2 5}} \times \frac{\mathbf{2 5}}{\mathbf{1 0}} \times \mathbf{2 5}=$ |  |  |

## 25 binders

11. Let the required number of days be $x$.

More men, Less days (Indirect Proportion)
Less working hours, More days (Indirect
Proportion)

| Men | Hours | Days |
| :--- | :---: | :---: |
| 8 | 9 | 24 |
| 12 | 6 | $x$ |
| $\Rightarrow \boldsymbol{x}=\frac{\mathbf{8}}{\mathbf{1 2}} \times \frac{\mathbf{9}}{\mathbf{6}} \times \mathbf{2 4}=\mathbf{2 4 d a y s}$ |  |  |

12. 2 women $=1 \mathrm{man}$

14 women $=7$ men
More men, Less days (Indirect Proportion)
Less working hours, More days (Indirect Proportion)

|  | Men | Hours |
| :--- | :---: | :---: |
| 5 | 8 | Days |
| 7 | 6 | 21 |
| $\Rightarrow$ | $\boldsymbol{x}=\frac{\mathbf{5}}{\mathbf{7}} \times \frac{\mathbf{8}}{\mathbf{6}} \times \mathbf{2 1}=\mathbf{2 0}$ days |  |

13. Let the required cost be rs $x$.

More articles, More cost (Direct Proportion)

| Articles | Cost in Rs. |
| :--- | :--- |
| $m$ | $n$ |
| $p$ | $x$ |

$$
\Rightarrow \mathrm{x}=\frac{p n}{m}
$$

14. Work done by $(\mathrm{m}+2)$ men in ( $\mathrm{m}-2$ ) days

$$
=(\mathrm{m}+3)(\mathrm{m}-2)
$$

Work done by (m-2) men in ( $\mathrm{m}+5$ )
days

$$
\begin{aligned}
& =(\mathrm{m}-2)(\mathrm{m}+5) \\
\Rightarrow & \frac{(\mathbf{m}+3)(\mathbf{m}-2)}{(\mathbf{m}-\mathbf{2})(\mathbf{m}+5)}=\frac{4}{5} \Rightarrow \mathrm{~m}=5
\end{aligned}
$$

15. Let the required number of men be $x$.

Less days, More men (Indirect Proportion)
Less earnings, Less men (Direct
Proportion)

| Days | Earnings in Rs. | Men |
| :---: | :--- | :---: |
| 9 | 9000 | 36 |
| 6 | 6000 | $\boldsymbol{x}$ |
| $\Rightarrow \boldsymbol{x}$ | $=\frac{\mathbf{9}}{\mathbf{6}} \times \frac{\mathbf{6 0 0 0}}{\mathbf{9 0 0 0}} \times \mathbf{3 6}=\mathbf{3 6} \mathbf{~ m e n ~}$ |  |

16. In the second case in (60-30) days ie, 30 days the length of the rail track to be repaired (480-160) m, i.e. 320 m . More length of rail track, More men (Direct Proportion)

Men Days Length of rail track in meter

| 60 | 30 | 160 |
| :---: | :---: | :---: |
| $\boldsymbol{x}$ | 30 | 320 |
| $\Rightarrow \boldsymbol{x}$ | $=\frac{\mathbf{3 2 0}}{\mathbf{1 6 0}} \times \mathbf{6 0}$ | $=\mathbf{1 2 0}$ men |

Additional men required $=(120-60)$ men

$$
=60 \mathrm{men}
$$

17. 8 men $=12$ women $\Rightarrow 1$ man $=\frac{3 w}{2}$

12 men +8 women $=12\left(\frac{3 w}{2}\right)+8 w=26 w o m e n$
Let the required number of days be $x$.
More women, Less days (indirect Proportion)

| Women | Days |
| :---: | :--- |
| 12 | 52 |
| 26 | $\boldsymbol{x}$ |

$\Rightarrow x=\frac{12 \times 52}{26}=24$ days
18. After 15 days, 3000 soldiers have provision for 45 days.

Let the number of soldiers be $x$.
More days, Less soldiers (Indirect
Proportion)
Days Soldiers
453000
75 x
$\Rightarrow x=\frac{45 \times 3000}{75}=1800$ soldiers
Required Soldiers $=3000-1800=1200$

