

## MATHEMATICS

Let  $C_0$  be a circle of radius 1. For  $n \geq 1$ , let  $C_n$  be a circle whose area equals the area of a square inscribed in  $C_{n-1}$ .

Then  $\sum_{i=0}^{\infty} \text{Area}(C_i)$  equals

A.  $\pi^2$

B.  $\frac{\pi - 2}{\pi^2}$

C.  $\frac{1}{\pi^2}$

D.  $\frac{\pi^2}{\pi - 2}$

2 For a real number  $r$  we denote by  $[r]$  the largest integer less than or equal to  $r$ . If  $x, y$  are real numbers with  $x, y \geq 1$  then which of the following statements is always true?

A.  $[x + y] \leq [x] + [y]$

B.  $[xy] \leq [x][y]$

C.  $[2^x] \leq 2^{[x]}$

D.  $\left[ \frac{x}{y} \right] \leq \frac{[x]}{[y]}$

3 For each positive integer  $n$ , let

$A_n = \max \left\{ \binom{n}{r} \mid 0 \leq r \leq n \right\}$ . Then the number of

elements  $n$  in  $\{1, 2, \dots, 20\}$  for which  $1.9 \leq \frac{A_n}{A_{n-1}} \leq 2$  is

A. 9

B. 10

C. 11

D. 12

- 4 Let  $b, d > 0$ . The locus of all points  $P(r, \theta)$  for which the line  $OP$  (where  $O$  is the origin) cuts the line  $r \sin \theta = b$  in  $Q$  such that  $PQ = d$  is
- $(r - d) \sin \theta = b$
  - $(r \pm d) \sin \theta = b$
  - $(r - d) \cos \theta = b$
  - $(r \pm d) \cos \theta = b$
- 5 Let  $C$  be the circle  $x^2 + y^2 = 1$  in the  $xy$ -plane. For each  $t \geq 0$ , let  $L_t$  be the line passing through  $(0, 1)$  and  $(t, 0)$ . Note that  $L_t$  intersects  $C$  in two points, one of which is  $(0, 1)$ . Let  $Q_t$  be the other point. As  $t$  varies between 1 and  $1 + \sqrt{2}$ , the collection of points  $Q_t$  sweeps out an arc on  $C$ . The angle subtended by this arc at  $(0, 0)$  is
- $\frac{\pi}{8}$
  - $\frac{\pi}{4}$
  - $\frac{\pi}{3}$
  - $\frac{3\pi}{8}$
- 6 In an ellipse, its foci and the ends of its major axis are equally spaced. If the length of its semi-minor axis is  $2\sqrt{2}$ , then the length of its semi-major axis is
- 4
  - $2\sqrt{3}$
  - $\sqrt{10}$
  - 3



- 10 For a real number  $x$  let  $[x]$  denote the largest number less than or equal to  $x$ . For  $x \in \mathbb{R}$  let  $f(x) = [x]\sin(\pi x)$ . Then
- $\forall$ A.  $f$  is differentiable on  $\mathbb{R}$ .  
 $\forall$  B.  $f$  is symmetric about the line  $x = 0$ .  
~~C.~~  $\int_{-3}^3 f(x) dx = 0$ .  
 $\downarrow$ D. For each real  $\alpha$ , the equation  $f(x) - \alpha = 0$  has infinitely many roots.

- 11 Let  $f : [0, \pi] \rightarrow \mathbb{R}$  be defined as

$$f(x) = \begin{cases} \sin x, & \text{if } x \text{ is irrational and } x \in [0, \pi] \\ \tan^2 x, & \text{if } x \text{ is rational and } x \in [0, \pi]. \end{cases}$$

The number of points in  $[0, \pi]$  at which the function  $f$  is continuous is

- A. 6  
B. 4  
C. 2  
D. 0
- 12 Let  $f : [0, 1] \rightarrow [0, \infty)$  be a continuous function such that  $\int_0^1 f(x) dx = 10$ . Which of the following statements is **NOT** necessarily true?

A.  $\int_0^1 e^{-x} f(x) dx \leq 10$

B.  $\int_0^1 \frac{f(x)}{(1+x)^2} dx \leq 10$

C.  $-10 \leq \int_0^1 \sin(100x) f(x) dx \leq 10$

D.  $\int_0^1 f(x)^2 dx \leq 100$

- 13 A continuous function  $f : \mathbb{R} \rightarrow \mathbb{R}$  satisfies the equation

$$f(x) = x + \int_0^x f(t) dt.$$

Which of the following options is true?

- A.  $f(x+y) = f(x) + f(y)$   
 B.  $f(x+y) = f(x)f(y)$   
 C.  $f(x+y) = f(x) + f(y) + f(x)f(y)$   
 D.  $f(x+y) = f(xy)$
- 14 For a real number  $x$  let  $[x]$  denote the largest integer less than or equal to  $x$  and  $\{x\} = x - [x]$ . Let  $n$  be a positive

integer. Then  $\int_0^n \cos(2\pi[x]\{x\}) dx$  is equal to

- A. 0  
 B. 1  
 C.  $n$   
 D.  $2n-1$
- 15 Two persons  $A$  and  $B$  throw a (fair) die (six-faced cube with faces numbered from 1 to 6) alternately, starting with  $A$ . The first person to get an outcome different from the previous one by the opponent wins. The probability that  $B$  wins is

- A.  $\frac{5}{6}$   
 B.  $\frac{6}{7}$   
 C.  $\frac{7}{8}$   
 D.  $\frac{8}{9}$

- 16 Let  $n \geq 3$ . A list of numbers  $x_1, x_2, \dots, x_n$  has mean  $\mu$  and standard deviation  $\sigma$ . A new list of numbers  $y_1, y_2, \dots, y_n$  is made as follows:  $y_1 = \frac{x_1 + x_2}{2}$ ,  $y_2 = \frac{x_1 + x_2}{2}$  and  $y_j = x_j$  for  $j = 3, 4, \dots, n$ . The mean and the standard deviation of the new list are  $\hat{\mu}$  and  $\hat{\sigma}$ . Then which of the following is necessarily true?

- A.  $\mu = \hat{\mu}$  and  $\sigma \leq \hat{\sigma}$   
 B.  $\mu = \hat{\mu}$  and  $\sigma \geq \hat{\sigma}$   
 C.  $\sigma = \hat{\sigma}$   
 D.  $\mu \neq \hat{\mu}$

- 17 What is the angle subtended by an edge of a regular tetrahedron at its center?

- A.  $\cos^{-1}\left(\frac{-1}{2}\right)$       B.  $\cos^{-1}\left(\frac{-1}{\sqrt{2}}\right)$   
 C.  $\cos^{-1}\left(\frac{1}{3}\right)$       D.  $\cos^{-1}\left(\frac{-1}{\sqrt{3}}\right)$

- 18 Let  $S = \{(a, b) : a, b \in \mathbb{Z}, 0 \leq a, b \leq 18\}$ . The number of elements  $(x, y)$  in  $S$  such that  $3x + 4y + 5$  is divisible by 19 is

- A. 38      B. 19  
 C. 18      D. 1

19 For a real number  $r$  let  $[r]$  denote the largest integer less than or equal to  $r$ . Let  $a > 1$  be a real number which is not an integer, and let  $k$  be the smallest positive integer such that  $[a^k] > [a]^k$ . Then which of the following statements is always true?

A.  $k \leq 2([a]+1)^2$

B.  $k \leq ([a]+1)^4$

C.  $k \leq 2^{[a]+1}$

D.  $k \leq \frac{1}{a-[a]} + 1$

20 Let  $X$  be a set of 5 elements. The number  $d$  of ordered pairs  $(A, B)$  of subsets of  $X$  such that  $A \neq \phi, B \neq \phi, A \cap B = \phi$  satisfies

A.  $50 \leq d \leq 100$

B.  $101 \leq d \leq 150$

C.  $151 \leq d \leq 200$

D.  $201 \leq d$

## PHYSICS

- 21 A uniform thin rod of length  $2L$  and mass  $m$  lies on a horizontal table. A horizontal impulse  $J$  is given to the rod at one end. There is no friction. The total kinetic energy of the rod just after the impulse will be

A.  $\frac{J^2}{2m}$

B.  $\frac{J^2}{m}$

C.  $\frac{2J^2}{m}$

D.  $\frac{6J^2}{m}$

- 22 A solid cylinder  $P$  rolls without slipping from rest down an inclined plane attaining a speed  $v_p$  at the bottom. Another smooth solid cylinder  $Q$  of same mass and dimensions slides without friction from rest down the inclined plane attaining a speed  $v_q$  at the bottom. The ratio of the speeds

$$\left(\frac{v_q}{v_p}\right) \text{ is}$$

A.  $\sqrt{3/4}$

B.  $\sqrt{3/2}$

C.  $\sqrt{2/3}$

D.  $\sqrt{4/3}$

- 23 A body moves in a circular orbit of radius  $R$  under the action of a central force. Potential due to the central force is given by  $V(r) = kr$  ( $k$  is a positive constant). Period of revolution of the body is proportional to

A.  $R^{1/2}$

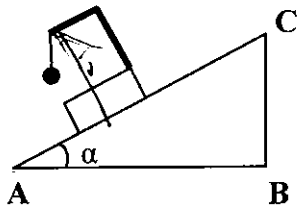
B.  $R^{-1/2}$

C.  $R^{-3/2}$

D.  $R^{-5/2}$



- 24 A simple pendulum is attached to a block which slides without friction down an inclined plane (ABC) having an angle of inclination  $\alpha$  as shown.



While the block is sliding down the pendulum oscillates in such a way that at its mean position the direction of the string is

- A. at angle  $\alpha$  to the perpendicular to the inclined plane AC.  
 B. parallel to the inclined plane AC.  
 C. vertically downwards.  
 D. perpendicular to the inclined plane AC.

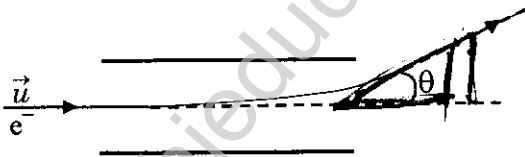
- 25 Water containing air bubbles flows without turbulence through a horizontal pipe which has a region of narrow cross-section. In this region the bubbles

- A. move with greater speed and are smaller than in the rest of the pipe.  
 B. move with greater speed and are larger in size than in the rest of the pipe.  
 C. move with lesser speed and are smaller than in the rest of the pipe.  
 D. move with lesser speed and are of the same size as in the rest of the pipe.

- 26 A solid expands upon heating because
- the potential energy of interaction between atoms in the solid is asymmetric about the equilibrium positions of atoms.
  - the frequency of vibration of the atoms increases.
  - the heating generates a thermal gradient between opposite sides.
  - a fluid called the caloric flows into the interatomic spacing of the solid during heating thereby expanding it.
- 27 Consider two thermometers  $T_1$  and  $T_2$  of equal length which can be used to measure temperature over the range  $\theta_1$  to  $\theta_2$ .  $T_1$  contains mercury as the thermometric liquid while  $T_2$  contains bromine. The volumes of the two liquids are the same at the temperature  $\theta_1$ . The volumetric coefficients of expansion of mercury and bromine are  $18 \times 10^{-5} \text{ K}^{-1}$  and  $108 \times 10^{-5} \text{ K}^{-1}$ , respectively. The increase in length of each liquid is the same for the same increase in temperature. If the diameters of the capillary tubes of the two thermometers are  $d_1$  and  $d_2$  respectively, then the ratio  $d_1:d_2$  would be closest to
- |        |        |
|--------|--------|
| A. 6.0 | B. 2.5 |
| C. 0.6 | D. 0.4 |
- 28 An ideal gas follows a process described by  $PV^2 = C$  from  $(P_1, V_1, T_1)$  to  $(P_2, V_2, T_2)$  ( $C$  is a constant). Then
- if  $P_1 > P_2$  then  $T_2 > T_1$ .
  - if  $V_2 > V_1$  then  $T_2 < T_1$
  - if  $V_2 > V_1$  then  $T_2 > T_1$
  - if  $P_1 > P_2$  then  $V_1 > V_2$

- 29 A whistle emitting a loud sound of frequency 540 Hz is whirled in a horizontal circle of radius 2 m and at a constant angular speed of 15 rad/s. The speed of sound is 330 m/s. The ratio of the highest to the lowest frequency heard by a listener standing at rest at a large distance from the center of the circle is
- A. 1.0  
B. 1.1  
C. 1.2  
D. 1.4
- 30 Monochromatic light passes through a prism. Compared to that in air, inside the prism the light's
- A. speed and wavelength are different but frequency remains same.  
B. speed and frequency are different but wavelength remains same.  
C. wavelength and frequency are different, but speed remains same.  
D. speed, wavelength and frequency are all different.
- 31 The flat face of a plano-convex lens of focal length 10 cm is silvered. A point source placed 30 cm in front of the curved surface will produce a
- A. real image 15 cm away from the lens.  
B. real image 6 cm away from the lens.  
C. virtual image 15 cm away from the lens.  
D. virtual image 6 cm away from the lens.

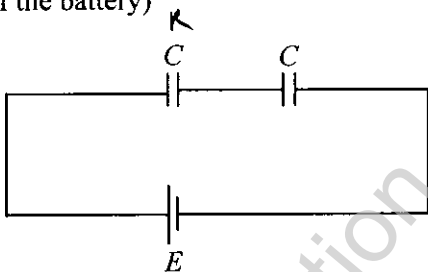
- 32 Two identical metallic square loops  $L_1$  and  $L_2$  are placed next to each other with their sides parallel on a smooth horizontal table. Loop  $L_1$  is fixed and a current which increases as a function of time is passed through it. Then loop  $L_2$
- rotates about its center of mass.
  - moves towards  $L_1$ .
  - remains stationary.
  - moves away from  $L_1$ .
- 33 An electron enters a parallel plate capacitor with horizontal speed  $u$  and is found to deflect by angle  $\theta$  on leaving the capacitor as shown. It is found that  $\tan\theta = 0.4$  and gravity is negligible



If the initial horizontal speed is doubled, then  $\tan\theta$  will be

- 0.1
  - 0.2
  - 0.8
  - 1.6
- 34 Consider a spherical shell of radius  $R$  with a total charge  $+Q$  uniformly spread on its surface (center of the shell lies at the origin  $x = 0$ ). Two point charges,  $+q$  and  $-q$  are brought, one after the other, from far away and placed at  $x = -a/2$  and  $x = +a/2$  ( $a < R$ ), respectively. Magnitude of the work done in this process is
- $(Q+q)^2/4\pi\epsilon_0 a$
  - zero
  - $q^2/4\pi\epsilon_0 a$
  - $Qq/4\pi\epsilon_0 a$

- 38 Two identical parallel plate capacitors of capacitance  $C$  each are connected in series with a battery of emf,  $E$  as shown. If one of the capacitors is now filled with a dielectric of dielectric constant  $k$ , the amount of charge which will flow through the battery is (neglect internal resistance of the battery)



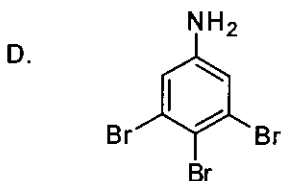
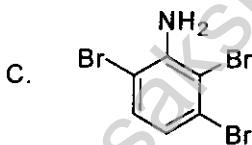
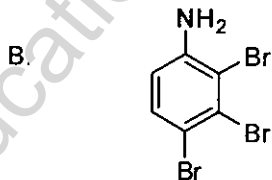
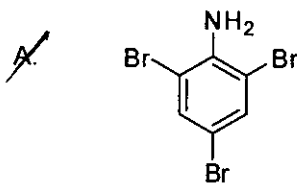
- A.  $\frac{k+1}{2(k-1)}CE$                       B.  $\frac{k-1}{2(k+1)}CE$   
 C.  $\frac{k-2}{k+2}CE$                          D.  $\frac{k+2}{k-2}CE$
- 36 A certain p-n junction, having a depletion region of width  $20 \mu\text{m}$ , was found to have a breakdown voltage of  $100 \text{ V}$ . If the width of the depletion region is reduced to  $1 \mu\text{m}$  during its production, then it can be used as a Zener diode for voltage regulation of
- A.  $5 \text{ V}$                                       B.  $10 \text{ V}$   
 C.  $7.5 \text{ V}$                                     D.  $2000 \text{ V}$
- 37 The half life of a particle of mass  $1.6 \times 10^{-26} \text{ kg}$  is  $6.9 \text{ s}$  and a stream of such particles is travelling with the kinetic energy of a particle being  $0.05 \text{ eV}$ . The fraction of particles which will decay when they travel a distance of  $1 \text{ m}$  is
- A.  $0.1$                                         B.  $0.01$   
 C.  $0.001$                                     D.  $0.0001$

- 38 A 160 watt light source is radiating light of wavelength  $6200 \text{ \AA}$  uniformly in all directions. The photon flux at a distance of  $1.8 \text{ m}$  is of the order of (Planck's constant  $6.63 \times 10^{-34} \text{ J-s}$ )
- $10^2 \text{ m}^{-2} \text{ s}^{-1}$
  - $10^{12} \text{ m}^{-2} \text{ s}^{-1}$
  - $10^{19} \text{ m}^{-2} \text{ s}^{-1}$
  - $10^{25} \text{ m}^{-2} \text{ s}^{-1}$
- 39 The wavelength of the first Balmer line caused by a transition from the  $n = 3$  level to the  $n = 2$  level in hydrogen is  $\lambda_1$ . The wavelength of the line caused by an electronic transition from  $n = 5$  to  $n = 3$  is
- $\frac{375}{128} \lambda_1$
  - $\frac{125}{64} \lambda_1$
  - $\frac{64}{125} \lambda_1$
  - $\frac{128}{375} \lambda_1$
- 40 The binding energy per nucleon of  ${}^5_3\text{B}^{10}$  is  $8.0 \text{ MeV}$  and that of  ${}^5_3\text{B}^{11}$  is  $7.5 \text{ MeV}$ . The energy required to remove a neutron from  ${}^5_3\text{B}^{11}$  is (mass of electron and proton are  $9.11 \times 10^{-31} \text{ kg}$  and  $1.67 \times 10^{-27} \text{ kg}$ , respectively)
- $2.5 \text{ MeV}$ .
  - $8.0 \text{ MeV}$ .
  - $0.5 \text{ MeV}$ .
  - $7.5 \text{ MeV}$ .

## CHEMISTRY

- 41 When 1.88 g of  $\text{AgBr(s)}$  is added to a  $10^{-3}$  M aqueous solution of  $\text{KBr}$ , the concentration of  $\text{Ag}^+$  is  $5 \times 10^{-10}$  M. If the same amount of  $\text{AgBr(s)}$  is added to a  $10^{-2}$  M aqueous solution of  $\text{AgNO}_3$ , the concentration of  $\text{Br}^-$  is
- A.  $9.4 \times 10^{-9}$  M                      B.  $5 \times 10^{-10}$  M  
C.  $1 \times 10^{-11}$  M                      D.  $5 \times 10^{-11}$  M

- 42 Aniline reacts with excess  $\text{Br}_2/\text{H}_2\text{O}$  to give the major product



- 43 The metal with the highest oxidation state present in  $\text{K}_2\text{CrO}_4$ ,  $\text{NbCl}_5$  and  $\text{MnO}_2$  is
- A. Nb                                      B. Mn  
C. K                                      D. Cr

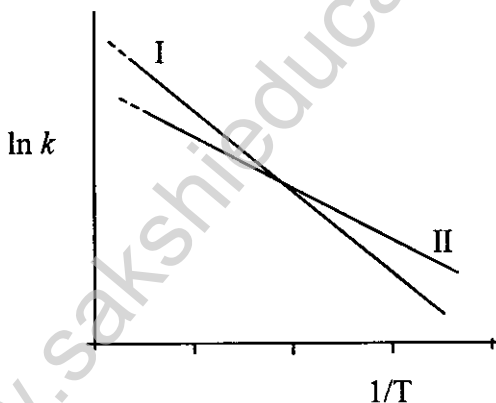
44 The number of geometrical isomers of  $[\text{CrCl}_2(\text{en})(\text{NH}_3)_2]$ , where en = ethylenediamine, is

- A. 2  
B. 3  
C. 4  
D. 1

45 The element that combines with oxygen to give an amphoteric oxide is

- A. N  
B. P  
C. Al  
D. Na

46 The Arrhenius plots of two reactions, I and II are shown graphically



The graph suggests that

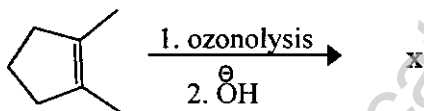
- A.  $E_I > E_{II}$  and  $A_I > A_{II}$   
B.  $E_{II} > E_I$  and  $A_{II} > A_I$   
C.  $E_I > E_{II}$  and  $A_{II} > A_I$   
D.  $E_{II} > E_I$  and  $A_I > A_{II}$



47  $\text{Ni}(\text{CO})_4$  is

- A. tetrahedral and paramagnetic
- B. square planar and diamagnetic**
- C. tetrahedral and diamagnetic
- D. square planar and paramagnetic

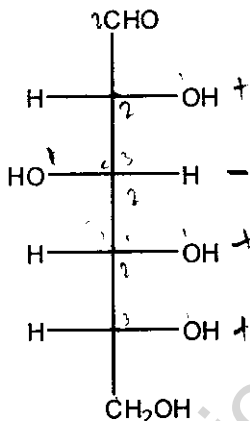
48 In the following reaction,



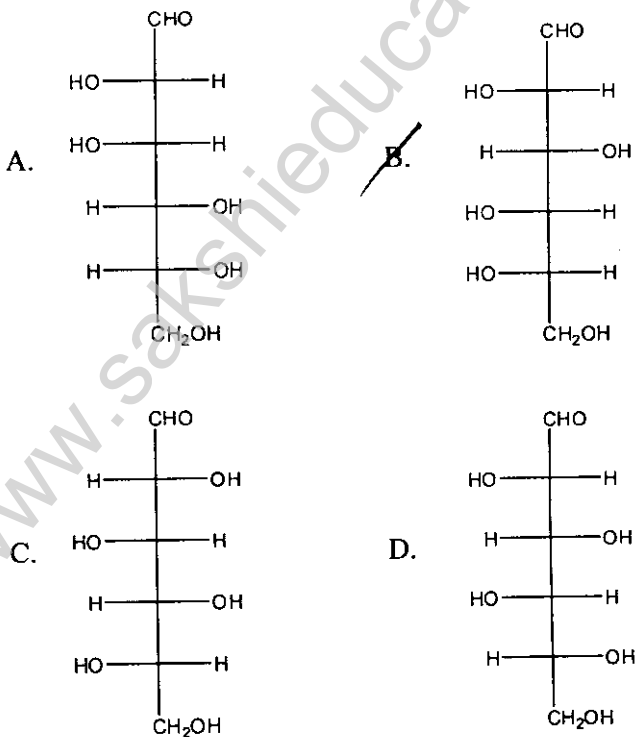
the major product **X** is

- A.**
- B.
- C.
- D.

49 Given the structure of D-(+)-glucose as



The structure of L-(-)-glucose is



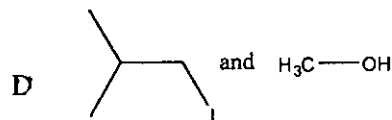
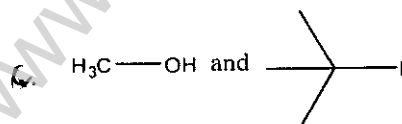
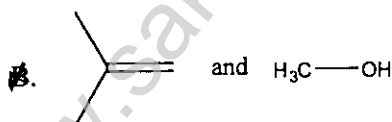
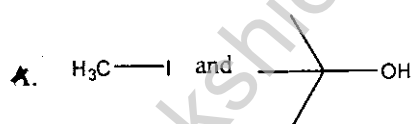
50. In a cubic close packed structure, fractional contributions of an atom at the corner and at the face in the unit cell are, respectively

- A.  $1/8$  and  $1/2$                       B.  $1/2$  and  $1/4$   
 C.  $1/4$  and  $1/2$                       D.  $1/4$  and  $1/8$

51. The equilibrium constant  $K_c$  of the reaction,  $2A \rightleftharpoons B + C$  is 0.5 at  $25^\circ\text{C}$  and 1 atm. The reaction will proceed in the backward direction when concentrations  $[A]$ ,  $[B]$  and  $[C]$  are, respectively

- A.  $10^{-3}$ ,  $10^{-2}$  and  $10^{-2}$  M  
 B.  $10^{-1}$ ,  $10^{-2}$  and  $10^{-2}$  M  
 C.  $10^{-2}$ ,  $10^{-2}$  and  $10^{-3}$  M  
 D.  $10^{-2}$ ,  $10^{-3}$  and  $10^{-3}$  M

52. Major products formed in the reaction of t-butyl methyl ether with HI are



53 If the molar conductivities (in  $S\text{ cm}^2\text{ mol}^{-1}$ ) of NaCl, KCl and NaOH at infinite dilution are 126, 150 and 250, respectively, the molar conductivity of KOH (in  $S\text{ cm}^2\text{ mol}^{-1}$ ) is

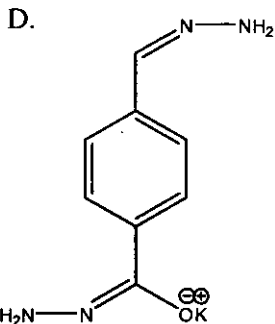
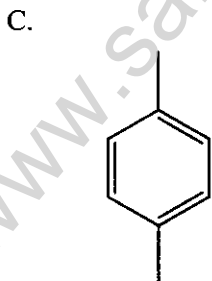
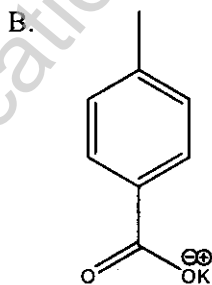
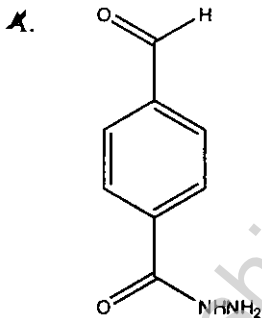
A. 526

B. 226

C. 26

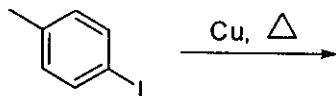
~~D.~~ 274

54 4-Formylbenzoic acid on treatment with one equivalent of hydrazine followed by heating with alcoholic KOH gives the major product

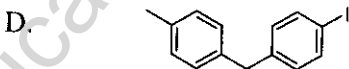
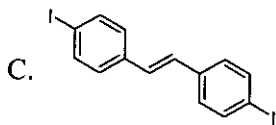
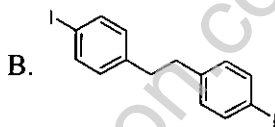
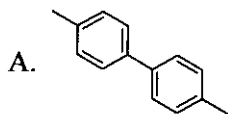


- 55 Two elements, X and Y, have atomic numbers 33 and 17, respectively. The molecular formula of a stable compound formed between them is
- A. XY
  - B. XY<sub>2</sub>
  - C. XY<sub>3</sub>
  - D. XY<sub>4</sub>
- 56 The number of moles of KMnO<sub>4</sub> required to oxidize one equivalent of KI in the presence of sulfuric acid is
- A. 5
  - B. 2
  - C. 1/2
  - D. 1/5
- 57 Three successive measurements in an experiment gave the values 10.9, 11.4042 and 11.42. The correct way of reporting the average value is
- A. 11.2080
  - B. 11.21
  - C. 11.2
  - D. 11
- 58 The latent heat of melting of ice at 0 °C is 6 kJ mol<sup>-1</sup>. The entropy change during the melting in J K<sup>-1</sup> mol<sup>-1</sup> is closest to
- A. 22
  - B. 11
  - C. -11
  - D. -22

59 The major product of the following reaction



is



60 The energies of  $d_{xy}$  and  $d_z^2$  orbitals in octahedral and tetrahedral transition metal complexes are such that

A.  $E(d_{xy}) > E(d_z^2)$  in both tetrahedral and octahedral complexes

B.  $E(d_{xy}) < E(d_z^2)$  in both tetrahedral and octahedral complexes

C.  $E(d_{xy}) > E(d_z^2)$  in tetrahedral but  $E(d_{xy}) < E(d_z^2)$  in octahedral complexes

D.  $E(d_{xy}) < E(d_z^2)$  in tetrahedral but  $E(d_{xy}) > E(d_z^2)$  in octahedral complexes

# BIOLOGY

- 61 In which of the following types of glands is the secretion collected inside the cell and discharged by disintegration of the entire gland?
- A. Apocrine  
B. Merocrine  
C. Holocrine  
D. Epicrine
- 62 Which one of the following interactions does **NOT** promote coevolution?
- A. Commensalism  
B. Mutualism  
C. Parasitism  
D. Interspecific competition
- 63 Stratification is more common in which of the following?
- A. Deciduous forest  
B. Tropical rain forest  
C. Temperate forest  
D. Tropical savannah
- 64 Where is the third ventricle of the brain located?
- A. Cerebrum  
B. Cerebellum  
C. Pons varoli  
D. Diencephalon
- 65 Which of the following is the final product of a gene?
- A. a polypeptide only  
B. an RNA only  
C. either polypeptide or RNA  
D. a nucleotide only

- 66 Forelimbs of whales, bats, humans and cheetah are examples of which of the following processes?
- A. Divergent evolution
  - B. Convergent evolution
  - C. Adaptation
  - D. Saltation
- 67 Which of the following results from conjugation in *Paramecium*?
- A. Cell death
  - B. Cell division
  - C. Budding
  - D. Recombination
- 68 In an experiment investigating photoperiodic response, the leaves of a plant are removed. What is the most likely outcome?
- A. Photoperiodism is not affected
  - B. Photoperiodic response does not occur
  - C. The plant starts flowering
  - D. The plant starts to grow taller
- 69 Testosterone is secreted by which endocrine part of testis?
- A. Leydig cells
  - B. Seminiferous tubules
  - C. Tunica albugenia
  - D. Sertoli cells



- 70 The mutation of a purine to a pyrimidine is known as
- A. transition
  - B. frame shift
  - C. nonsense
  - D. transversion
- 71 Which of the following is secreted at the ends of an axon?
- A. Ascorbic acid
  - B. Acetic acid
  - C. Acetyl choline
  - D. Acetyl CoA
- 72 A bacterial colony is produced from
- A. a single bacterium by its repetitive division
  - B. multiple bacterium without replication
  - C. clumping of two to three bacteria
  - D. a single bacterium without cell division
- 73 Rhinoviruses are the causative agents of
- A. Diarrhoea
  - B. AIDS
  - C. Dengue
  - D. Common cold

- 74 What is the genetic material of Ebola virus?
- A. Single-stranded DNA
  - B. Double-stranded RNA
  - C. Single-stranded RNA
  - D. Double-stranded DNA
- 75 Name the terminal acceptor of electrons in the mitochondrial electron transport chain
- A. Nitrate
  - B. Fumarate
  - C. Succinate
  - D. Oxygen
- 76 Two tubes labeled 'P' and 'Q' contain food stuff. Tube 'P' gave positive test with Benedict's solution while tube 'Q' gave positive test with Nitric acid. Which of the following is correct?
- A. Tube 'P' contains sugar; tube 'Q' contains protein
  - B. Tube 'P' contains protein; tube 'Q' contains sugar
  - C. Both, tube 'P' and tube 'Q' contain sugar
  - D. Both, tube 'P' and tube 'Q' contain protein
- 77 How many linear DNA fragments will be produced when a circular plasmid is digested with a restriction enzyme having 3 sites?
- |      |      |
|------|------|
| A. 4 | B. 5 |
| C. 3 | D. 2 |

- 78 If the humidity of the atmosphere suddenly increases substantially, the water flow in the xylem will
- A. increase
  - B. decrease
  - C. remain unaltered
  - D. increase sharply and then reduce slowly to the pre-existing level
- 79 Which one of the following is the complementary sequence for the DNA with 5'-CGTACTA-3'
- A. 5'-TAGTACG-3'
  - B. 5'-ATCATGC-3'
  - C. 5'-UTCUTGC-3'
  - D. 5'-GCUAGCA-3'
- 80 A diploid plant has 14 chromosomes, but its egg cell has 6 chromosomes. Which one of the following is the most likely explanation of this?
- A. Non-disjunction in meiosis I and II
  - B. Non-disjunction in meiosis I
  - C. Non-disjunction in mitosis
  - D. Normal meiosis



- 84 Let  $n \geq 3$  and let  $C_1, C_2, \dots, C_n$ , be circles with radii  $r_1, r_2, \dots, r_n$ , respectively. Assume that  $C_i$  and  $C_{i+1}$  touch externally for  $1 \leq i \leq n-1$ . It is also given that the  $x$ -axis and the line  $y = 2\sqrt{2}x + 10$  are tangential to each of the circles. Then  $r_1, r_2, \dots, r_n$  are in
- an arithmetic progression with common difference  $3 + \sqrt{2}$
  - a geometric progression with common ratio  $3 + \sqrt{2}$
  - an arithmetic progression with common difference  $2 + \sqrt{3}$
  - a geometric progression with common ratio  $2 + \sqrt{3}$
- 85 The number of integers  $n$  for which  $3x^3 - 25x + n = 0$  has three real roots is
- |       |             |
|-------|-------------|
| A. 1  | B. 25       |
| C. 55 | D. infinite |
- 86 An ellipse inscribed in a semi-circle touches the circular arc at two distinct points and also touches the bounding diameter. Its major axis is parallel to the bounding diameter. When the ellipse has the maximum possible area, its eccentricity is
- |                         |                         |
|-------------------------|-------------------------|
| A. $\frac{1}{\sqrt{2}}$ | B. $\frac{1}{2}$        |
| C. $\frac{1}{\sqrt{3}}$ | D. $\sqrt{\frac{2}{3}}$ |

87 Let  $I_n = \int_0^{\pi/2} x^n \cos x \, dx$ , where  $n$  is a non-negative integer.

Then  $\sum_{n=2}^{\infty} \left( \frac{I_n}{n!} + \frac{I_{n-2}}{(n-2)!} \right)$  equals

A.  $e^{\pi/2} - 1 - \frac{\pi}{2}$

B.  $e^{\pi/2} - 1$

C.  $e^{\pi/2} - \frac{\pi}{2}$

D.  $e^{\pi/2}$

88 For a real number  $x$  let  $[x]$  denote the largest integer less than or equal to  $x$ . The smallest positive integer  $n$  for which the integral  $\int_1^n [x][\sqrt{x}] \, dx$  exceeds 60 is

A. 8

B. 9

C. 10

D.  $[60^{2/3}]$

89 Choose a number  $n$  uniformly at random from the set  $\{1, 2, \dots, 100\}$ . Choose one of the first seven days of the year 2014 at random and consider  $n$  consecutive days starting from the chosen day. What is the probability that among the chosen  $n$  days, the number of Sundays is different from the number of Mondays?

A.  $\frac{1}{2}$

B.  $\frac{2}{7}$

C.  $\frac{12}{49}$

D.  $\frac{43}{175}$

90 Let  $S = \{(a, b) \mid a, b \in \mathbb{Z}, 0 \leq a, b \leq 18\}$ . The number of lines in  $\mathbb{R}^2$  passing through  $(0, 0)$  and exactly one other point in  $S$  is

A. 16

B. 22

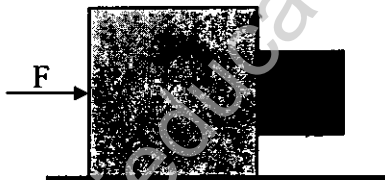
C. 28

D. 32

# PHYSICS

- 91 A solid sphere spinning about a horizontal axis with an angular velocity  $\omega$  is placed on a horizontal surface. Subsequently it rolls without slipping with an angular velocity of
- A.  $2\omega/5$
  - B.  $7\omega/5$
  - C.  $2\omega/7$
  - D.  $\omega$

- 92 Consider the system shown below.



A horizontal force  $F$  is applied to a block  $X$  of mass  $8\text{ kg}$  such that the block  $Y$  of mass  $2\text{ kg}$  adjacent to it does not slip downwards under gravity. There is no friction between the horizontal plane and the base of the block  $X$ . The coefficient of friction between the surfaces of blocks  $X$  and  $Y$  is  $0.5$ . Take acceleration due to gravity to be  $10\text{ ms}^{-2}$ . The minimum value of  $F$  is

- A.  $200\text{ N}$
- B.  $160\text{ N}$
- C.  $40\text{ N}$
- D.  $240\text{ N}$

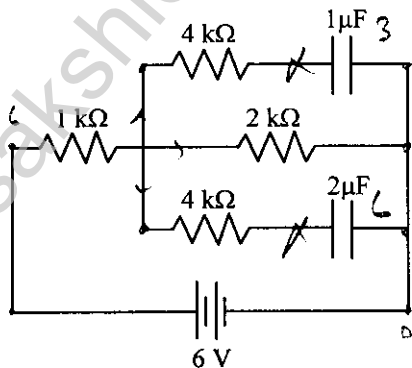




- 96 The angles of incidence and refraction of a monochromatic ray of light of wavelength  $\lambda$  at an air-glass interface are  $i$  and  $r$ , respectively. A parallel beam of light with a small spread  $\delta\lambda$  in wavelength about a mean wavelength  $\lambda$  is refracted at the same air-glass interface. The refractive index  $\mu$  of glass depends on the wavelength  $\lambda$  as  $\mu(\lambda) = a + b/\lambda^2$  where  $a$  and  $b$  are constants. Then the angular spread in the angle of refraction of the beam is

- A.  $\left| \frac{\sin i}{\lambda^3 \cos r} \delta\lambda \right|$   
 B.  $\left| \frac{2b}{\lambda^3} \delta\lambda \right|$   
 C.  $\left| \frac{2b \tan r}{a\lambda^3 + b\lambda} \delta\lambda \right|$   
 D.  $\left| \frac{2b(a + b/\lambda^2) \sin i}{\lambda^3} \delta\lambda \right|$

- 97 What are the charges stored in the  $1 \mu\text{F}$  and  $2 \mu\text{F}$  capacitors in the circuit below, once the currents become steady?



- A.  $8 \mu\text{C}$  and  $4 \mu\text{C}$  respectively  
 B.  $4 \mu\text{C}$  and  $8 \mu\text{C}$  respectively  
 C.  $3 \mu\text{C}$  and  $6 \mu\text{C}$  respectively  
 D.  $6 \mu\text{C}$  and  $3 \mu\text{C}$  respectively

98 A 1.5 kW (kilo-watt) laser beam of wavelength  $6400 \text{ \AA}$  is used to levitate a thin aluminium disk of same area as the cross section of the beam. The laser light is reflected by the aluminium disk without any absorption. The mass of the foil is close to

- A.  $10^{-9} \text{ kg}$
- B.  $10^{-3} \text{ kg}$
- C.  $10^{-4} \text{ kg}$
- D.  $10^{-6} \text{ kg}$

99 When ultraviolet radiation of a certain frequency falls on a potassium target, the photoelectrons released can be stopped completely by a retarding potential of 0.6 V. If the frequency of the radiation is increased by 10%, this stopping potential rises to 0.9 V. The work function of potassium is

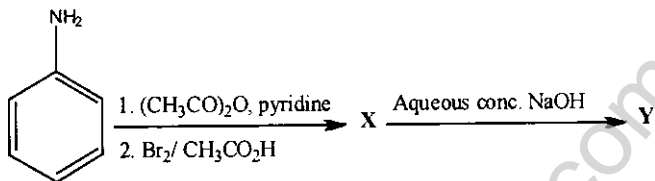
- A. 2.0 eV
- B. 2.4 eV
- C. 3.0 eV
- D. 2.8 eV

100 The dimensions of Stefan-Boltzmann constant  $\sigma$  can be written in terms of Planck's constant  $h$ , Boltzmann constant  $k_B$  and the speed of light  $c$  as  $\sigma = h^\alpha k_B^\beta c^\gamma$ . Here

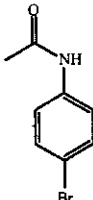
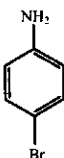
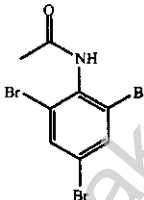
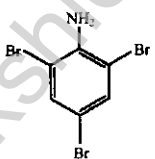
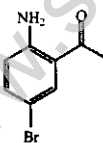
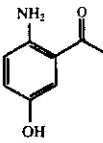
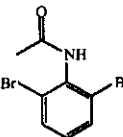
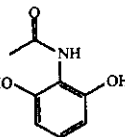
- A.  $\alpha = 3, \beta = 4$  and  $\gamma = -3$
- B.  $\alpha = 3, \beta = -4$  and  $\gamma = 2$
- C.  $\alpha = -3, \beta = 4$  and  $\gamma = -2$
- D.  $\alpha = 2, \beta = -3$  and  $\gamma = -1$

## CHEMISTRY

101 In the reaction sequence



X and Y are, respectively,

- A.  , 
- B.  , 
- C.  , 
- D.  , 



106 The radius of  $K^+$  is 133 pm and that of  $Cl^-$  is 181 pm. The volume of the unit cell of KCl expressed in  $10^{-22} \text{ cm}^3$  is

- A. 0.31
- B. 1.21
- C. 2.48
- D. 6.28

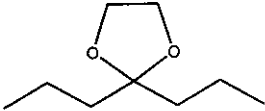
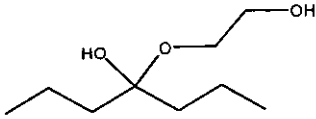
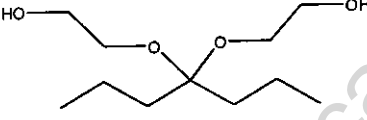
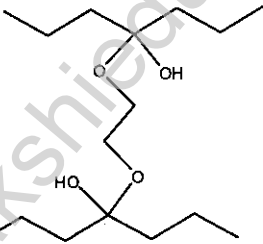
107 The reaction,  $K_2Cr_2O_7 + m FeSO_4 + n H_2SO_4 \rightarrow Cr_2(SO_4)_3 + p Fe_2(SO_4)_3 + K_2SO_4 + q H_2O$  when balanced, m, n, p, and q are, respectively

- A. 6, 14, 3, 14
- B. 6, 7, 3, 7
- C. 3, 7, 2, 7
- D. 4, 14, 2, 14

108 The standard free energy change (in J) for the reaction  $3Fe^{2+}(aq) + 2Cr(s) = 2Cr^{3+}(aq) + 3Fe(s)$  given  $E_{Fe^{2+}/Fe}^{\circ} = -0.44 \text{ V}$  and  $E_{Cr^{3+}/Cr}^{\circ} = -0.74 \text{ V}$  is ( $F = 96500 \text{ C}$ )

- A. 57,900
- B. -57,900
- C. -173,700
- D. 173,700

109 Calcium butanoate on heating followed by treatment with 1,2-ethanediol in the presence of catalytic amount of an acid, produces a major product which is

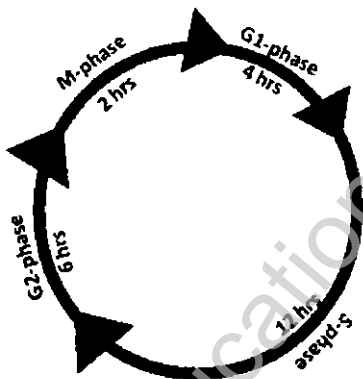
- A. 
- B. 
- C. 
- D. 

110  $\text{XeF}_6$  on complete hydrolysis yields 'X'. The molecular formula of X and its geometry, respectively, are

- A.  $\text{XeO}_2$  and linear
- B.  $\text{XeO}_3$  and trigonal planar -
- C.  $\text{XeO}_3$  and pyramidal -
- D.  $\text{XeO}_4$  and tetrahedral

# BIOLOGY

- 111 Following the cell cycle scheme given below, what is the probability that a cell would be in M-phase at any given time?



- A.  $1/24$   
B.  $1/12$   
C.  $1/6$   
D.  $1/2$
- 112 A flower with Tt genotype is cross-pollinated by TT pollens. What will the genotypes of the resulting endosperm and embryo, respectively, be?
- A. TTT, (TT + Tt)  
B. (TTT + TTt), TT  
C. TTt, Tt  
D. TTt, (TT + Tt)

- 113 A new life form discovered on a distant planet has a genetic code consisting of five unique nucleotides and only one stop codon. If each codon has four bases, what is the maximum number of unique amino acids this life form can use?
- A. 624
  - B. 20
  - C. 124
  - D. 3124
- 114 A spontaneous mutation results in a couple having only female progeny. When the daughter marries and has children, none of them are males. However, in the third generation there are few male offspring. What is the most likely explanation of this observation?
- A. The mutation reverses spontaneously in the third generation
  - B. The mutation occurs on the X chromosome and is both recessive and lethal
  - C. The mutation occurs on the X chromosome and is both recessive and dominant
  - D. The mutation occurs on an autosome and is dominant



- 115 A circular plasmid of 10,000 base pairs (bp) is digested with two restriction enzymes, A and B, to produce a 3000 bp and a 2000 bp bands when visualised on an agarose gel. When digested with one enzyme at a time, only one band is visible at 5000 bp. If the first site for enzyme A (A1) is present at the 100<sup>th</sup> base, the order in which the remaining sites (A2, B1 and B2) are present is
- A. 3100, 5100, 8100
  - B. 8100, 3100, 5100
  - C. 5100, 3100, 8100
  - D. 8100, 5100, 3100
- 116 After meiosis-II, daughter cells differ from the parent cells and each other in their genotypes. This can occur because of which one of the following mechanism(s)?
- A. Only synaptic crossing over
  - B. Only crossing over and independent assortment of chromosomes
  - C. Only crossing over and chromosomal segregation
  - D. Crossing over, independent assortment and segregation of chromosomes

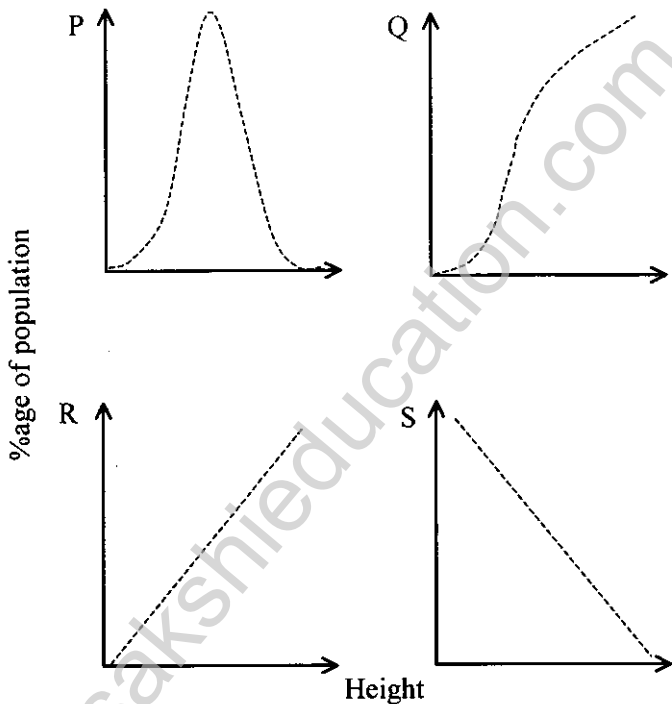
117 A desert lizard (an ectotherm) and a mouse (an endotherm) are placed inside a chamber at  $15^{\circ}\text{C}$  and their body temperatures [ $T(L)$  for the lizard and  $T(M)$  for the mouse] and metabolic rates [ $M(L)$  for the lizard and  $M(M)$  for the mouse] are monitored. Which one of the following is correct?

- A.  $T(L)$  and  $M(L)$  will fall while  $T(M)$  and  $M(M)$  will increase
- B.  $T(L)$  and  $M(L)$  will increase while  $T(M)$  and  $M(M)$  will fall
- C.  $T(L)$  and  $M(L)$  will fall,  $T(M)$  will remain same and  $M(M)$  will increase
- D.  $T(L)$  and  $M(L)$  will remain same and  $T(M)$  and  $M(M)$  will decrease

118 In Griffith's experiments mice died when injected with

- A. heat killed S-strain
- B. heat killed S-strain combined with R-strain
- C. heat killed R-strain
- D. live R-strain

- 119 Human height is a multigenic character. If the heights of all the individuals living in a metropolis are measured and the percentages of the population belonging to a specific height are plotted as shown below, which of the plots would represent the most realistic distribution?



- A. P  
B. Q  
C. R  
D. S

- 120 If mitochondria isolated from a cell are first placed without carbon source in a buffer at pH 8.0 and then transferred to a buffer at pH 4, it will lead to
- A. an increase in intra-mitochondrial acidity  
B. a decrease in intra-mitochondrial acidity  
C. blockage of ATP synthesis  
D. synthesis of ATP