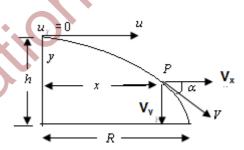
# www.sakshieducation.com <a href="https://www.sakshieducation.com">Horizontal projection</a>

- 1. Consider a body horizontally from the top of a tower with a velocity 'u'.
  - a) It reaches the ground along a parabolic path.
  - b) Its time of descent is  $\sqrt{2h/g}$ .
  - c) The horizontal displacement is  $R = u\sqrt{2h/g}$
  - d) The angle  $\square$  with which it strikes the ground is given by  $\tan \square \square \frac{\sqrt{2h/g}}{u} = \frac{gt}{u}$
  - e) The velocity with which it hits the ground is given by  $v = \sqrt{u^2 + 2gh}$  or  $v = \sqrt{u^2 + (gt)^2}$ .

#### Position after time t

Horizontal displacement, x = u t

Vertical displacement,  $y = \frac{1}{2}gt^2$ 



### 2. Velocity after time t

$$v = \sqrt{u^2 + (gt)^2} = \sqrt{u^2 + 2gh}$$

If angle made with the horizontal is  $\Box$   $\tan \alpha = \frac{gt}{u} = \frac{gt}{\sqrt{2gh}}$ .

## 3. Equation of path

$$y = \frac{1}{2}g\frac{x^2}{u^2}$$

- **4.** Form a certain height. If two bodies are projected horizontally with velocities  $u_1$  and  $u_2$  in opposite directions.
  - a) Time after which velocity vectors are perpendicular is  $t = \frac{\sqrt{u_1 u_2}}{g}$
  - b) Time after which displacement vectors are perpendicular is  $t = \frac{2\sqrt{u_1u_2}}{g}$
  - c) Distance between the two bodies when velocity vectors are perpendicular is  $\frac{\sqrt{u_1u_2}}{\alpha}(u_1+u_2)$

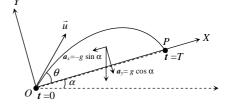
- d) Horizontal distance between the two bodies when displacement vectors' are  $2\frac{\sqrt{u_1u_2}}{\sigma}(u_1+u_2)$ perpendicular is
- 5. Body is dropped from the window of the moving train. The path of the body appears as
  - a) Vertical straight line for an observer in the train
  - b) Parabolic for an observer outside the train
- **6.** From the top of a tower a stone is dropped and simultaneously another stone is projected horizontally with a uniform velocity. Both of them reach the ground simultaneously.
- 7. Motion of a body along an inclined plane
  - a) A body is projected up with a speed u from an inclined plane which makes an angle  $\alpha$  with the horizontal and velocity of projection makes an angle  $\theta$  with the inclined plane.
  - b) The component of initial velocity parallel and perpendicular to the plane are equal to  $u \cos \theta$  and  $u \sin \theta$  respectively i.e.  $u_{\parallel} = u \cos \theta$  and  $u_{\perp} = u \sin \theta$ .
  - c) The component of g along the plane is  $g \sin \alpha$  and perpendicular to the plane is  $g \cos \alpha$  as shown in the figure *i.e.*  $a_{\parallel} = -g \sin \alpha$  and  $a_{\perp} = g \cos \alpha$ .
  - d) Time of flight

Time of flight on an inclined plane  $T = \frac{2u_{\perp}}{a}$ 

$$T = \frac{2u\sin\theta}{g\cos\alpha}$$

c) Maximum height

Maximum height on an inclined plane  $H = \frac{u_{\perp}^2}{2a_{\perp}}$ 



$$H = \frac{u^2 \sin^2 \theta}{2 a \cos \theta}$$

d) Horizontal range

$$R = \frac{2u^2}{g} \frac{\sin \theta \cos(\theta + \alpha)}{\cos^2 \alpha}$$

(i) Maximum range occurs when  $\theta = \frac{\pi}{4} - \frac{\alpha}{2}$ 

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(ii) The maximum range along the inclined plane when the projectile is thrown upwards is given by

$$R_{\text{max}} = \frac{u^2}{g(1+\sin\alpha)}$$

(iii) The maximum range along the inclined plane when the projectile is thrown downwards is given by

$$R_{\text{max}} = \frac{u^2}{g(1-\sin\alpha)} \quad \text{and} \quad T^2g = 2R_{\text{max}}$$