

Cells

1. Electric Cell

- a) It is a device which converts chemical energy into electrical energy.
- b) There are two types of cells
 - i) Primary cell
 - ii) Secondary cell

2. Electromotive force (e.m.f) of a Cell

- a) The work done in carrying a unit positive charge once in the whole circuit including the cell, is defined as the electromotive force.
- b) Electromotive force is the potential difference between the terminals of a cell in open circuit.
- c) Electromotive force depends on (1) nature of electrolyte (2) metal of the electrodes.
- d) Electromotive force does not depend on (1) area of plates (2) distance between the electrodes (3) Quantity of electrolyte (4) size of the cell.
- e) Electromotive force is the characteristic property of the cell. The direction of current inside the cell is always from negative to positive electrode.
- f) The unit of electromotive force is volt.

3. Internal resistance (r):

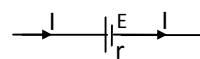
The internal resistance of a cell is the resistance offered by the column of the electrolyte between the positive plate and the negative plate.

- i) The internal resistance of a perfect cell or ideal cell is zero.
- ii) Internal resistance depends on
 - a) Strength of electrolyte ($r \propto \text{strength}$)
 - b) Distance between plates ($r \propto d$)
 - c) Area of the plates $\left[r \propto \frac{1}{A} \right]$
 - d) Temperature of electrolyte $\left[r \propto \frac{1}{t} \right]$

4. Relation between EMF and PD

1) In case of charging of a cell

a) The current flows from +ve to -ve terminal inside the cell.



b) $V > E$

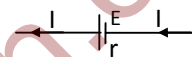
c) $V = E + ir$

2) In case of discharge of a cell

a) The current flows from -ve to +ve terminal inside the cells

b) $V < E$

c) $V = E - ir$



3) The difference between E and V is called **lost volts**

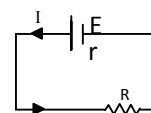
$$\therefore \text{Lost volts} = E - V = ir$$

4) A cell of emf ' E ' and its resistance ' r ' is connected to resistance ' R '.

a) $i = \frac{E}{R + r}$

b) P.D. across resistance R is given by

$$V = iR = \frac{ER}{R + r}$$



c) Fraction of energy useful $= \frac{V}{E} = \frac{R}{R + r}$

d) % of fractional useful energy $= \left(\frac{V}{E} \right) 100 = \left(\frac{R}{R + r} \right) 100$

e) Fraction of energy lost $= \frac{E - V}{E} = \frac{ir}{E} = \frac{r}{R + r}$

f) % of lost energy $= \left(\frac{r}{R + r} \right) 100$

g) $r = \frac{(E - V)R}{V}$

h) For single cell, the condition for maximum current is $R = r$.

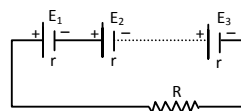
5. Back emf

a) The copper electrode gets covered with a layer of hydrogen and this hinders flow of current. In the neighbourhood of both electrodes, the concentrations of

ions get altered. This results in an emf acting in a direction opposite to the emf of the cell. This is called back emf.

- b) This formation of hydrogen around the anode is called polarization.
- c) To reduce the back e.m.f manganese dioxide and potassium dichromate are added to electrolyte of cell. These are called **depolarizers**.

6. Series combination of cells



- a) $E = E_1 + E_2 + E_3 + \dots E_n$
- b) $r = r_1 + r_2 + r_3 + \dots r_n$
- c) When cells of e.m.f. are E_1, E_2 , and $E_3 \dots$ and of internal resistances $r_1, r_2, r_3 \dots$ are connected in series across an external resistance R , the current i is given by

$$i = \frac{E_1 + E_2 + E_3 \dots}{R + (r_1 + r_2 + r_3 + \dots)}$$

- d) If the e.m.f s of all the n cells and their internal resistances are same, then
- $$i = \frac{nE}{(R + nr)}$$
- e) If $n r \gg R$, then $i = E/r$, i.e. the current obtained from n cells is equal to that obtained from a single cell.
 - f) If $n r \ll R$ then $i = n E/R$.
 - g) This type of combination is used when the internal resistance of battery is negligible in comparison to the external resistance and e.m.f required is high.
 - h) In this combination same current flows through all the cells.

7. Wrongly connected cells

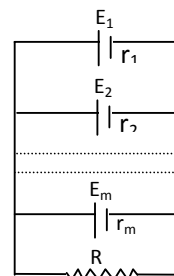
Suppose by mistake m cells are wrongly connected in above circuit then

- a) Total emf = emf due to properly connected cells – emf due to wrongly connected cells

$$= (n - m) E - mE = (n - 2m) E$$

- b) Total internal resistance of cells = nr
- c) Total resistance in the circuit = $R + nr$

- d) The current in circuit = $\frac{(n - 2m)E}{R + nr}$



8. Cell in parallel

i) $i = i_1 + i_2 + i_3 + \dots i_n$

ii) The e.m.f of the combination is equal to the e.m.f of a single cell i.e. $E = E_1 = E_2$

$$= E_3 = \dots i = \frac{E}{\left(R + \frac{r}{m}\right)}$$

iii) If $r \gg R$ then $I = mE/r$

$$i = n \times (\text{current obtained from a single cell})$$

iv) If $r \ll R$ then $i = E/R$

This type of combination is used when $r \gg R$ and more current is required in the circuit.

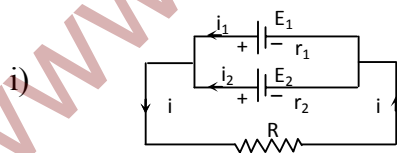
v) If the e.m.f of m cells and their internal resistance are different then

1) $i = i_1 + i_2 + i_3 \dots i_n$

$$2) I = \frac{\left[\frac{E_1}{r_1} + \frac{E_2}{r_2} + \dots \frac{E_m}{r_n}\right]}{\left[1 + R\left(\frac{1}{r_1} + \frac{1}{r_2} + \dots \frac{1}{r_n}\right)\right]} = \frac{\left(\frac{\sum E}{\sum \frac{1}{r}}\right)}{\left(R + \frac{1}{\sum \frac{1}{r}}\right)}$$

$$3) E_{\text{total}} = \frac{\sum \frac{E}{r}}{\sum \frac{1}{r}} \quad 4) r_{\text{total}} = \frac{1}{\sum \frac{1}{r}}$$

9. If two cells of emf E_1 and E_2 having internal resistances r_1 and r_2 are connected in parallel to an external resistance R , then



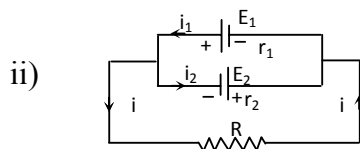
a) The effective emf, $E = \frac{E_1 r_2 + E_2 r_1}{r_1 + r_2}$

b) The effective internal resistance, $r = \frac{r_1 r_2}{r_1 + r_2}$

c) Current through the circuit, $i = \frac{E}{r + R}$

d) $i = i_1 + i_2$

e) $i_1 = \frac{E_1 - iR}{r_1}$ and $i_2 = \frac{E_2 - iR}{r_2}$



a) The effective emf, $E = \frac{E_1 r_2 + E_2 r_1}{r_1 + r_2}$

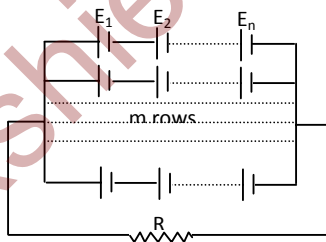
b) The effective internal resistance, $r = \frac{r_1 r_2}{r_1 + r_2}$

c) Current through the circuit, $i = \frac{E}{r + R}$

d) $i = i_1 - i_2$

e) $i_1 = \frac{E_1 - iR}{r_1}$ and $i_2 = \frac{E_2 + iR}{r_2}$

10. Mixed grouping of cells



i) The e.m.f of cells in a row = nE .

ii) Total e.m.f of the combination = nE

iii) The total internal resistance = $\frac{nr}{m}$

iv) The total resistance of the circuit = $R + \frac{nr}{m}$

v) The current flowing through the external resistance (i) = $\frac{nE}{R + \frac{nr}{m}} = \frac{mnE}{mR + nr}$

- vi) For maximum current to flow through the external circuit, the external resistance should be equal to the total internal resistance. or $R = \frac{nr}{m}$ or, $mR = nr$

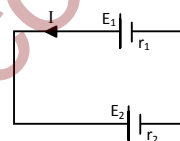
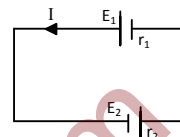
11. Two cells of e.m.f.s E_1 and E_2 be connected in a circuit. Let r_1 and r_2 be the internal resistance of the cells.

a) The current through the circuit $I = \frac{E_1 + E_2}{r_1 + r_2}$

b) The terminal voltage across the cells

$$V_1 = E_1 - Ir_1$$

$$V_2 = E_2 - Ir_2$$



12. Let two cells of e.m.f.s E_1 and E_2 be connected in parallel in a circuit.

Let r_1 and r_2 be the internal resistance of the cells.

a) The direction of the resultant current is determined by the direction of the higher e.m.f.

b) If $E_1 < E_2$, the current through the circuit is $I = \frac{E_1 - E_2}{r_1 + r_2}$.

c) While the cell E_1 is discharging, the cell E_2 is in the charging. The terminal voltage across the cells $V_1 = E_1 - Ir_1$ and $V_2 = E_2 + Ir_2$.