



$$\frac{(X-Y)^2}{2} + 6\frac{(X-Y)(X+Y)}{2} + 8\frac{(X+Y)^2}{2} = 10$$

$$\Rightarrow 15x^2 + 14xy + 3y^2 = 20$$

5. The coordinate axes are rotated through an angle  $135^\circ$ . If the coordinates of a point P in the new system are known to be  $(4, -3)$ , then the coordinates of P in the original system are

[EAMCET 2003]

- 1)  $\left(\frac{1}{\sqrt{2}}, \frac{7}{\sqrt{2}}\right)$     2)  $\left(\frac{1}{\sqrt{2}}, \frac{-7}{\sqrt{2}}\right)$     3)  $\left(\frac{-1}{\sqrt{2}}, \frac{-7}{\sqrt{2}}\right)$     4)  $\left(\frac{-1}{\sqrt{2}}, \frac{7}{2}\right)$

Ans: 4

Sol.  $x = 4 \cos 135^\circ - (-3) \sin 135^\circ = -\frac{1}{\sqrt{2}}$

$$y = 4 \sin 135^\circ + (-3) \cos 135^\circ = \frac{7}{\sqrt{2}}$$

6. If the axes are rotated through an angle  $45^\circ$  in the positive direction without changing the origin, then the coordinates of the point  $(\sqrt{2}, 4)$  in the old system are

[EAMCET 2002]

- 1)  $(1 - 2\sqrt{2}, 1 + 2\sqrt{2})$     2)  $(1 + 2\sqrt{2}, 1 - 2\sqrt{2})$   
 3)  $(2\sqrt{2}, \sqrt{2})$     4)  $(\sqrt{2}, \sqrt{2})$

Ans: 1

Sol.  $x = X \cos \theta - y \sin \theta$  given  $(X, Y) = (\sqrt{2}, 4)$

$$y = X \sin \theta + Y \cos \theta \text{ and } \theta = \frac{\pi}{4}$$

7. The coordinate axes are rotated about the origin O in the counter-clockwise direction through an angle  $60^\circ$ . If p and q are the intercepts made on the new axes by a straight line whose equation referred to the original axes is  $x + y = 1$ , then

$$\frac{1}{p^2} + \frac{1}{q^2} = \quad \text{[EAMCET 2000]}$$

- 1) 1    2) 4    3) 6    4) 8

Ans: 1

Sol. The perpendicular distance from origin to  $x + y = 1$  and  $\frac{x}{p} + \frac{y}{q} = 1$  are equal

$$\therefore \frac{1}{p^2} + \frac{1}{q^2} = 1$$

