

**SB/
SX**

KVPY QUESTION PAPER – STREAM SB/SX

November 04, 2012

PART I

One-Mark Questions

MATHEMATICS

- 1 Three children, each accompanied by a guardian, seek admission in a school. The principal wants to interview all the 6 persons one after the other subject to the condition that no child is interviewed before its guardian. In how many ways can this be done?
- A. 60 B. 90 C. 120 D. 180
- 2 In the real number system, the equation $\sqrt{x+3} - 4\sqrt{x-1} + \sqrt{x+8} - 6\sqrt{x-1} = 1$ has
- A. no solution
B. exactly two distinct solutions
C. exactly four distinct solutions
D. infinitely many solutions
- 3 The maximum value M of $3^x + 5^x - 9^x + 15^x - 25^x$, as x varies over reals, satisfies
- A. $3 < M < 5$ C. $0 < M < 2$
B. $9 < M < 25$ D. $5 < M < 9$
- 4 Suppose two perpendicular tangents can be drawn from the origin to the circle $x^2 + y^2 - 6x - 2py + 17 = 0$, for some

real p . Then $|p|$ is equal to

- A. 0 B. 3 C. 5 D. 17

- 5 Let a, b, c, d be numbers in the set $\{1, 2, 3, 4, 5, 6\}$ such that the curves $y = 2x^3 + ax + b$ and $y = 2x^3 + cx + d$ have no point in common. The maximum possible value of $(a-c)^2 + b-d$ is

- A. 0 B. 5 C. 30 D. 36

- 6 Consider the conic $ex^2 + \pi y^2 - 2e^2x - 2\pi^2y + e^3 + \pi^3 = \pi e$. Suppose P is any point on the conic and S_1, S_2 are the foci of the conic, then the maximum value of $(PS_1 + PS_2)$ is

- A. πe B. $\sqrt{\pi e}$ C. $2\sqrt{\pi}$ D. $2\sqrt{e}$

- 7 Let $f(x) = \frac{\sin(x-a) + \sin(x+a)}{\cos(x-a) - \cos(x+a)}$, then

- A. $f(x+2\pi) = f(x)$ but $f(x+\alpha) \neq f(x)$ for any $0 < \alpha < 2\pi$
B. f is a strictly increasing function
C. f is a strictly decreasing function
D. f is a constant function

- 8 The value of $\tan 81^\circ - \tan 63^\circ - \tan 27^\circ + \tan 9^\circ$ is

- A. 0 B. 2 C. 3 D. 4

- 9 The mid-point of the domain of the function $f(x) = \sqrt{4 - \sqrt{2x+5}}$ for real x is

- A. $\frac{1}{4}$ B. $\frac{3}{2}$ C. $\frac{2}{3}$ D. $-\frac{2}{5}$

- 10 Let n be a natural number and let a be a real number. The number of zeros of $x^{2n+1} - (2n+1)x + a = 0$ in the interval $[-1, 1]$ is

- A. 2 if $a > 0$ C. at most one for every value of a
B. 2 if $a < 0$ D. at least three for every value of a

- 11 Let $f: \mathbb{R} \rightarrow \mathbb{R}$ be the function

$$f(x) = (x-a_1)(x-a_2) + (x-a_2)(x-a_3) + (x-a_3)(x-a_1)$$

with $a_1, a_2, a_3 \in \mathbb{R}$. Then $f(x) \geq 0$ if and only if

- A. at least two of a_1, a_2, a_3 are equal
B. $a_1 = a_2 = a_3$
C. a_1, a_2, a_3 are all distinct
D. a_1, a_2, a_3 are all positive and distinct

- 12 The value $\frac{\int_0^{\pi/2} (\sin x)^{\sqrt{2}+1} dx}{\int_0^{\pi/2} (\sin x)^{\sqrt{2}-1} dx}$ is

- A. $\frac{\sqrt{2}+1}{\sqrt{2}-1}$ B. $\frac{\sqrt{2}-1}{\sqrt{2}+1}$ C. $\frac{\sqrt{2}+1}{\sqrt{2}}$ D. $2 - \sqrt{2}$

- 13 The value $\int_{-2012}^{2012} (\sin(x^3) + x^5 + 1) dx$ is
 A. 2012 B. 2013 C. 0 D. 4024
- 14 Let $[x]$ and $\{x\}$ be the integer part and fractional part of a real number x respectively. The value of the integral $\int_0^5 [x]\{x\} dx$ is
 A. 5/2 B. 5 C. 34.5 D. 35.5
- 15 Let $S_n = \sum_{k=1}^n k$ denote the sum of the first n positive integers. The numbers $S_1, S_2, S_3, \dots, S_{99}$ are written on 99 cards. The probability of drawing a card with an even number written on it is
 A. $\frac{1}{2}$ B. $\frac{49}{100}$ C. $\frac{49}{99}$ D. $\frac{48}{99}$
- 16 A purse contains 4 copper coins and 3 silver coins. A second purse contains 6 copper coins and 4 silver coins. A purse is chosen randomly and a coin is taken out of it. What is the probability that it is a copper coin?
 A. $\frac{41}{70}$ B. $\frac{31}{70}$ C. $\frac{27}{70}$ D. $\frac{1}{3}$
- 17 Let H be the orthocentre of an acute-angled triangle ABC and O be its circumcenter. Then

$$\overline{HA} + \overline{HB} + \overline{HC}$$

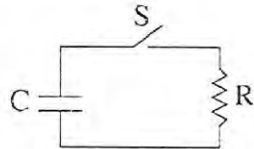
- A. is equal to \overline{HO}
 B. is equal to $3\overline{HO}$
 C. is equal to $2\overline{HO}$
 D. is not a scalar multiple of \overline{HO} in general
- 18 The number of ordered pairs (m, n) , where $m, n \in \{1, 2, 3, \dots, 50\}$, such that $6^m + 9^n$ is a multiple of 5 is
 A. 1250 B. 2500 C. 625 D. 500
- 19 Suppose $a_1, a_2, a_3, \dots, a_{2012}$ are integers arranged on a circle. Each number is equal to the average of its two adjacent numbers. If the sum of all even indexed numbers is 3018, what is the sum of all numbers?
 A. 0 B. 1509 C. 3018 D. 6036
- 20 Let $S = \{1, 2, 3, \dots, n\}$ and $A = \{(a, b) \mid 1 \leq a, b \leq n\} = S \times S$. A subset B of A is said to be a *good* subset if $(x, x) \in B$ for every $x \in S$. Then the number of *good* subsets of A is
 A. 1 B. 2^n C. $2^{n(n-1)}$ D. 2^{n^2}

PHYSICS

- 21 An ideal monatomic gas expands to twice its volume. If the process is isothermal, the magnitude of work done by the gas is W_i . If the process is adiabatic, the magnitude of work done by the gas is W_a . Which of the following is true?

- A. $W_i = W_a > 0$ C. $W_i > W_a = 0$
 B. $W_i > W_a > 0$ D. $W_a > W_i = 0$

- 22 The capacitor of capacitance C in the circuit shown is fully charged initially. Resistance is R .



After the switch S is closed, the time taken to reduce the stored energy in the capacitor to half its initial value is

- A. $RC/2$ C. $2RC \ln 2$
 B. $RC \ln 2$ D. $\frac{RC \ln 2}{2}$

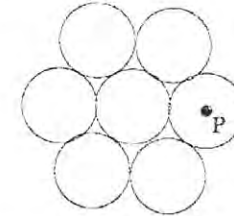
- 23 A liquid drop placed on a horizontal plane has a near spherical shape (slightly flattened due to gravity). Let R be the radius of its largest horizontal section. A small disturbance causes the drop to vibrate with frequency ν about its equilibrium shape. By dimensional analysis the ratio

$$\frac{\nu}{\sqrt{\frac{\sigma}{\rho R^3}}}$$

can be (Here σ is surface tension, ρ is density, g is acceleration due to gravity, and k is an arbitrary dimensionless constant.)

- A. $k\rho g R^2 / \sigma$ C. $k\rho R^2 / g\sigma$
 B. $k\rho R^3 / g\sigma$ D. $k\rho / g\sigma$

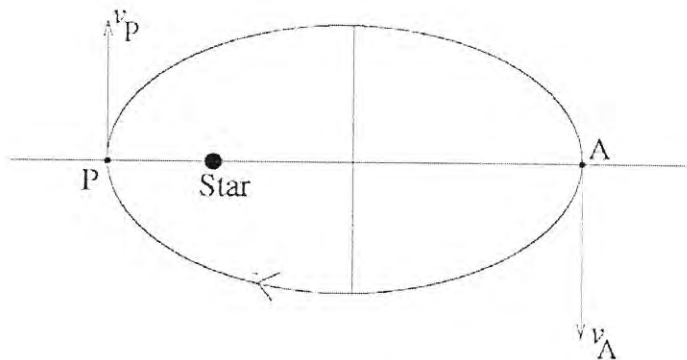
- 24 Seven identical coins are rigidly arranged on a flat table in the pattern shown below so that each coin touches its neighbours. Each coin is a thin disc of mass m and radius r . Note that the moment of inertia of an individual coin about an axis passing through center and perpendicular to the plane of the coin is $\frac{mr^2}{2}$.



The moment of inertia of the system of seven coins about an axis that passes through the point P (the centre of the coin positioned directly to the right of the central coin) and perpendicular to the plane of the coins is

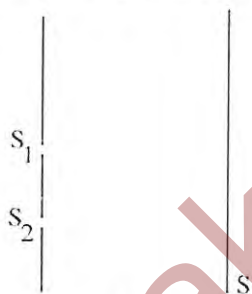
- A. $\frac{55}{2}mr^2$ B. $\frac{127}{2}mr^2$ C. $\frac{111}{2}mr^2$ D. $55mr^2$

- 25 A planet orbits in an elliptical path of eccentricity e around a massive star considered fixed at one of the foci. The point in space where it is closest to the star is denoted by P and the point where it is farthest is denoted by A . Let v_P and v_A be the respective speeds at P and A . Then



- A. $\frac{v_P}{v_A} = \frac{1+e}{1-e}$ C. $\frac{v_P}{v_A} = \frac{1+e^2}{1-e}$
- B. $\frac{v_P}{v_A} = 1$ D. $\frac{v_P}{v_A} = \frac{1+e^2}{1-e^2}$

- 26 In a Young's double slit experiment the intensity of light at each slit is I_0 . Interference pattern is observed along a direction parallel to the line $S_1 S_2$ on screen S .



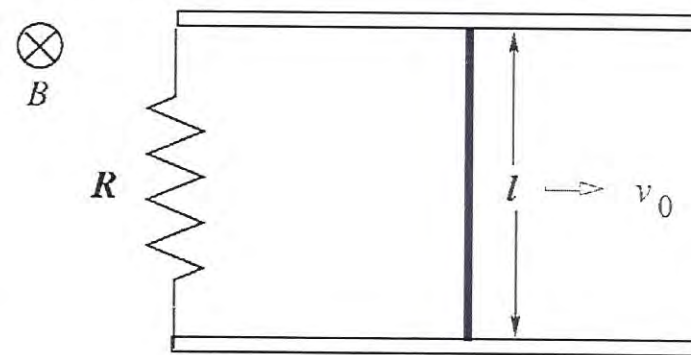
The minimum, maximum, and the intensity averaged over the entire screen are respectively

- A. $0, 4I_0, 2I_0$ C. $0, 4I_0, I_0$
- B. $I_0, 2I_0, 3I_0/2$ D. $0, 2I_0, I_0$

- 27 A loop carrying current I has the shape of a regular polygon of n sides. If R is the distance from the centre to any vertex, then the magnitude of the magnetic induction vector \vec{B} at the centre of the loop is

- A. $n \frac{\mu_0 I}{2\pi R} \tan \frac{\pi}{n}$ C. $\frac{\mu_0 I}{2R}$
- B. $n \frac{\mu_0 I}{2\pi R} \tan \frac{2\pi}{n}$ D. $\frac{\mu_0 I}{\pi R} \tan \frac{\pi}{n}$

- 28 A conducting rod of mass m and length l is free to move without friction on two parallel long conducting rails, as shown below. There is a resistance R across the rails. In the entire space around, there is a uniform magnetic field B normal to the plane of the rod and rails. The rod is given an impulsive velocity v_0 .



Finally, the initial energy $\frac{1}{2}mv_0^2$

- A. will be converted fully into heat energy in the resistor
- B. will enable rod to continue to move with velocity v_0 since the rails are frictionless
- C. will be converted fully into magnetic energy due to induced current
- D. will be converted into the work done against the magnetic field
- 29 A steady current I flows through a wire of radius r , length L and resistivity ρ . The current produces heat in the wire. The rate of heat loss in a wire is proportional to its surface area. The steady temperature of the wire is independent of
- A. L B. r C. I D. ρ
- 30 The ratio of the speed of sound to the average speed of an air molecule at 300K and 1 atmospheric pressure is close to
- A. 1 C. $\sqrt{1/300}$
 B. $\sqrt{300}$ D. 300
- 31 In one model of the electron, the electron of mass m_e is thought to be a uniformly charged shell of radius R and total charge e , whose electrostatic energy E is equivalent to its mass m_e via Einstein's mass energy relation $E = m_e c^2$. In this model, R is approximately ($m_e = 9.1 \times 10^{-31}$ kg, $c = 3 \times 10^8$ m.s⁻¹, $1/4\pi\epsilon_0 = 9 \times 10^9$ Farads.m⁻¹, magnitude of the electron charge = 1.6×10^{-19} C)

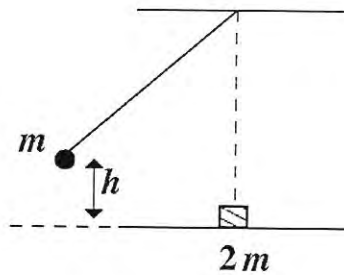
- A. 1.4×10^{-15} m C. 5.3×10^{-11} m
 B. 2×10^{-13} m D. 2.8×10^{-35} m

- 32 A body is executing simple harmonic motion of amplitude a and period T about the equilibrium position $x = 0$. Large numbers of snapshots are taken at random of this body in motion. The probability of the body being found in a very small interval x to $x + |dx|$ is highest at
- A. $x = \pm a$ C. $x = \pm a/2$
 B. $x = 0$ D. $x = \pm a/\sqrt{2}$
- 33 Two identical bodies are made of a material for which the heat capacity increases with temperature. One of these is held at a temperature of 100°C while the other one is kept at 0°C. If the two are brought into contact, then, assuming no heat loss to the environment, the final temperature that they will reach is
- A. 50°C C. less than 50°C
 B. more than 50°C D. 0°C
- 34 A particle is acted upon by a force given by $F = -\alpha x^3 - \beta x^4$ where α and β are positive constants. At the point $x = 0$, the particle is
- A. in stable equilibrium
 B. in unstable equilibrium
 C. in neutral equilibrium
 D. not in equilibrium

- 35 The potential energy of a point particle is given by the expression $V(x) = -\alpha x + \beta \sin(x/\gamma)$. A dimensionless combination of the constants α , β and γ is

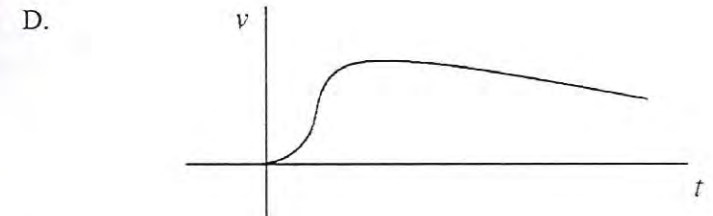
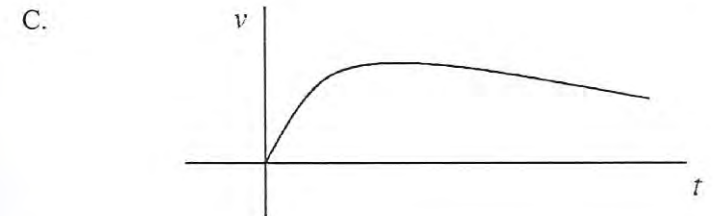
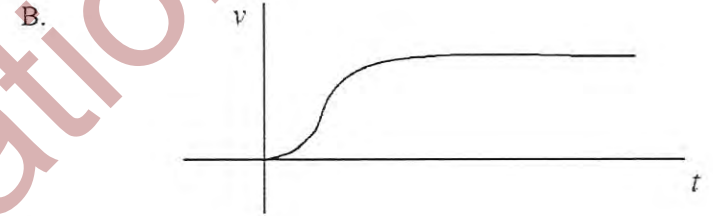
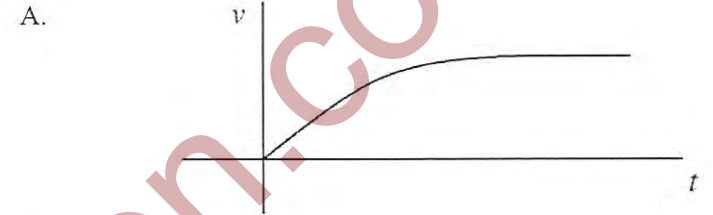
A. $\alpha/\beta\gamma$ B. $\alpha^2/\beta\gamma$ C. $\gamma/\alpha\beta$ D. $\alpha\gamma/\beta$

- 36 A ball of mass m suspended from a rigid support by an inextensible massless string is released from a height h above its lowest point. At its lowest point it collides elastically with a block of mass $2m$ at rest on a frictionless surface. Neglect the dimensions of the ball and the block. After the collision the ball rises to a maximum height of



A. $h/3$ B. $h/2$ C. $h/8$ D. $h/9$

- 37 A particle released from rest is falling through a thick fluid under gravity. The fluid exerts a resistive force on the particle proportional to the square of its speed. Which one of the following graphs best depicts the variation of its speed v with time t ?



- 38 A cylindrical steel rod of length 0.10 m and thermal conductivity $50 \text{ W.m}^{-1}\text{.K}^{-1}$ is welded end to end to copper rod of thermal conductivity $400 \text{ W.m}^{-1}\text{.K}^{-1}$ and of the same area of cross section but 0.20 m long. The free end of the steel rod is maintained at 100°C and that of the copper rod at 0°C . Assuming that the rods are perfectly insulated from the

surrounding, the temperature at the junction of the two rods is

- A. 20°C B. 30°C C. 40°C D. 50°C

39 A parent nucleus X is decaying into daughter nucleus Y which in turn decays to Z. The half lives of X and Y are 40000 years and 20 years respectively. In a certain sample, it is found that the number of Y nuclei hardly changes with time. If the number of X nuclei in the sample is 4×10^{20} , the number of Y nuclei present in it is

- A. 2×10^{17} B. 2×10^{20} C. 4×10^{23} D. 4×10^{20}

40 An unpolarized beam of light of intensity I_0 passes through two linear polarizers making an angle of 30° with respect to each other. The emergent beam will have an intensity

- A. $\frac{3I_0}{4}$ B. $\frac{\sqrt{3}I_0}{4}$ C. $\frac{3I_0}{8}$ D. $\frac{I_0}{8}$

CHEMISTRY

41 Among the following, the species with the highest bond order is

- A. O_2 B. F_2 C. O_2^+ D. F_2^-

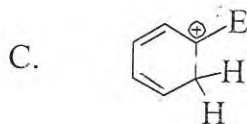
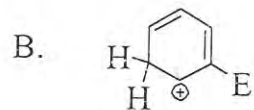
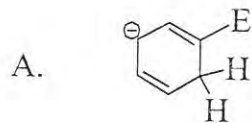
42 The molecule with **non-zero** dipole moment is

- A. BCl_3 B. $BeCl_2$ C. CCl_4 D. NCl_3

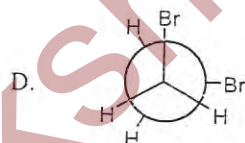
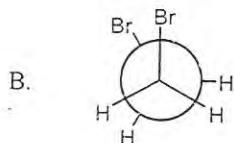
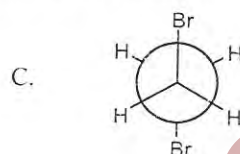
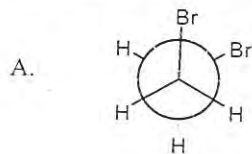
43 For a one-electron atom, the set of allowed quantum numbers is

- A. $n=1, l=0, m_l=0, m_s=+\frac{1}{2}$
B. $n=1, l=1, m_l=0, m_s=+\frac{1}{2}$
C. $n=1, l=0, m_l=-1, m_s=-\frac{1}{2}$
D. $n=1, l=1, m_l=1, m_s=-\frac{1}{2}$

44 In the reaction of benzene with an electrophile E^+ , the structure of the intermediate σ -complex can be represented as



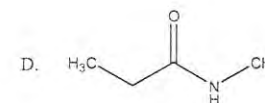
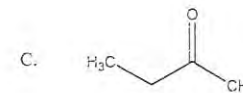
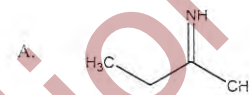
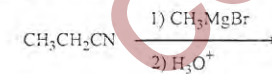
45 The most stable conformation of 2, 3-dibromobutane is



46 Typical electronic energy gaps in molecules are about 1.0 eV. In terms of temperature, the gap is closest to

- A. 10^2 K B. 10^4 K C. 10^3 K D. 10^5 K

47 The major final product in the following reaction is



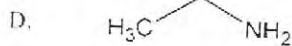
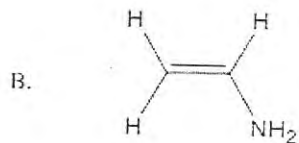
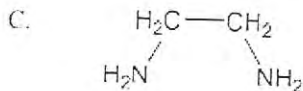
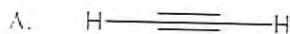
48 A zero-order reaction, $A \rightarrow \text{Product}$, with an initial concentration $[A]_0$ has a half-life of 0.2 s. If one starts with the concentration $2[A]_0$, then the half-life is

- A. 0.1 s B. 0.4 s C. 0.2 s D. 0.8 s

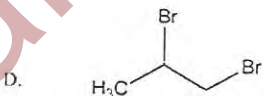
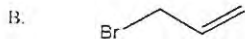
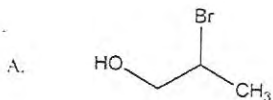
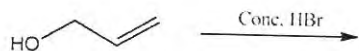
49 The isoelectronic pair of ions is

- A. Sc^{2+} and V^{3+} C. Mn^{2+} and Fe^{3+}
 B. Mn^{3+} and Fe^{2+} D. Ni^{3+} and Fe^{2+}

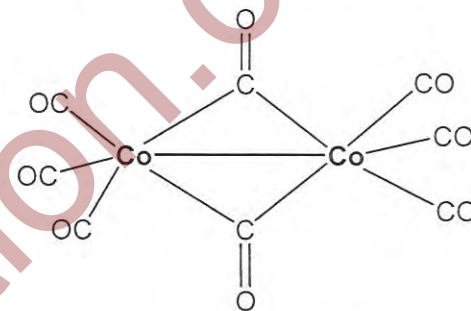
50 The major product in the following reaction is



51 The major product of the following reaction is



52 The oxidation state of cobalt in the following molecule is



A. 3

B. 1

C. 2

D. 0

53 The pK_a of a weak acid is 5.85. The concentrations of the acid and its conjugate base are equal at a pH of

A. 6.85

B. 5.85

C. 4.85

D. 7.85

54 For a tetrahedral complex $[\text{MCl}_4]^{2-}$, the spin-only magnetic moment is 3.83 BM. The element M is

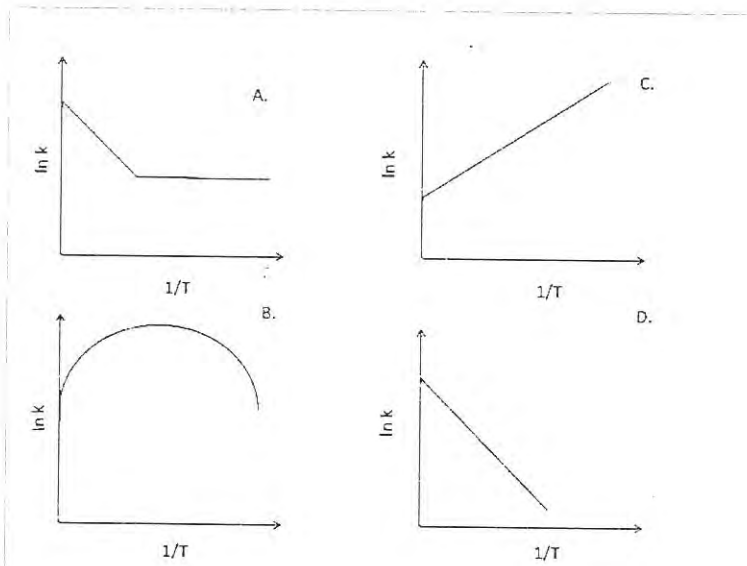
A. Co

B. Cu

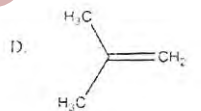
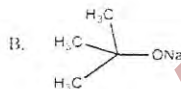
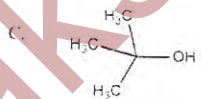
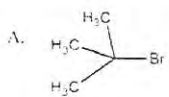
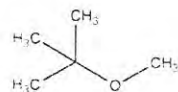
C. Mn

D. Fe

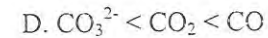
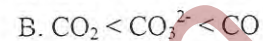
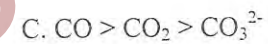
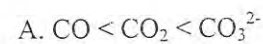
55 Among the following graphs showing variation of rate (k) with temperature (T) for a reaction, the one that exhibits Arrhenius behavior over the entire temperature range is



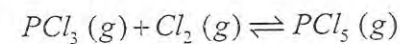
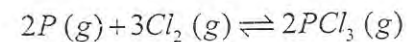
- 56 The reaction that gives the following molecule as the major product is



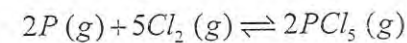
- 57 The C-O bond length in CO, CO₂, and CO₃²⁻ follows the order



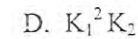
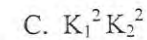
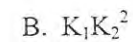
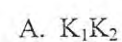
- 58 The equilibrium constant for the following reactions are K₁ and K₂, respectively.



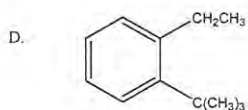
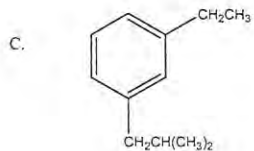
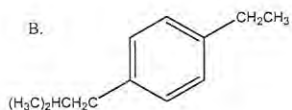
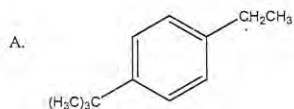
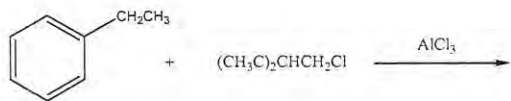
Then the equilibrium constant for the reaction



is



59 The major product of the following reaction is



60 Doping silicon with boron produces a

- A. n-type semiconductor C. p-type semiconductor
 B. metallic conductor D. insulator

BIOLOGY

61 The disorders that arise when the immune system destroys 'self' cells are called autoimmune disorders. Which of the following would be classified under this?

- A. rheumatoid arthritis C. rhinitis
 B. asthma D. eczema

62 Which of the following class of immunoglobulins can trigger the complement cascade?

- A. IgA B. IgM C. IgD D. IgE

63 Diabetes insipidus is due to

- A. hypersecretion of vasopressin
 B. hyposecretion of insulin
 C. hypersecretion of insulin
 D. hyposecretion of vasopressin

64 Fossils are most often found in which kind of rocks?

- A. meteorites C. igneous rocks
 B. sedimentary rocks D. metamorphic rocks

65 Peptic ulcers are caused by

- A. a fungus, *Candida albicans*
 B. a virus, cytomegalovirus
 C. a parasite, *Trypanosoma brucei*
 D. a bacterium, *Helicobacter pylori*

- 66 Transfer RNA (tRNA)
- A. is present in the ribosomes and provides structural integrity
 - B. usually has clover leaf-like structure
 - C. carries genetic information from DNA to ribosomes
 - D. codes for proteins
- 67 Some animals excrete uric acid in urine (uricotelic) as it requires very little water. This is an adaptation to conserve water loss. Which animals among the following are most likely to be uricotelic?
- A. fishes
 - B. amphibians
 - C. birds
 - D. mammals
- 68 A ripe mango, kept with unripe mangoes causes their ripening. This is due to the release of a gaseous plant hormone
- A. auxin
 - B. gibberlin
 - C. cytokinine
 - D. ethylene
- 69 Human chromosomes undergo structural changes during the cell cycle. Chromosomal structure can be best visualized if a chromosome is isolated from a cell at
- A. G1 phase
 - B. S phase
 - C. G2 phase
 - D. M phase

- 70 By which of the following mechanisms is glucose reabsorbed from the glomerular filtrate by the kidney tubule?
- A. osmosis
 - B. diffusion
 - C. active transport
 - D. passive transport
- 71 In mammals, the hormones secreted by the pituitary, the master gland, is itself regulated by
- A. hypothalamus
 - B. median cortex
 - C. pineal gland
 - D. cerebrum
- 72 Which of the following is true for TCA cycle in eukaryotes?
- A. takes place in mitochondrion
 - B. produces no ATP
 - C. takes place in Golgi complex
 - D. independent of electron transport chain
- 73 A hormone molecule binds to a specific protein on the plasma membrane inducing a signal. The protein it binds to is called
- A. ligand
 - B. antibody
 - C. receptor
 - D. histone
- 74 DNA mutations that do not cause any functional change in the protein product are known as
- A. nonsense mutations
 - B. missense mutations
 - C. deletion mutations
 - D. silent mutations

75 Plant roots are usually devoid of chlorophyll and cannot perform photosynthesis. However, there are exceptions. Which of the following plant root can perform photosynthesis?

- A. Arabidopsis
- B. Tinospora
- C. Rice
- D. Hibiscus

76 Vitamin A deficiency leads to night-blindness. Which of the following is the reason for the disease?

- A. rod cells are not converted to cone cells
- B. rhodopsin pigment of rod cells is defective
- C. melanin pigment is not synthesized in cone cells
- D. cornea of eye gets dried

77 In Dengue virus infection, patients often develop haemorrhagic fever due to internal bleeding. This happens due to the reduction of

- A. platelets
- B. RBCs
- C. WBCs
- D. lymphocytes

78 If the sequence of bases in sense strand of DNA is 5'-GTTTCATCG-3', then the sequence of bases in its RNA transcript would be

- A. 5'-GTTTCATCG-3'
- B. 5'-GUUCAUCG-3'
- C. 5'-CAAGTAGC-3'
- D. 5'-CAAGUAGC-3'

79 A reflex action is a quick involuntary response to stimulus. Which of the following is an example of BOTH, unconditioned and conditioned reflex?

- A. knee Jerk reflex
- B. secretion of saliva in response to the aroma of food
- C. sneezing reflex
- D. contraction of the pupil in response to bright light

80 In a food chain such as grass → deer → lion, the energy cost of respiration as a proportion of total assimilated energy at each level would be

- A. 60% - 30% - 20%
- B. 20% - 30% - 60%
- C. 20% - 60% - 30%
- D. 30% - 30% - 30%

PART II

Two-Mark Questions

MATHEMATICS

- 81 Suppose a, b, c are real numbers, and each of the equations $x^2 + 2ax + b^2 = 0$ and $x^2 + 2bx + c^2 = 0$ has two distinct real roots. Then the equation $x^2 + 2cx + a^2 = 0$ has
- A. two distinct positive real roots
 B. two equal roots
 C. one positive and one negative root
 D. no real roots
- 82 The coefficient of x^{2012} in $\frac{1+x}{(1+x^2)(1-x)}$ is
- A. 2010 B. 2011 C. 2012 D. 2013
- 83 Let (x, y) be a variable point on the curve $4x^2 + 9y^2 - 8x - 36y + 15 = 0$. Then $\min(x^2 - 2x + y^2 - 4y + 5) + \max(x^2 - 2x + y^2 - 4y + 5)$ is
- A. $\frac{325}{36}$ B. $\frac{36}{325}$ C. $\frac{13}{25}$ D. $\frac{25}{13}$

- 84 The sum of all $x \in [0, \pi]$ which satisfy the equation $\sin x + \frac{1}{2} \cos x = \sin^2(x + \frac{\pi}{4})$ is
- A. $\frac{\pi}{6}$ B. $\frac{5\pi}{6}$ C. π D. 2π
- 85 A polynomial $P(x)$ with real coefficients has the property that $P''(x) \neq 0$ for all x . Suppose $P(0) = 1$ and $P'(0) = -1$. What can you say about $P(1)$?
- A. $P(1) \geq 0$ C. $P(1) \neq 0$
 B. $P(1) \leq 0$ D. $-\frac{1}{2} < P(1) < \frac{1}{2}$
- 86 Define a sequence $\langle a_n \rangle$ by $a_1 = 5, a_n = a_1 a_2 \dots a_{n-1} + 4$ for $n > 1$. Then $\lim_{n \rightarrow \infty} \frac{\sqrt{a_n}}{a_{n-1}}$
- A. equals $\frac{1}{2}$ C. equals 1
 B. equals $\frac{2}{5}$ D. does not exist
- 87 The value of the integral $\int_{-\pi}^{\pi} \frac{\cos^2 x}{1+a^x} dx$, where $a > 0$, is
- A. π B. $a\pi$ C. $\frac{\pi}{2}$ D. 2π

88 Consider

$$L = \sqrt[3]{2012} + \sqrt[3]{2013} + \dots + \sqrt[3]{3011}$$

$$R = \sqrt[3]{2013} + \sqrt[3]{2014} + \dots + \sqrt[3]{3012}$$

$$\text{and } I = \int_{2012}^{3012} \sqrt[3]{x} \, dx.$$

Then

A. $L + R < 2I$

C. $L + R > 2I$

B. $L + R = 2I$

D. $\sqrt{LR} = I$

89 A man tosses a coin 10 times, scoring 1 point for each head and 2 points for each tail. Let $P(K)$ be the probability of scoring at least K points. The largest value of K such that $P(K) > \frac{1}{2}$ is

A. 14

B. 15

C. 16

D. 17

90 Let $f(x) = \frac{x+1}{x-1}$ for all $x \neq 1$. Let

$$f^1(x) = f(x), f^2(x) = f(f(x)) \text{ and generally}$$

$$f^n(x) = f(f^{n-1}(x)) \text{ for } n > 1.$$

$$\text{Let } P = f^1(2)f^2(3)f^3(4)f^4(5)$$

Which of the following is a multiple of P ?

A. 125

B. 375

C. 250

D. 147

PHYSICS

91 The total energy of a black body radiation source is collected for five minutes and used to heat water. The temperature of the water increases from 10.0°C to 11.0°C . The absolute temperature of the black body is doubled and its surface area halved and the experiment repeated for the same time. Which of the following statements would be most nearly correct?

A. The temperature of the water would increase from 10.0°C to a final temperature of 12°C

B. The temperature of the water would increase from 10.0°C to a final temperature of 18°C

C. The temperature of the water would increase from 10.0°C to a final temperature of 14°C

D. The temperature of the water would increase from 10.0°C to a final temperature of 11°C

92 A small asteroid is orbiting around the sun in a circular orbit of radius r_0 with speed V_0 . A rocket is launched from the asteroid with speed $V = \alpha V_0$, where V is the speed relative to the sun. The highest value of α for which the rocket will remain bound to the solar system is (ignoring gravity due to the asteroid and effects of other planets)

A. $\sqrt{2}$

B. 2

C. $\sqrt{3}$

D. 1

- 93 A radioactive nucleus A has a single decay mode with half life τ_A . Another radioactive nucleus B has two decay modes 1 and 2. If decay mode 2 were absent, the half life of B would have been $\tau_A/2$. If decay mode 1 were absent, the half life of B would have been $3\tau_A$. If the actual half life of B is τ_B , then the ratio τ_B/τ_A is

A. $3/7$ B. $7/2$ C. $7/3$ D. 1

- 94 A stream of photons having energy 3 eV each impinges on a potassium surface. The work function of potassium is 2.3 eV. The emerging photo-electrons are slowed down by a copper plate placed 5 mm away. If the potential difference between the two metal plates is 1 V, the maximum distance the electrons can move away from the potassium surface before being turned back is

A. 3.5 mm B. 1.5 mm C. 2.5 mm D. 5.0 mm

- 95 Consider three concentric metallic spheres A, B and C of radii a , b , c respectively where $a < b < c$. A and B are connected whereas C is grounded. The potential of the middle sphere B is raised to V then the charge on the sphere C is

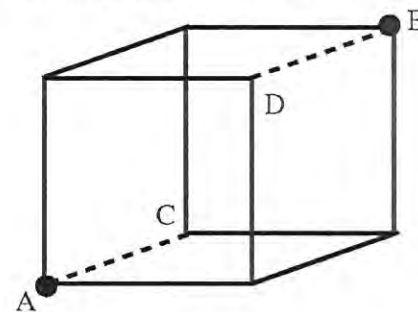
A. $-4\pi\epsilon_0 V \frac{bc}{c-b}$ C. $-4\pi\epsilon_0 V \frac{ac}{c-a}$
 B. $+4\pi\epsilon_0 V \frac{bc}{c-b}$ D. zero

- 96 On a bright sunny day a diver of height h stands at the bottom of a lake of depth H . Looking upward, he can see objects outside the lake in a circular region of radius R . Beyond this circle he sees the images of objects lying on

the floor of the lake. If refractive index of water is $4/3$, then the value of R is

A. $\frac{3(H-h)}{\sqrt{7}}$ C. $\frac{(H-h)}{\sqrt{7/3}}$
 B. $3h\sqrt{7}$ D. $\frac{(H-h)}{\sqrt{5/3}}$

- 97 As shown in the figure below, a cube is formed with ten identical resistances R (thick lines) and two shorting wires (dotted lines) along the arms AC and BD.



Resistance between point A and B is

A. $R/2$ B. $5R/6$ C. $3R/4$ D. R

- 98 A standing wave in a pipe with a length $L = 1.2$ m is described by

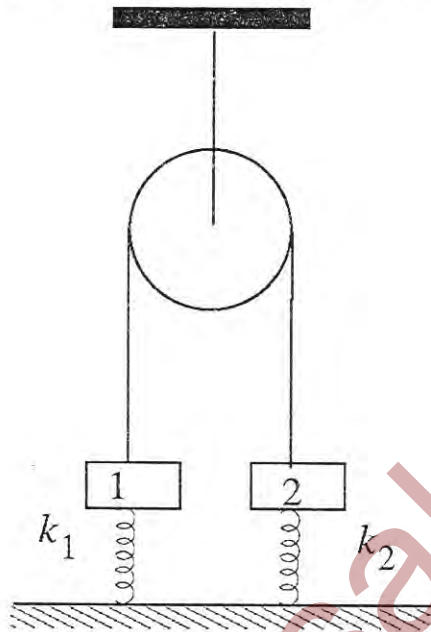
$$y(x,t) = y_0 \sin[(2\pi/L)x] \sin[(2\pi/L)x + \pi/4]$$

Based on above information, which one of the following statement is **incorrect**.

(Speed of sound in air is $300 \text{ m}\cdot\text{s}^{-1}$).

- A. The pipe is closed at both ends
- B. The wavelength of the wave could be 1.2 m
- C. There could be a node at $x = 0$ and antinode at $x = L/2$
- D. The frequency of the fundamental mode of vibrations is 137.5 Hz

- 99 Two blocks (1 and 2) of equal mass m are connected by an ideal string (see figure below) over a frictionless pulley. The blocks are attached to the ground by springs having spring constants k_1 and k_2 such that $k_1 > k_2$.

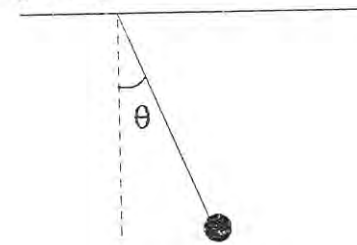


Initially, both springs are unstretched. The block 1 is slowly pulled down a distance x and released. Just after the release the possible values of the magnitudes of the

accelerations of the blocks a_1 and a_2 can be

- A. either $\left(a_1 = a_2 = \frac{(k_1 + k_2)x}{2m} \right)$ or $\left(a_1 = \frac{k_1 x}{m} - g \text{ and } a_2 = \frac{k_2 x}{m} + g \right)$
- B. $\left(a_1 = a_2 = \frac{(k_1 + k_2)x}{2m} \right)$ only
- C. $\left(a_1 = a_2 = \frac{(k_1 - k_2)x}{2m} \right)$ only
- D. either $\left(a_1 = a_2 = \frac{(k_1 - k_2)x}{2m} \right)$ or $\left(a_1 = a_2 = \frac{(k_1 k_2)x}{(k_1 + k_2)m} - g \right)$

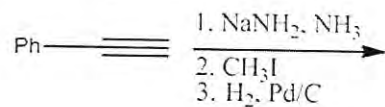
- 100 A simple pendulum is released from rest at the horizontally stretched position. When the string makes an angle θ with the vertical, the angle ϕ which the acceleration vector of the bob makes with the string is given by

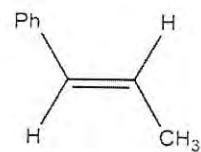
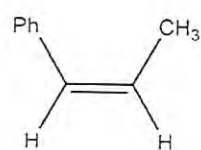
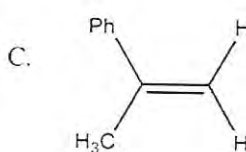



- A. $\phi = 0$
- B. $\phi = \tan^{-1} \left(\frac{\tan \theta}{2} \right)$
- C. $\phi = \tan^{-1} (2 \tan \theta)$
- D. $\phi = \pi / 2$

CHEMISTRY

- 101 The final major product obtained in the following sequence of reactions is

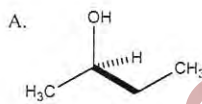
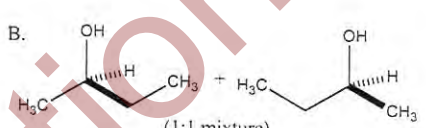
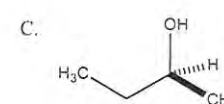
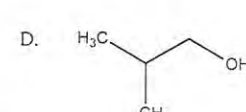


- A. 
- B. 
- C. 
- D. 

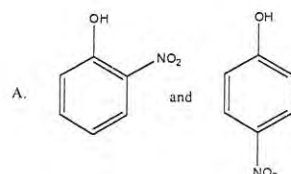
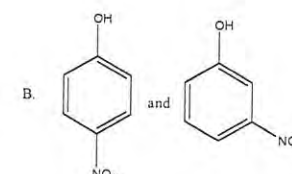
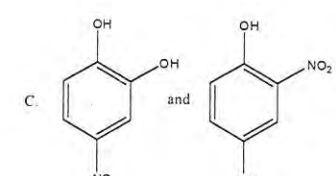
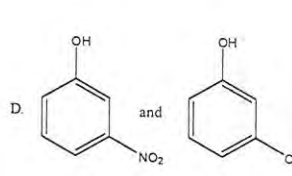
- 102 In the DNA of E. Coli the mole ratio of adenine to cytosine is 0.7. If the number of moles of adenine in the DNA is 350000, the number of moles of guanine is equal to

- A. 350000 C. 225000
B. 500000 D. 700000

- 103 (*R*)-2-bromobutane upon treatment with aq. NaOH gives

- A. 
- B. 
- C. 
- D. 

- 104 Phenol on treatment with dil. HNO_3 gives two products **P** and **Q**. **P** is steam volatile but **Q** is not. **P** and **Q** are, respectively

- A. 
- B. 
- C. 
- D. 

105 A metal is irradiated with light of wavelength 660 nm. Given that the work function of the metal is 1.0 eV, the de Broglie wavelength of the ejected electron is close to

- A. 6.6×10^{-7} m C. 1.3×10^{-9} m
B. 8.9×10^{-11} m D. 6.6×10^{-13} m

106 The inter-planar spacing between the (2 2 1) planes of a cubic lattice of length 450 pm is

- A. 50 pm B. 150 pm C. 300 pm D. 450 pm

107 The ΔH for vaporization of a liquid is 20 kJ/mol. Assuming ideal behaviour, the change in internal energy for the vaporization of 1 mol of the liquid at 60°C and 1 bar is close to

- A. 13.2 kJ/mol C. 19.5 kJ/mol
B. 17.2 kJ/mol D. 20.0 kJ/mol

108 Among the following, the species that is both tetrahedral and diamagnetic is

- A. $[\text{NiCl}_4]^{2-}$ C. $\text{Ni}(\text{CO})_4$
B. $[\text{Ni}(\text{CN})_4]^{2-}$ D. $[\text{Ni}(\text{H}_2\text{O})_6]^{2+}$

109 Three moles of an ideal gas expands reversibly under isothermal condition from 2 L to 20 L at 300 K. The amount of heat-change (in kJ/mol) in the process is

- A. 0 B. 7.2 C. 10.2 D. 17.2

110 The following data are obtained for a reaction, $X + Y \rightarrow$ Products.

Expt.	$[\text{X}_0]/\text{mol}$	$[\text{Y}_0]/\text{mol}$	rate/mol L ⁻¹ s ⁻¹
1	0.25	0.25	1.0×10^{-6}
2	0.50	0.25	4.0×10^{-6}
3	0.25	0.50	8.0×10^{-6}

The overall order of the reaction is

- A. 2 B. 4 C. 3 D. 5

BIOLOGY

- 111 When hydrogen peroxide is applied on the wound as a disinfectant, there is frothing at the site of injury, which is due to the presence of an enzyme in the skin that uses hydrogen peroxide as a substrate to produce
- A. hydrogen C. water
B. carbon Dioxide D. oxygen
- 112 Persons suffering from hypertension (high blood pressure) are advised a low-salt diet because
- A. more salt is absorbed in the body of a patient with hypertension
B. high salt leads to water retention in the blood that further increases the blood pressure
C. high salt increases nerve conduction and increases blood pressure
D. high salt causes adrenaline release that increases blood pressure
- 113 Insectivorous plants that mostly grow on swampy soil use insects as a source of
- A. carbon C. phosphorous
B. nitrogen D. magnesium
- 114 In cattle, the coat colour red and white are two dominant traits, which express equally in F1 to produce roan (red and white colour in equal proportion). If F1 progeny are self-bred, the resulting progeny in F2 will have phenotypic ratio (red:roan:white) is
- A. 1:1:1 B. 3:9:3 C. 1:2:1 D. 3:9:4

- 115 The restriction endonuclease EcoR-I recognises and cleaves DNA sequence as shown below

5'-G A A T T C-3'

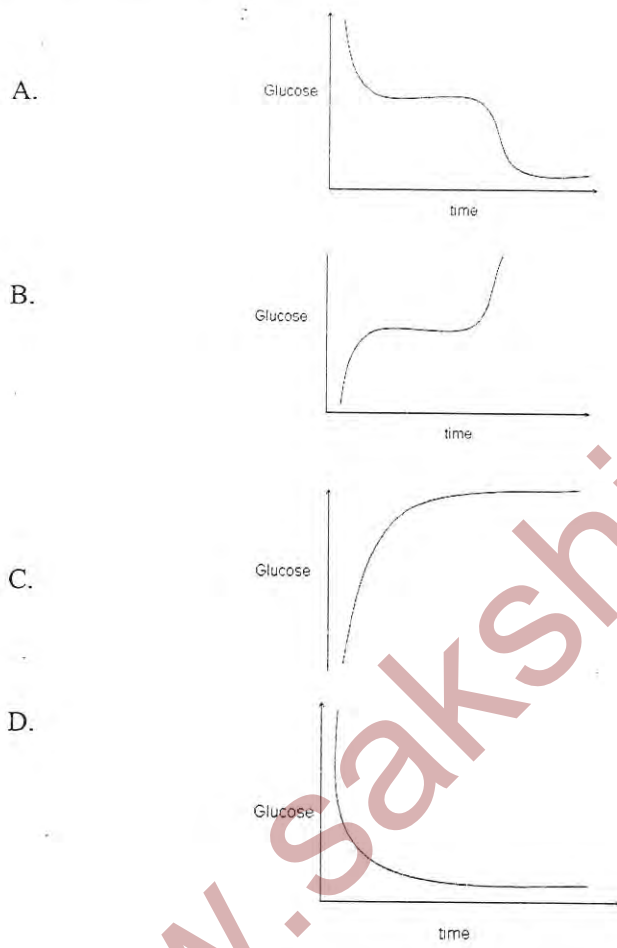
3'-C T T A A G-5'

What is the probable number of cleavage sites that can occur in a 10 kb long random DNA sequence?

- A. 10 B. 2 C. 100 D. 50
- 116 Which one of the following is true about enzyme catalysis?
- A. the enzyme changes at the end of the reaction
B. the activation barrier of the process is lower in the presence of an enzyme
C. the rate of the reaction is retarded in the presence of an enzyme
D. the rate of the reaction is independent of substrate concentration
- 117 *Vibrio cholerae* causes cholera in humans. Ganga water was once used successfully to combat the infection. The possible reason could be

- A. high salt content of Ganga water
B. low salt content of Ganga water
C. presence of bacteriophages in Ganga water
D. presence of antibiotics in Ganga water

118 When a person begins to fast, after some time glycogen stored in the liver is mobilized as a source of glucose. Which of the following graphs best represents the change of glucose level (y axis) in his blood, starting from the time (x axis) when he begins to fast?



119 The following sequence contains the open reading frame of a polypeptide. How many amino acids will the polypeptide consist of?

5'-AGCATATGATCGTTTCTCTGCTTTGAACT-3'

- A. 4 B. 2 C. 10 D. 7

120 Insects constitute the largest animal group on earth. About 25-30% of the insect species are known to be herbivores. In spite of such huge herbivore pressure, globally, green plants have persisted. One possible reason for this persistence is:

- A. food preference of insects has tended to change with time
- B. herbivore insects have become inefficient feeders of green plants
- C. herbivore population has been kept in control by predators
- D. decline in reproduction of herbivores with time

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Answer Key for Stream - SB/SX	
Question_No	Answer_Key
01	B
02	D
03	C
04	C
05	B
06	C
07	D
08	D
09	B
10	C
11	B
12	D
13	D
14	B
15	C
16	A
17	C
18	A
19	D
20	C
21	B
22	D
23	A
24	C
25	A
26	A
27	A
28	A
29	A
30	A
31	A
32	A
33	B
34	A
35	D
36	D
37	A
38	A
39	A
40	C
41	C
42	D
43	A
44	D
45	C
46	B
47	C
48	B
49	C
50	A

Answer Key for Stream - SB/SX	
Question_No	Answer_Key
51	B
52	D
53	B
54	A
55	D
56	B
57	A
58	B
59	A
60	C
61	A
62	B
63	D
64	B
65	D
66	B
67	C
68	D
69	D
70	C
71	A
72	A
73	C
74	D
75	B
76	B
77	A
78	B
79	B
80	B
81	D
82 *	
83	A
84	C
85	C
86	C
87	C
88	A
89	B
90	B
91	B
92	A
93	A
94	A
95	A
96	A
97	A
98	D
99	A
100	B

Answer Key for Stream - SB/SX	
Question_No	Answer_Key
101	D
102	B
103	C
104	A
105	C
106	B
107	B
108	C
109	D
110	D
111	D
112	B
113	B
114	C
115	B
116	B
117	C
118	A
119	D
120	C

* Printing error in the question