

## MOMENT OF INERTIA

**1. Moment of inertia of a body is independent of**

- 1) Mass of the body
- 2) distribution of mass of the body
- 3) temperature of the body
- 4) angular velocity of the body

**2. Moment of inertia of a body depends upon**

- 1) distribution of mass of the body
- 2) position of axis of rotation
- 3) temperature of the body
- 4) all of the above

**3. If  $I_1$ ,  $I_2$ , and  $I_3$  are moments of inertia of a disc about its geometric axis, diameter and a tangent in its plane, then**

- 1)  $I_1 > I_2 > I_3$
- 2)  $I_3 > I_2 > I_1$
- 3)  $I_3 > I_1 > I_2$
- 4)  $I_2 > I_1 > I_3$

**4. Moment of inertia of a ring is minimum**

- 1) about its geometric axis
- 2) about a diameter
- 3) about a tangent in its plane
- 4) tangent perpendicular to its plane

**5. Moment of inertia of a solid cylinder of mass  $m$ , length  $l$ , and radius  $r$  about an axis passing through its centre and perpendicular to its length is**

- 1)  $\frac{ml^2}{12}$
- 2)  $\frac{ml^2}{3}$
- 3)  $\frac{ml^2}{12} + \frac{mr^2}{4}$
- 4)  $\frac{ml^2}{12} + \frac{mr^2}{3}$

**6. Moment of inertia of a uniform plate of mass  $M$ , length ' $l$ ' and breadth ' $b$ ' about an axis passing through its centre of mass and normal to the plane is**

- 1)  $M(l^2+b^2) / 2$
- 2)  $M(l^2+b^2) / 12$
- 3)  $M(l^2+b^2) / 3$
- 4)  $M(l^2+b^2)$

**7. The moment of inertia of a thin uniform rod of mass  $M$  and length  $l$  about an axis perpendicular to the rod, through its centre is  $I$ . The moment of inertia of the rod about an axis perpendicular to the rod through its end point is**

- 1)  $I/4$
- 2)  $I/2$
- 3)  $2I$
- 4)  $4I$

**8. The correct relation of the following is**

- 1)  $\vec{\tau} = \vec{r} \cdot \vec{F}$
- 2)  $\vec{\tau} = \vec{r} \times \vec{F}$
- 3)  $\vec{\tau} = \frac{\vec{F}}{\vec{r}}$
- 4)  $\vec{\tau} = \vec{r} + \vec{F}$

**9. When a constant torque is applied on a rigid body, then**

- 1) The body moves with linear acceleration
- 2) The body rotates with constant angular velocity
- 3) The body rotates with constant angular acceleration
- 4) The body undergoes equal angular displacement in equal intervals of time

**10. When a rigid body is rotating, every point in it describes a circular path**

- 1) Only if the axis of rotation passes symmetrically through the centre of gravity of the body
- 2) Only if the axis of rotation passes symmetrically through the body
- 3) Provided the axis passes through the edge of the body
- 4) Whatever be the axis of rotation

**11. A solid metal sphere and a solid wooden sphere are having the same mass. If they are spinning with same angular velocity, then**

- 1) metal sphere possesses more angular momentum
- 2) wooden sphere will have more angular momentum
- 3) both will have same angular momentum
- 4) none of the above

**12. If polar ice caps melt, the length of the day**

- 1) Will increase
- 2) will decrease
- 3) will remain same
- 4) cannot be decided

**13. A boy standing on a rotating table with heavy spheres in his hands suddenly brings his hands close to his body. The angular velocity of the table**

- 1) Remains unchanged
- 2) Becomes zero
- 3) decreases
- 4) increases

**14. A solid sphere, solid cylinder and a disc are allowed to roll down from the top of an incline plane from the same height. Then**

- 1) Disc will reach the bottom first
- 2) Solid cylinder will reach the bottom first
- 3) Sphere will reach the bottom first
- 4) All will reach the bottom simultaneously

15. Two identical hollow spheres roll down two inclined planes of same height but of different angles of inclination. Then, they reach the bottom
- 1) with same speeds and in same time
  - 2) with different speeds and in different times
  - 3) with same speed but in different times
  - 4) with different speeds in same time
16. Moment of inertia of a rigid body depends on
- A) Mass of body
  - B) Position of axis of rotation
  - C) Angular velocity of the body
  - D) Time period of its rotation
- 1) A and B are correct
  - 2) B and C are correct
  - 3) A and C are correct
  - 4) C and D are correct
17. Identify the correct order in which the values of M.I. decreases for the following
- i. M.I. of solid sphere of mass 'M' and radius 'R' about its diameter of rotation
  - ii. M.I. of uniform ring of mass 'M' and radius 'R' about its tangent perpendicular to its plane
  - iii. M.I. of uniform disk of mass 'M' and radius 'R' about its diameter
  - iv. M.I of a uniform solid cylinder of mass M about its own axis of rotation
- 1) iii, i, iv, ii
  - 2) i, iv, iii, ii
  - 3) i, ii, iii, iv
  - 4) iv, iii, ii, i
18. Four objects with the same mass and radius are spinning freely about a diameter with the same angular speed. Arrange the work required to stop them in the decreasing order
- a) Solid sphere
  - b) Hollow sphere
  - c) Disc
  - d) Hoop
- 1) d, b, c, a
  - 2) a, b, c, d
  - 3) b, a, d, c
  - 4) c, a, b, d

19. A thin disc rotates about an axis passing through its centre and perpendicular to its plane with a constant angular velocity ' $\omega$ '.  $I$  is the moment of inertia of that disc and ' $L$ ' is its angular momentum about the given axis. Then rotational kinetic energy of the disc ' $E$ ' is

- A)  $E \propto L^2$                       B)  $E \propto L^{-2}$   
C)  $E \propto I$                         D)  $E \propto I^{-1}$  (if  $L$  constant)

- 1) A and C are correct
- 2) B and C are correct
- 3) B and D are correct
- 4) A and D are correct

20. **(A):**  $I_S$  and  $I_H$  are moment of inertia about the diameters of a solid and thin-walled hollow sphere respectively. If the radius and masses of above spheres are equal,  $I_H > I_S$ .

**(R):** In solid sphere, the mass is continuously and regularly distributed about the centre, whereas the mass, to a large extent, is concentrated on the surface of hollow sphere.

- 1) Both (A) and (R) are true and (R) is the correct explanation of (A)
- 2) Both (A) & (R) are true but (R) is not correct explanation of (A)
- 3) (A) is true and (R) is false
- 4) (A) is false but (R) is true

21. **(A):** The angular momentum of a particle w.r.t. origin moving parallel to x-axis with constant velocity is constant.

**(R):** There is no change in the perpendicular distance of the particle from the origin.

- (1) Both (A) and (R) are true and (R) is the correct explanation of (A)
- (2) Both (A) and (R) are true and (R) is not the correct explanation of (A)
- (3) (A) is true but (R) is false                                      (4) (A) is false but (R) is true

22. (A): A gymnast curls his body while diving to perform more number of somersaults in air.

(R): Curling reduces his moment of inertia and increases angular velocity.

- (1) Both (A) and (R) are true and (R) is the correct explanation of (A)  
 (2) Both (A) and (R) are true and (R) is not the correct explanation of (A)  
 (3) (A) is true but (R) is false  
 (4) (A) is false but (R) is true

23. (A): If a raw egg and a boiled egg are spinning on the table by applying same torque then raw egg comes, to rest quickly.

(R): While spinning, moment of inertia of boiled egg will be less than that of raw egg.

- (1) Both (A) and (R) are true and (R) is the correct explanation of (A)  
 (2) Both (A) and (R) are true and (R) is not the correct explanation of (A)  
 (3) (A) is true but (R) is false  
 (4) (A) is false but (R) is true

24. Match list I with list II

List - I

- a) Torque  
 b) Angular momentum  
 c) Rotational K.E  
 d) Work done by centripetal force

List - II

- e)  $(1/2) L$   
 f) Zero  
 g)  $I\alpha$   
 h)  $I\omega$

- (1) a-h, b-e, c-f, d-g (2) a-f, b-h, c-g, d-e (3) a-e, b-f, c-g, d-h (4) a-g, b-h, c-e, d-f

25. If M is the mass and R the radius, match the Moment of Inertia for the given objects about the indicated axes

Object

Moment of Inertia

- (a) circular ring (e)  $\frac{7}{5}MR^2$  about tangent  
 (b) hollow sphere (f)  $\frac{5}{4}MR^2$  about tangent  $\perp$  to plane  
 (c) circular disc (g)  $2MR^2$  about tangent, to plane  
 (d) solid sphere (h)  $\frac{5}{3}MR^2$  about tangent

- (1) a-g, b-e, c-g, d-f (2) a-g, b-h, c-f, d-e (3) a-f, b-g, c-e, d-h (4) a-f, b-h, c-g, d-e

26. The radius of gyration of a body about an axis at a distance of 4 cm from its centre of mass is 5 cm. The radius of gyration about a parallel axis through centre of mass is
- 1) 2 cm                      2) 5 cm                      3) 4 cm                      4) 3 cm
27. The moment of inertia of a cylinder about its own axis is equal to its moment of inertia about an axis passing through its centre and normal to its length. The ratio of length to radius is
- 1) 2 : 1                      2)  $\sqrt{3} : 1$                       3) 3 : 1                      4)  $\sqrt{2} : 1$
28. Two circular loops of radii R and nR are made of same wire. If their M.I about their normal axis through centre is in the ratio 1: 8, the value of n is
- 1) 6                      2) 1                      3) 2                      4) 4
29. The radius of gyration of a solid sphere of radius 'R' about its tangential axis is
- 1)  $\frac{7R}{5}$                       2)  $\frac{3R}{5}$                       3)  $R\sqrt{\frac{7}{5}}$                       4)  $R\sqrt{\frac{3}{5}}$
30. The moment of inertia of an uniform circular disc about its central axis is 'I'. Its M.I about a tangent in its plane is equal to
- 1) 2I                      2) 2.5 I                      3) 1.5 I                      4)  $\frac{I}{2}$
31. Two circular rings of equal mass and radius are placed touching each other. The moment of inertia of the system about tangential axis in the plane of system passing through point of contact of rings is
- 1)  $3 mr^2$                       2)  $\frac{3}{2} mr^2$                       3)  $6 mr^2$                       4)  $\frac{5}{2} mr^2$
32. Four small spheres each of radius 'r' and mass 'm' are placed with their centers at the four corners of a square of side 'L'. The M.I. of the system about any side of square is
- 1)  $\frac{8mr^2}{5} + mL^2$                       2)  $\frac{8mr^2}{5} + 2mL^2$                       3)  $\frac{5mr^2}{8} + mL^2$                       4)  $\frac{5mr^2}{8} + 2mL^2$
33. A disc of mass 'm' and radius R has a concentric hole of radius 'r'. It's M.I. about an axis through centre and normal to its plane is
- 1)  $\frac{m}{2}(R-r)^2$                       2)  $\frac{m}{2}(R^2 - r^2)$                       3)  $\frac{m}{2}(R+r)^2$                       4)  $\frac{m}{2}(R^2 + r^2)$

34. A circular disc of radius 'R' and thickness R/6 has moment of inertia 'I' about an axis passing through its centre and perpendicular to its plane. It is melted and recasted into a solid sphere. The M.I of the sphere about its diameter as axis of rotation is
- 1) I                                      2) 2I/3                                      3) I/5                                      4) I/10
35. A uniform circular disc of radius R lies in the XY - plane with its centre at the origin of co-ordinate system. Its moment of inertia about an axis, lying in the xy-plane, parallel to the x-axis and passing through a point on the y-axis at a distance  $y = 2R$  is  $I_1$ . Its moment of inertia about an axis lying in a plane perpendicular to xy-plane passing through a point on the x-axis at a distance  $x = d$  is  $I_2$ . If  $I_1 = I_2$ , the value of 'd' is
- 1)  $\frac{\sqrt{19}}{2}R$                                       2)  $\frac{\sqrt{17}}{2}R$                                       3)  $\frac{\sqrt{15}}{2}R$                                       4)  $\frac{\sqrt{13}}{2}R$
36. Three spheres, each of mass 'm' and radius 'R' are kept in touch with each other such that their centers form an equilateral triangle. The M.I. of the system about a median of triangle is
- 1)  $\frac{21}{5}MR^2$                                       2)  $\frac{16}{5}MR^2$                                       3)  $\frac{7}{2}MR^2$                                       4)  $\frac{4}{5}MR^2$
37. A mass is whirled in a circular path with an angular momentum L. If the length of string and angular velocity, both are doubled, the new angular momentum is
- 1) L                                      2) 4L                                      3) 8L                                      4) 16L
38. If 484 J of energy is spent in increasing the speed of a wheel from 60 rpm to 360 rpm, the M.I. of the wheel is.
- 1) 1.6 kg m<sup>2</sup>                                      2) 0.3 kg m<sup>2</sup>                                      3) 0.7 kg m<sup>2</sup>                                      4) 1.2 kg m<sup>2</sup>
39. The diameter of a rotating fly wheel is R. Its coefficient of linear expansion is  $\alpha$ . If the temperature is increased by  $\Delta T$ , the percentage change in its rotational KE would be.
- 1)  $\alpha \cdot \Delta t \cdot 100$                                       2)  $2 \cdot \alpha \cdot \Delta t \cdot 100$                                       3)  $\frac{\alpha \Delta t}{2} \times 100$                                       4)  $\frac{2\alpha \Delta t}{5} \times 100$
40. The K.E. of a body rotating at 300 rpm is 62.8J. Its angular momentum is
- 1) 1 Js                                      2) 2 Js                                      3) 4 Js                                      4) 8 Js

41. A thin circular ring of mass 'm' and radius R is rotating about its axis with a constant angular velocity  $\omega$ . The objects each of mass M are attached gently to the opposite ends of a diameter of the ring. The new angular velocity of ring is

- 1)  $\frac{\omega m}{M+m}$                       2)  $\frac{\omega m}{m+2M}$                       3)  $\frac{\omega(m+2M)}{m}$                       4)  $\frac{\omega(m-2M)}{m+2M}$

42. A particle performs uniform circular motion with an angular momentum L. If the angular frequency of particle is doubled and kinetic energy is halved, its angular momentum becomes

- 1) 4L                                      2) 2L                                      3) L/L                                      4) L/4

43. A heavy wheel of radius 20 cm and weight 10kg is to be dragged over a step of height 10cm, by a horizontal force F applied at the centre of the wheel. The minimum value of F is

- 1) 20 kgwt                                      2) 1 kgwt                                      3)  $10\sqrt{3}$ kgwt                                      4)  $10\sqrt{2}$ kgwt

44. The M.I. of a uniform disc about an axis passing through its centre and perpendicular to its plane is  $1 \text{ kg m}^2$ . It is rotating with an angular velocity of  $100 \text{ rad s}^{-1}$ . A second disc of same mass and radius is joined to it coaxially. Now these two discs together continue to rotate about the same axis. Then the loss in kinetic energy in kilo joules is

- 1) 2.5                                      2) 3                                      3) 3.5                                      4) 4

45. A rod of length l is held vertically stationary with its lower end located at a point 'P', on the horizontal plane. When the rod is released to topple about 'P', the velocity of the upper end of the rod with which it hits the ground is

- 1)  $\sqrt{\frac{g}{\ell}}$                                       2)  $\sqrt{3g\ell}$                                       3)  $3\sqrt{\frac{g}{\ell}}$                                       4)  $\sqrt{\frac{3g}{\ell}} \text{ s}$



**KEY**

1) 4    2) 4    3) 3    4) 2    5) 3    6) 2    7) 4    8) 2    9) 3    10) 4

11) 2    12) 1    13) 4    14) 3    15) 3    16) 1    17) 1    18) 1    19) 4    20) 1

21) 1    22) 1    23) 1    24) 4    25) 2    26) 3    27) 2    28) 3    29) 3    30) 2

31) 1    32) 2    33) 2    34) 3    35) 3    36) 2    37) 3    38) 3    39) 2    40) 3

41) 2    42) 4    43) 3    44) 1    45) 4

## HINTS

$$26. k^2 = k_{cg}^2 + r^2$$

$$5^2 = k_{cg}^2 + 4^2$$

$$k_c = 3cm$$

$$27. \frac{mr^2}{2} = \frac{mr^2}{4} + \frac{ml^2}{12}$$

$$\frac{l}{r} = \frac{\sqrt{3}}{1}$$

$$28. I = mr^2$$

but  $m = 2\pi r \times a$

$$I \propto r^3$$

$$\frac{1}{8} = \frac{1}{r^3} \Rightarrow r = 2$$

$$29. I = \frac{7}{5}MR^2 = MK^2 \quad K = R\sqrt{\frac{7}{5}}$$

$$30. I = \frac{mr^2}{2} = \frac{5}{4}mr^2$$

$$I^1 = \frac{mr^2}{4} + mr^2 = 2.5 I$$

$$31. I = \left[ \frac{mr^2}{2} + mr^2 \right] \times 2 = 3mr^2$$

$$32. I = \frac{2}{5}mr^2 + \frac{2}{5}mr^2 + \left( \frac{2}{5}mr^2 + ml^2 \right) 2$$

$$33. I = \int_r^R dm.x^2 = \int_r^R \frac{M}{\pi(R^2 - r^2)} 2\pi x.dx.x^2$$

$$I = \frac{M}{2}(R^2 - r^2)$$

$$34. I = \frac{MR^2}{2} \quad I^1 = \frac{2}{5} M \cdot x^2 \quad \text{where } x = R/2$$

$$= \frac{2}{5} M \cdot \frac{R^2}{4} = \frac{I}{5}$$

$$35. \frac{MR^2}{4} + M \cdot 4R^2 = I_1 \quad \frac{MR^2}{2} + Md^2 = I_2$$

$$\frac{MR^2}{2} + Md^2 = \frac{MR^2}{4} + 4MR^2$$

$$d^2 = \frac{17R^2}{4} - \frac{R^2}{2} \Rightarrow d = \frac{R\sqrt{15}}{2}$$

$$36. I = \frac{2}{5} mr^2 + \left(\frac{7}{5} mr^2\right) \times 2 = \frac{16}{5} mr^2$$

$$37. L = I\omega = mr^2 \cdot \omega$$

$$L \propto r^2 \omega$$

$$L^1 = 8L$$

$$38. 484 = \frac{1}{2} I [(12\pi)^2 - (2\pi)^2]$$

$$484 = \frac{1}{2} I \times 14\pi \times 10\pi$$

$$I = 0.7 \text{ kgm}^2$$

$$39. E = \frac{L^2}{2I} \Rightarrow E \propto \frac{1}{I} \quad \frac{\Delta E}{E} = -\frac{\Delta I}{I}$$

$$\frac{\Delta E}{E} = 2 \alpha \Delta t \quad \frac{\Delta E}{E} \times 100 = 2 \alpha \Delta t \times 100$$

$$40. E = \frac{L^2}{2I} = \frac{1}{2} L \omega \quad L = \frac{2E}{\omega} = \frac{2 \times 62.8}{10 \times 3.14} = 4$$

41.  $mR^2 \omega = R^2 (m+2M) \omega^1$

$$\omega^1 = \frac{m}{m+2M} \omega$$

42.  $E = \frac{1}{2} LW$       OR  $E \propto LW$

$$\frac{E}{2} \propto L^1 2W$$
      OR  $2 = \frac{L}{L^1} \times \frac{1}{2}$

$$\frac{L}{L^1} = 4$$
       $\Rightarrow L^1 = L/4$

43.  $F \times 10 = W \sqrt{20^2 - 10^2}$        $F \times 10 = W \times 10\sqrt{3}$

$$F = W \sqrt{3}$$
       $= 10\sqrt{3} \text{ kgwt}$

44.  $I\omega = (I_1 + I_2) \omega$        $I \times 100 = 2I$

$$\omega^1 = 25 \text{ rads}^{-1}$$

$$\Delta E = \frac{1}{2} \times \frac{1 \times 1}{2} \times 100^2$$

45.  $mg \frac{l}{2} = \frac{1}{2} \frac{ml^2}{3} \omega^2$        $\omega = \sqrt{3g/l}$