

EXPANSION OF GASES

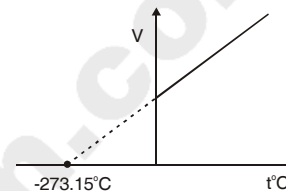
1. Since the expansion of gases is much more than that of liquid, all the expansions of gases are real.
2. A gas has two types of coefficients of expansions.

i) Volume expansion coefficient and ii) Pressure expansion of coefficient

3. **Volume coefficient of a gas (α):** At constant pressure the ratio of increase of volume per 1°C rise in temperature to its original volume at 0°C is called volume coefficient of a gas.

$$\alpha = \frac{V_t - V_0}{V_0 t} \quad \text{or} \quad \alpha = \frac{V_2 - V_1}{V_1 t_2 - V_2 t_1} \quad \text{Or} \quad V_t = V_0 (1 + \alpha t)$$

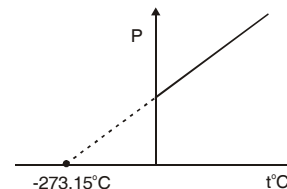
Unit of α : $^\circ\text{C}^{-1}$ or K^{-1} .



4. **Pressure coefficient of a gas (β):** At constant volume the ratio of increase of pressure per 1°C rise in temperature to its original pressure at 0°C is called pressure coefficient of gas.

$$\beta = \frac{P_t - P_0}{P_0 t} \quad \text{or} \quad \beta = \frac{P_2 - P_1}{P_1 t_2 - P_2 t_1} \quad \text{Or} \quad P_t = P_0 (1 + \beta t)$$

. Unit: $^\circ\text{C}^{-1}$ or K^{-1}



5. Regnault's apparatus is used to determine the volume coefficient of a gas.
6. Jolly's bulb apparatus is used to determine the pressure coefficient of a gas.
7. Volume coefficient and pressure coefficient of a gas are equal and each equal to $\frac{1}{273} / ^\circ\text{C}$ or $0.0036 / ^\circ\text{C}$ for all gases.

8. Absolute scale of temperature:

- a) P-t graph or V-t graph is straight line intersecting the temperature axis at $\sim 273.15^\circ\text{C}$. This temperature is called absolute zero. (0 K)
- b) Absolute zero is the temperature at which the volume of a given mass of a gas at constant pressure or the pressure of the same gas at constant volume becomes zero.
- c) The lowest temperature attainable is $\sim 273.15^\circ\text{C}$ or 0 K.
- d) The scale of temperature on which the zero corresponds to $\sim 273^\circ\text{C}$ and each degree is equal to the Celsius degree is called the absolute scale of temperature or thermodynamic scale of temperature.
 $T \text{ K} = t + 273.15^\circ\text{C}$.
- e) There is no negative temperature on Kelvin scale.

9. Boyle's law:

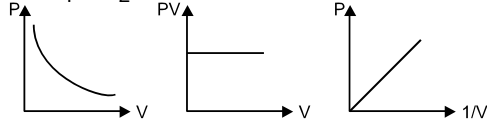
- a) At constant temperature, the pressure of a given mass of a gas is inversely proportional to its volume.

$$P \propto \frac{1}{V} \text{ or } PV = K \text{ (n, T are constant) or } P_1V_1 = P_2V_2.$$

b) The value of K depends on the mass and temperature of the gas and the system of units.

c) At constant temperature, the pressure of a given mass of gas is directly proportional to its density.

$$P \propto d \text{ or } \frac{P}{d} = K \text{ or } \frac{P_1}{d_1} = \frac{P_2}{d_2}.$$



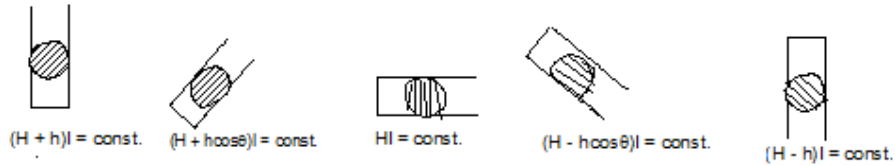
d) P-V graph at a constant temperature (isothermal) is a rectangular hyperbola.

e) PV-V graph is a straight line parallel to volume axis.

f) $P-\frac{1}{V}$ graph is a straight line passing through the origin.

g) Many gases obey Boyle's law only at high temperatures and low pressures.

10. Quill tube :



11. Air bubble in a lake:

An air bubble is reaching the top of a lake from the bottom (Temperature being constant), the depth of the lake is 'h'.

a) If the volume of the bubble becomes n times, $h = H(n-1)$

For the other liquid of density d, $h = \frac{76 \times 13.6}{d}(n-1)$

b) If radius (or) diameter of the bubble becomes n times $h = H(n^3 - 1)$

For other liquid of density d, $h = \frac{76 \times 13.6}{d}(n^3 - 1)$

c) If the surface area of the bubble becomes n times $h = H(n^{3/2} - 1)$

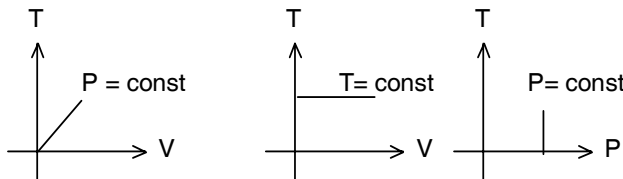
Where H is the atmospheric pressure

d) For other liquid of density d, $h = \frac{76 \times 13.6}{d}(n^{3/2} - 1)$

12. Charles' Law (I):

The volume of a given mass of a gas is proportional to its absolute temperature at constant pressure.

$$V \propto T \text{ (or) } \frac{V_1}{V_2} = \frac{T_1}{T_2} \text{ (P = const)}$$



13. **Charles' Law (II):** The pressure of a given mass of a gas is proportional to its absolute temperature at constant volume. (Gay-lusacs' law) $P \propto T$ (or) $\frac{P_1}{P_2} = \frac{T_1}{T_2}$ ($V = \text{const}$)

14. The constant volume gas thermometer works on the principle of Gay-lusacs' law.

15. **Gas Equation :**

a) For 1 gm of a gas $\frac{PV}{T} = r$ For m grams of the gas $\frac{PV}{T} = mr$

'r' is the specific gas constant which depends on nature of the gas and amount of the gas and different for different gases.

b) For one mole of a gas $\frac{PV}{T} = R$ For n moles of a gas $\frac{PV}{T} = nR$

Where R is the universal gas constant, which is constant for all gases $r = \frac{R}{M}$

c) Boltzmann constant $K = \frac{R}{N}$ where N is the Avogadro number.

$N = 6.023 \times 10^{23}$ and $K = 1.38 \times 10^{-23} \text{J/k}$

16. **Ideal Gases:**

- a) A gas which obeys gas laws at all temperatures and pressures is called an ideal gas.
- b) Ideal gas molecules have no specific shape (or) size. These are point masses.
- c) These exist in gaseous state even at absolute zero.
- d) There are no molecular forces of attractions and hence there is no PE for the ideal gas molecules. They have only KE.
- e) At absolute zero the internal energy of an ideal gas is zero.
- e) Real gases obey gas laws at low pressure and high temperatures.
- f) Values of R:

$$\begin{aligned} R &= 8.31 \times 10^7 \text{ erg/gm. mole/K} \\ &= 8.31 \text{ J/gm mole/K} \\ &= 8.31 \times 10^3 \text{ J/kg mole/K} \\ &= 1.98 \text{ cal/gm mole/}^\circ\text{C} \\ &= 0.083 \text{ litre atm/K} \end{aligned}$$

18. A sample of an ideal gas occupies a volume V at a pressure P and absolute temperature T. The mass of each molecule is m. If K is the Boltzmann constant, then the density of the gas is $d = \frac{Pm}{KT}$

19. If two vessels of equal volume containing same gas at temperature T_1 and T_2 and pressure P_1 and P_2 combine by a time capillary tube, the final common pressure is $P = \frac{P_1T_2 + P_2T_1}{T_1 + T_2}$

20. Two vessels of volumes V_1 and V_2 contain air pressures P_1 and P_2 respectively. If they are connected by a small tube of negligible volume then the common pressure is $P = \frac{P_1V_1 + P_2V_2}{V_1 + V_2}$.