2011 (I) MATHEMATICAL SCIENCES TEST BOOKLET

Time: 3:00 Hours

Maximum Marks: 200

INSTRUCTIONS

- 1. You have opted for English as medium of Question Paper. This Test Booklet contains one hundred and twenty (20 Part'A'+40 Part 'B' +60 Part 'C') Multiple Choice Questions (MCQs). You are required to answer a maximum of 15, 25 and 20 questions from part 'A' 'B' and 'C' respectively. If more than required number of questions are answered, only first 15, 25 and 20 questions in Parts 'A' 'B' and 'C' respectively, will be taken up for evaluation.
- 2. Answer sheet has been provided separately. Before you start filling up your particulars, please ensure that the booklet contains requisite number of pages and that these are not torn or mutilated. If it is so, you may request the Invigilator to change the booklet. Likewise, check the answer sheet also. Sheets for rough work have been appended to the test booklet.
- 3. Write your Roll No., Name, Your address and Serial Number of this Test Booklet on the Answer sheet in the space provided on the side 1 of Answer sheet. Also put your signatures in the space identified.
- 4. You must darken the appropriate circles related to Roll Number, Subject Code, Booklet Code and Centre Code on the OMR answer sheet. It is the sole responsibility of the candidate to meticulously follow the instructions given on the Answer Sheet, failing which, the computer shall not be able to decipher the correct details which may ultimately result in loss, including rejection of the OMR answer sheet.
- 5. Each question in Part 'A' carries 2 marks, Part 'B' 3 marks and Part 'C' 4.75 marks respectively. There will be negative marking @ 0.5marks in Part 'A' and @0.75 in Part 'B' for each wrong answer and no negative marking for Part 'C'.
- 6. Below each question in Part 'A' and 'B', four alternatives or responses are given.
 Only one of these alternatives is the "correct" option to the question. You have to find, for each question, the correct or the best answer. In Part 'C' each question may have 'ONE' or 'MORE' correct options. Credit in a question shall be given only on identification of 'ALL' the correct options in Part 'C'. No credit shall be allowed in a question if any incorrect option is marked as correct answer.
- 7. Candidates found copying or resorting to any unfair means are liable to be disqualified from this and future examinations.
- Candidate should not write anything anywhere except on answer sheet or sheets for rough work.
- After the test is over, you MUST hand over the answer sheet (OMR) to the invigilator.
- 10. Use of calculator is not permitted.

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Logarithms

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	0	1	2	3	4	5	6	7	8	9	1	2	3	4	5	6	7	8	9
10	0000	0043	0086	0128	0170	0212	0253	0294	0334	0374	5 4	8	13 12	17 16	21 20	26 24	30 28	34 32	38 36
11	0414	0.453	0492	0531	0569	0607	0645	0682	0719	0755	4	8	12 11	16 15	20 18	23 22	27 26	31 29	35 33
12	0792	0828	0864	0899	0934	0969	1004	1039	1072	1106	3	7	11	14 14		21	25 24	28 27	
13	1139	1173	1206	1239	1271						3	6	10	13	16	19	23	26	29
14	1461	1492	1523	1553	1584	1303	1335	1367	1399	1430	3	6	10			19	22	25	28
						1614	1644	1673	1703	1732	3	6	9	12	14	17		23	
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16	2041	2068	2095	2122	2148	2175	2201	2227	2253	2279	3	6	8	11 10	14 13	16 16	19 18	22	24 23
17	2304	2330	2335	2380	2405	2430	2455	2480	2504	2529	3	5	8	10	13 12	15	18	20	23
18	2553	2577	2601	2625	2648	2672			2742		2	5	7	9	12	14	17	19	21
19	2788	2810	2833	2856	2878		2695	2718		2765	2	4	7 7	9	11	13	16		20
						2900	2923	2945	2967	2989	2	4	6	8	11	13	15		19
20 21	3010 3222	3032 3243	3054 3263	3075 3284	3096 3304	3118 3324	3139 3345	3160 3365	3181 3385	3201 3404	2	4	6	8		13	15		19 18
22	3424	3444	3464	3483	3502	3522	3541	3560	3579	3598	2	4	6	8	10		14		17
23 24	3617 3802	3636 3820	3655 3838	3674 3856	3692 3874	3711	3729 3909	3747 3927	3766 3945	3784 3962	2 2	4	6 5	7	9		13 12		17 16
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25 26	3979 4150	3997 4166	4014	4200	4048	4065 4232	4082	4099 4265	4281	4133 4298	2	3	5 5	7 7	9 8		12		15
27	4314	4330	4346	4362	4378	4393	4409	4425	4440	4456	2	3	5	6	8	9	.11		14
28 29	4472 4624	4487 4639	4502 4654	4518 4669	4533	454B	4564	4579	4594	4609	2	3	5	6	3	9	11		14
		4039			4683	4698	4713	4728	4742	4757	1	3	4	6	7	9	10	12	13
30 31	4771	4786 4928	4800 4942	4814	4829 4969	4843 4983	4857 49 97	4871 5011	4886 5024	4900 5038	1	3	4	6 6	7 7		10		13 12
32	5051	5065	5079	5092	5105	5119	5132	5145	5159	5172	1	3	4	5	7		9		12
33	5185	5198	5211-	5224	5237	5250	5263	5276	5289	5302	1	3	4	5	6		9	10	12
34	5315	5328	5340	5353	5366	5378	5391	5403	5416	5428	1	3	4	5	6	8	9	10	11
35		5453			5490		5514			5551				5				10	
36 37	5563 5682	5575 5694	5587 5705	5599 5717	5611 5729	5623 5740	5635 5752	5647 5763	5658 5775	5670 5786	1	2	3	5 5	6 6		8		
38	5798	5809	5821	5832	5843	5855	5866	5877	5888	5899	1	2	3	5			8		
39	5911	5922	5933	5944	5955	5966	5977	5988	5999	6010	1	2	3	4	5		8	9	10
40		6031	6042		6064	6075	6085	6096	6107	6117	1	2	3	4	5		8		10
41 42	6128 6232	6138 6243	6149 6253	6160 6263	6170 6274	6180 6284	6191 6294	6201 6304	6212 6314	6222 6325	1	2	3	4	5 5		8 7		9
43		6345	6355	6365	6375	6385	6395	6405	6415	6425	i	2	3	4	5		7		9
44	6435	6444	6454	6464	6474	6484	6493	6503	6513	6522	1	2	3	4	5		7		9
45		6542	6551	6561	6571	6580	6590	6599	6609	6618	1	2	3	4	5	6	7		9
46 47		6637 6730	6646 6739		6065 6758	6675 6767	6684 6776	6693 6785	6702 6790	6712 6803	1	2		4			7		
48		6821	6830	6839	6848	6857	6866	6875	6884	6893	1	2		4	4		6		
49			6920			6946	6955	6964	6972	6981	1			4			6		
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Logarithms

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50	6990	6998	7007	7016	7024	7033	7042	7050	7059	7067	1	2	3	3	4	5	6	7	8
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52 53	7160 7243	7168 7251	7177 7259	7185 7267	7193 7275	7202 7284	7210 7292	7218 7300	7226 7308	7235 7316	1	2	2	3	4	5 5	6	7 6	7 7
54	7324	7332	7340	7348	7356	7364	7372	7380	7388	7396	1	2	2	3	4	5	6	6	. 7
55	7404	7412	7419	7427	7435	7443	7451	7459	7.466	7474	1	2	2	3	4	5	6	6	7
56	7482	7490	7497	7505	7513	7520	7528	7536	7543	7551	. 1	2	2	3	4	5	5	6	7
57 58	7559 7634	7566 7642	7574 7649	7582 7657	7589 7664	7597 7672	7604 7679	7612 7686	7619 7694	7627 7701	1	2	2	3	4	5	5 5	6	7
59	7709	7716	7723	7731	7738	7745	7752	7760	7767	7774	i	1	2	3	4	4	5	6	7
60	7782	7789	7796	7803	7810	7818	7825	7832	7839	7846	1	1	2	3	4	4	5	6	6
61	7853	7860	7868	7875	7882	7889	7896	7903	7910	7917	1	1	2	3	4	4	5	6	6
62 63	7924 7993	7931 8000	7938 8007	7945 8014	7952 8021	7959 8028	7966 8035	7973 8041	7980 8048	7987 8055	1	1	2	3	3	4	5	6	6
64	8062	8069	8075	8082	8089	8096	8102	8109	8116	8122	1		2	3	3	4	5	5 5	6 6
65	8129	8136	8142	8149	8156	8162	8169	8176	8182	8189	1	1	2	3	3	4	5	5	6
66	8195	8202	8209	8215	8222	8228	8235	8241	8248	8254	1	1	2	3	3	4	5	5	6
67 68	8261 8325	8267 8331	8274 8338	8280 8344	8287 8351	8293 8357	8299 8363	8306 8370	8312 8376	8319 8382	1	1	2	3	3	4	5 4	5 5	6
69	8388	8395	8401	8407	8414	8420	8426	8432	8439	8445	1	1	2	2	3	4	4	5	6
70	8451	8457	8463	8470	8476	8482	8 488	8494	8500	8506	1	1	2.	2	3	4	4	5	6
71	8513	8519	8525	8531	8537	8543	8549	8555	8561	8567	1	1	2	2	3	4	4.	5	5
72 73	8573 8633	8579 8639	8585 8645	8591 8651	8597 8657	8603 8663	8609 8669	8615 8675	8621 8681	8627 8686	1	1	2	2	3	4	4	5	5 5
74	8692	8698	8704	8710	8716	8722	8727	8733	8739	8745	1	1	2	2	3	4	4	5	5
75	8751	8756	8762	8768	8774	8779	8785	8791	8797	8802	1	1	2	2	3	3	4	5	5
76	8808	8814	8820	8825	8831	8837	8842	8848	8854	8859	1	1	2	2	3	3	4	5	5
77 78	8865 8921	8871 8927	8876 8932	8882 8938	8887 8943	#393 8949	8899 8954	8904 8960	8910 8965	8915 8971	1	1	2	2	3	3	4	4	5 5
79	8976	8982	8987	8993	8998	9004	9009	9015	9020	9025	1	i	2	2	3	3	4	4	5
80	9031	9036	9042	9047	9053	9058	9063	9069	9074	9079	1	1	2	2	3	3	4	4	5
81	9085	9090	9096	9101	9106	9112	9117	9122	9128	9133	1	1	2	2	3	3	4	4	5
82 83	9138 9191	9143 9196	9149 9201	9154 9206	9159 9212	9165 9217	9170 9222	9175 9227	9180 9232	9186 9238	1	1	2	2	3	3	4	4	5 5
84	9243			9258		9269	9274	9279		9289		i	2	2	3	3	4	4	5
85	9294	9299	9304	9309	9315	9320	9325	9330	9335	9340	1	1	2	2	3	3	4	4	5
86	9345	9350	9355	9360	9365	9370	9375	9380 9430	9385 9435	9390 9440	1	1	2	2	3	3	4	4	5
87 88	9395 9445	9400 9450	9405 9455	9410 9460	9415 9465	9420 9469	9425 9474	9479	9484	9489	0	1	1	2	2	3	3	4	5 4
89	9494	9499	9504	9509	9513	9518	9523	9528	9533	9538	ŏ	1	1	2	2	3	3	4	4
90	9542	9547	9552	9557	9562	9566	9571	9576	9581	9586	0	1	1	2	2	3	.3	4	4
91	9590	9595	9600	9605	9609	9614	9619	9624	9628	9633	0	1	1	2	2	3	3	4	4
92 93	9638 9685	9643 9689	9647 9694	9652 9699	9657 9703	9661 9708	9666 9713	9671 9717	9675 9722	9680 9727	0	1	1	2	2	3	3	4	4
94	9731	9736	9741	9745	9750	9754	9759	9763	9768	9773	0	1	1	2	2	3	3	4	4
95	9777	9782	9786	9791	9795	9800	9805	9809	9814	9818	0	1	1	2	2	3	3	4	4
96	9823	9827	9832	9836	9841	9845	9850	9854	9859	9863	0	1	1	2	2	3	3	4	4
97 98	9868 9912	9872 9917	9877 9921	9881 9926	9886 9930	9890 9934	9894 9939	9899 9943	9903 9948	9908 9952	0	1	1	2	2	3	3	4	4
99	9956	9961	9965	9969	9975	9978	9983	9987	9991	9996	0	1	1	2	2	3	3	3	4
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Antilogarithms

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00	1000	1002	1005	1007	1009	1012	1014	1016	1019	1021	0	0	1	1	1	1	2	2	2
01	1023	1026	1028	1030	1033	1035	1038	1040	1042	1045	ō	ő	1	1	1	1	2	2	2
	1047	1050	1052	1054	1057	1059	1062	1064	1067	1069	0	0	1	1	1	1	2 2 2	2	2
	1072	1074	1076	1079	1081	1084	1086	1089	1091	1094	0	0	1	1	1	1	2	2 2 2	2
04	1096	1099	1102	1104	1107	1109	1112	1114	1117	1119	0	1	1	1	1	2	2	2	2
	1122	1125	1127	1130	1132	1135	1138	1140	1143	1146	0	1	1	1	1	2	2	2	2
	1148	1151	1153	1156	1159	1161	1164	1167	1169	1172	0	1	1	1	1	2	2 2 2 2	2 2 2 2	2 2
	1175	1178	1180	1183	1186	1189	1191	1194	1197	1199	0	1	1	1	1	2	2	2	2
	1202 1230	1205 1233	1208 1236	1211	1213	1216	1219	1222	1225	1227	0	1	1	1	1	2	2	2	3
			1230	1239	1242	1245	1247	1250	1253	1256	0	1	1	1	1	2	2	2	3
	1259 1288	1262 1291	1265 1294	1268 1297	1271	1274	1276	1279	1282	1285	0	1	1	1	1	2	2	2	3
	1318	1321	1324	1327	1300 1330	1303 1334	1306 1337	1309 1340	1312 1343	1315 1346	0	1	1	1	2	2	2	2	3
	1349	1352	1355	1358	1361	1365	1368	1371	1374	1377	0	1	1		2	2	2	2	3
	1380	1384	1387	1390	1393	1396	1400	1403	1406	1409	-	1	1	1	2000	2	2 2 2	3	3
15	1413	1416	1419	1422	1426	1429	1432	1435	1439	1442	0	1	1	4	2	2	2	2	73
	1445	1449	1452	1455	1459	1462	1466	1469	1472	1476	0	1	1	1	2	2	2	3	3
	1479	1483	1486	1489	1493	1496	1500	1503	1507	1510	ŏ	1	1	1	2	2	2	3	3 3 3
	1514	1517	1521	1524	1528	1531	1535	1538	1542	1545	0	1	1	1	2	2	2	3	3
	1549	1552	1556	1560	1563	1567	1570	1574	1578	1581	0	1	1	i	2	2	3	3	3
20	1585	1589	1592	1596	1600	1603	1607	1611	1614	1618	0	1	1	1	2	2	3	3	3
21	1622	1626	1629	1633	1637	1641	1644	1648	1652	1656	Õ	1	i	2	2	2	3	3	3
22	1660	1663	1667		1675	1679	1683	1687	1690	1694	ŏ	1	1	2	2	2	3	3	3
	1698	1702	1706	1710	1714	1718	1722	1726	1730	1734	0	1	1	2	2222	2	3	3	4
24	1738	1742	1746	1750	1754	1758	1762	1766	1770	1774	0	1	1	2	2	2	3	3	4
25	1778	1782	1786	1791	1795	1799	1803	1807	1811	1816	0	1	1	2	2	2	3	3	4
26	1820	1824	1828	1832	1837	1841	1845	1849	1854	1858	0	1	1	2	2 2	3	3	3	4
27	1862	1866	1871	1875	1879	1884	1888	1892	1897	1901	. 0	1	1	2	2	3	3	3	4
28 29	1905 1950	1910 1954	1914	1919	1923	1928	1932	1936	1941	1945	0	1	1	2 2 2 2 2	2	3	3	4	4
23	1330	1934	1959	1963	1968	1972	1977	1982	1986	1991	0	1	1	2	2	3	3	4	4
30	1995 2042	2000	2004	2009 2056	2014 2061	2018	2023	2028	2032	2037	0	1	1	2	2 2	3	3	4	4
	2089	2094	2099	2104	2109	2065 2113	2070 2118	2075	2080	2084	0	1	1	2	2	3	3	4	4
	2138			2153	2158	2163		2123 2173	2128	2133	0	1	1	2		3	3	4	4
34	2188	2193	2198	2203	2208	2213	2218	2223	2178 2228	2183 2234	0	1	1 2	2	2	3	3	4	5
05												•				0	4	4	,
35	2239 2291	2244	2249	2254	2259	2265	2270	2275	2280	2286	1	1	2	2	3	3	4	4	5
36 37	2344	2296 2350	2301 2355	2307	2312	2317	2323	2328	2333	2339	1	1	2	2	3	3	4	4	5
38	2399	2404	2410	2360 2415	2366 2421	2371	2377	2382	2388	2393	1	1	2	2	3	3	4	4	5
39	2445	2460	2466	2472	2477	2427 2483	2432 2489	2438 2495	2443 2500	2449 2506	1	1	2	2	3	3	4	4 5	5 5
40	2512	2518	2523	2529	2535														
	2570	2576	2582	2588	2594	2541 2600	2547 2606	2553 2612	2559 2618	2564	1	1	2	2	3	4	4	5	5
	2630	2636	2642	2649	2655	2661	2667	2673	2679	2624 2685	1	1	2	2	3	4	4	5	5
	2692	2698	2704	2710	2716	2723	2729	2735	2742	2748	1	1	2	2	3	4	4	5	6
	2754	2761	2767	2773	2780	2786	2793	2799	2805	2812	1	1	2	3	3	4	4	5 5	5 6
45	2818	2825	2831	2838	2844	2851	2858	2864	2871	2877	4	4	2	2	2	4	e	r	
	2884	2891	2897	2904	2911	2917	2924	2931	2938	2944	1	1	2	3	3	4	5	5	6
	2951	2958	2965	2972	2979	2985	2992	2999	3006	3013	1	1	2	3	3	4	5 5	5 5	6
	3020	3027	3034	3041	3048	3055	3062	3069	3076	3083	1	1	2	3	4	4	5	6	6
	3090	3097	3105	3112	3119	3126	3133	3141	3148	3155	1	1	2	3	4	4	5	6	6
	0	1	2	3	4	5	6	7	8	9	1	2	3	4	5	6	7	8	9
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Antilogarithms

	0	1	2	3	4	5	6	7	8	9	1	2	3	4	5	6	7	- 8	9
.51 .52 .53	3162 3236 3311 3388 3467	3170 3243 3319 3396 3475	3177 3251 3327 3404 3483	3184 3258 3334 3412 3491	3192 3266 3342 3420 3499	3199 3273 3350 3428 3508	3206 3281 3357 3436 3516	3214 3289 3365 3443 3524	3221 3296 3373 3451 3532	3228 3304 3381 3459 3540	1 1 1 1 1	1 2 2 2 2 2	2 2 2 2 2	3 3 3 3	4 4 4 4 4	4 5 5 5	5 5 6 6	6	7 7 7
.56 .57	3548 3631 3715 3802 3890	3556 3639 3724 3811 3899	3565 3648 3733 3819 3908	3573 3656 3741 3828 3917	3581 3664 3750 3837 3926	3589 3673 3758 3846 3936	3597 3681 3767 3855 3945	3606 3690 3776 3864 3954	3614 3698 3784 3873 3963	3622 3707 3793 3882 3972	1 1 1 1	2 2 2 2 2	2 3 3 3	3 3 4 4	4 4 4 5	5 5 5 5	6 6 6	7 7 7 7 7	7 8 8
.61 .62 .63	3981 4074 4169 4266 4365	3990 4083 4178 4276 4375	3999 4093 4188 4285 4385	4009 4102 4198 4295 4395	4018 4111 4207 4305 4406	4027 4121 4217 4315 4416	4036 4130 4227 4325 4426	4046 4140 4236 4335 4436	4055 4150 4246 4345 4446	4064 4159 4256 4355 4457	1 1 1	2 2 2 2	3 3 3 3	4 4 4 4	5 5 5 5	666666	6 7 7 7 7	7 8 8 8	9
.66 .67 .68	4467 4571 4677 4786 4898	4477 4581 4688 4797 4909	4487 4592 4699 4808 4920	4498 4603 4710 4819 4932	4508 4613 4721 4831 4943	45.19 4624 4732 4842 4955	4529 4634 4742 4853 4966	4539 4645 4753 4864 4977	4550 4656 4764 4875 4989	4560 4667 4775 4887 5000	1 1 1 1	22222	33333	4 4 4 5	5 5 6 6	6 6 7 7 7	7 7 8 8	8 9 9 9	
.71 .72 .73	5012 5129 5248 5370 5495	5023 5140 5260 5383 5508	5035 5152 5272 5395 5521	5047 5164 5284 5408 5534	5058 5176 5297 5420 5546	5070 5188 5309 5433 5559	5082 5200 5321 5445 5572	5093 5212 5333 5458 5585	5105 5224 5346 5470 5598		1 1 1	2 2 3 3	4 4 4 4	5 5 5 5 5	6 6 6	7 7 7 8 8	8 9 9		
	5623 5754 5888 6026 6166	5636 5768 5902 6039 6180	5649 5781 5916 6053 6194	5662 5794 5929 6067 6209	5675 5808 5943 6081 6223	5689 5821 5957 6095 6237	5702 5834 5970 6109 6252	5715 5848 5984 6124 6266	5728 5861 5998 6138 6281	5741 5875 6012 6152 6295	1 1 1 1 1	3 3 3 3	4 4 4 4	5 5 6 6	7 7 7 7	8 8 8 9	9	11	
.81 .82	6310 6457 6607 6761 6918	6324 6471 6622 6776 6934	6339 6486 6637 6792 6950	6353 6501 6653 6808 6966	6368 6516 6668 6823 6982	6383 6531 6683 6839 6998	6397 6546 6699 6855 7015	6412 6561 6714 6871 7031	6427 6577 6730 6887 7047	6442 6592 6745 6902 7063	1 2 2 2 2	3 3 3 3	4 5 5 5	6 6 6	7 8 8 8	9 9 9 9	11 11 11	12 12 12 13	14 14 14
.86 .87 .88	7079 7244 7413 7586 7762	7096 7261 7430 7603 7780	7112 7278 7447 7621 7798	7129 7295 7464 7638 7816	7145 7311 7482 7656 7834	7161 7328 7499 7674 7852	7178 7345 7516 7691 7870	7194 7362 7534 7709 7889	7211 7379 7551 7727 7907	7228 7396 7568 7745 7925	2 2 2 2	3 3 4 4	5 5 5 5 5	7 7 7 7 7	9	10 10 10 11 11	12 12 12	13 13 14 14 14	15 16 16
.91 .92 .93	7943 8128 8318 8511 8710	7962 8147 8337 8531 8730	7980 8166 8356 8551 8750	7998 8185 8375 8570 8770	8017 8204 8395 8590 8790	8035 8222 8414 8610 8810	8054 8241 8433 8630 8831	8072 8260 8453 8650 8851	8091 8279 8472 8670 8872	8110 8299 8492 8690 8892	2 2 2 2	4 4 4 4	6 6 6 6	8	910	11 11 12 12 12	13 14 14	15 15 15 16 16	17 17 18
.96 .97 .98	8913 9120 9333 9550 9772	8933 9141 9354 9572 9795	8954 9162 9376 9594 9817	8974 9183 9397 9616 9840	8995 9204 9419 9638 9863	9016 9226 9441 9661 9886	9036 9247 9462 9683 9908	9057 9268 9484 9705 9931	9078 9290 9506 9727 9954	9099 9311 9528 9750 9977	2 2 2 2 2	4 4 4 5	6 7 7	9	11	13 13 13	15 15 16	17 17 17 18 18	19 20 20
	0	1	2	3	4	5	6	7	8	9	1.	2	3	4 5	5 6)	7	8	9

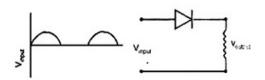
PART A

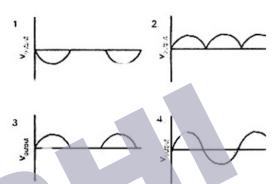
- 1 A physiological disorder X always leads to the disorder Y. However, disorder Y may occur by itself. A population shows 4% incidence of disorder Y. Which of the following inferences is valid?
 - 1 4% of the population suffers from both X & Y
 - Less than 4% of the population suffers from X
 - At least 4% of the population suffers from X
 - 4. There is no incidence of X in the given population
- 2. Exposing an organism to a certain chemical can change nucleotide bases in a gene, causing mutation. In one such mutated organism if a protein had only 70% of the primary amino acid sequence, which of the following is likely?
 - 1. Mutation broke the protein
 - The organism could not make amino acids
 - 3. Mutation created a terminator cogon
 - 4. The gene was not transcribed
- 3. The speed of a car increases every minute as shown in the following Table. The speed at the end of the 19th minute would be

Speed (m/sec)							
1.5							
3.0							
4.5							
36.0							
37.5							

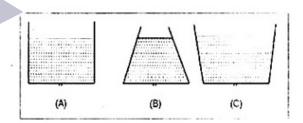
- 1. 26.5
- 2. 28.0
- 3. 27.0
- 4. 28.5

4. If V_{input} is applied to the circuit shown, the output would be





 Water is dripping out of a tiny hole at the bottom of three flasks whose base diameter is the same, and are initially filled to the same height, as shown

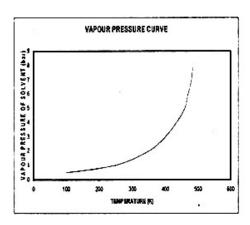


Which is the correct comparison of the rate of fall of the volume of water in the three flasks?

- 1. A fastest, B slowest
- 2. B fastest, A slowest
- 3. B fastest, C slowest
- 4. C fastest, B slowest
- 6. A reference material is required to be prepared with 4 ppm calcium. The amount of CaCO₃ (molecular weight = 100) required to prepare 1000 g of such a reference material is
 - 1. 10 µg
 - 2. 4 µg
 - 4 mg
 - 4. 10 mg

8

7.

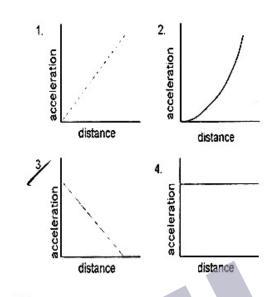


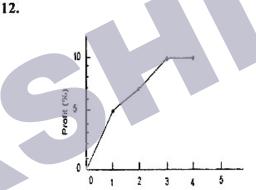
The normal boiling point of a solvent (whose vapour pressure curve is shown in the figure) on a planet whose normal atmospheric pressure is 3 bar, is about

- 1. 100 K
- 2. 273 K
- 3. 400 K
- 4. 500 K
- 8. How many σ bonds are present in the following molecule?

 $HC \equiv CCH = CHCH_3$

- 1. 4
- 2. 6
- 3. 10
- 4. 13
- 9. The reason for the hardness of diamond is
 - extended covalent bonding
 - layered structure
 - 3. formation of cage structures
 - 4. formation of tubular structures
- 10. The acidity of normal rain water is due to
 - ₹. SO₂
 - 2. CO₂
 - NO₂
 - 4. NO
- 11. A ball is dropped from a height h above the surface of the earth. Ignoring air drag, the curve that best represents its variation of acceleration is





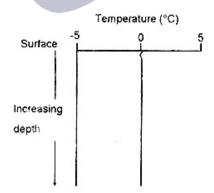
The cumulative profits of a company since its inception are shown in the diagram. If the net worth of the company at the end of 4th year is 99 crores, the principal it had started with was

- 1. 9.9 crores
- 2. 91 crores
- 3. 90 crores
- 4. 9.0 crores
- 13. Diabetic patients are advised a low glycaemic index diet. The reason for this is
 - They require less carbohydrate than healthy individuals
 - 2. They cannot assimilate ordinary carbohydrates
 - 3. They need to have slow, but sustained release of glucose in their blood stream
 - They can tolerate lower, but not higher than normal blood sugar tevels

- 14. Standing on a polished stone floor one feels colder than on a rough floor of the same stone.

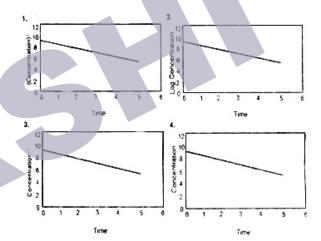
 This is because
 - 1. Thermal conductivity of the stone depends on the surface smoothness
 - Specific heat of the stone changes by polishing it
 - 3. The temperature of the polished floor is lower than that of the rough floor
 - There is greater heat loss from the soles of the feet when in contact with the polished floor than with the rough floor
- 15. Popular use of which of the following fertilizers increases the acidity of soil?
 - 1. Potassium Nitrate
 - 2. Urea
 - 3. Ammonium sulphate
 - 4. Superphosphate of lime
- 16. If the atmospheric concentration of carbon dioxide is doubled and there are favourable conditions of water, nutrients, light and temperature, what would happen to water requirement of plants?
 - 1. It decreases initially for a short time and then returns to the original value
 - 2. It increases
 - 3. It decreases
 - 4. It increases initially for a short time and then returns to the original value

17.



The graph represents the depth profile of temperature in the open ocean; in which region this is likely to be prevalent?

- 1. Tropical region
- 2. Equatorial region
- 3. Polar region
- 4. Sub-tropical region
- 18. Glucose molecules diffuse across a cell of diameter d in time τ . If the cell diameter is tripled, the diffusion time would
 - increase to 9τ
 - decrease to τ/3
 - increase to 3τ
 - decrease to τ/9
- 19. Identify the figure which depicts a first order reaction.



- 20. Which of the following particles has the largest range in a given medium if their initial energies are the same?
 - 1. alpha
 - 2. electron
 - 3. positron
 - 4. gamma

PART B

21. Let $S = \{A : A = [a_{ij}]_{s < s}, a_{ij} = 0 \text{ or } 1 \,\forall i, j, \}$

$$\sum_{j} a_{ij} = 1 \ \forall i \ \text{and} \quad \sum_{i} a_{ij} = 1 \ \forall j \ \right\}.$$

Then the number of elements in S is

- 1. 5²
- 2. 5⁵
- 3. 5!
- 4. 55
- The number of 4 digit numbers with no two digits common is
 - 1. 4536
 - 2. 3024
 - 3. 5040
 - 4. 4823
- 23. Let D be a non-zero n×n real matrix with n ≥ 2. Which of the following implications is valid?
 - 1. det (D) = 0 implies rank (D) = 0
 - 2. det(D) = 1 implies rank $(D) \neq 1$
 - 3. rank(D) = 1 implies $det(D) \neq 0$
 - 4: rank (D) = n implies det (D) \neq 1
- **24.** Let $f_n(x) = x^{1/n}$ for $x \in [0, 1]$. Then
 - 1. $\lim_{n\to\infty} f_n(x)$ exists for all $x \in [0,1]$.
 - 2. $\lim_{n\to\infty} f_n(x)$ defines a continuous function on [0,1].
 - 3. $\{f_n\}$ converges uniformly on [0,1].
 - 4. $\lim_{n\to\infty} f_n(x) = 0$ for all $x \in [0,1]$.
- 25. Let $A = \{x^2 : 0 \le x \le 1\}$ and $B = \{x^3 : 1 \le x \le 2\}$. Which of the following statements is true?
 - There is a one to one, onto function from A to B.
 - There is no one to one, onto function from A to B taking rationals to rationals.
 - There is no one to one function from A to B which is onto.
 - 4. There is no onto function from A to akshieducation.com which is one to one

26. Let ζ be a primitive fifth root of unity.

Define

$$A = \begin{pmatrix} \zeta^{-2} & 0 & 0 & 0 & 0 \\ 0 & \zeta^{-1} & 0 & 0 & 0 \\ 0 & 0 & 1 & 0 & 0 \\ 0 & 0 & 0 & \zeta & 0 \\ 0 & 0 & 0 & 0 & \zeta^2 \end{pmatrix}.$$

For a vector $v = (v_1, v_2, v_3, v_4, v_5) \in \mathbb{R}^5$,

define $|\mathbf{v}|_d = \sqrt{|\mathbf{v}A\mathbf{v}^T|}$ where \mathbf{v}^1 is transpose of \mathbf{v} . If $\mathbf{w} = (1, -1, 1, 1, -1)$, then $|\mathbf{w}|_A$ equals

- 1. 0
- 2. 1
- 3. -1
- 4. 2
- 27. The number of elements in the set { m : 1 ≤ m ≤ 1000, m and 1000 are relatively prime} is
 - 1. 100
 - 2. 250
 - 3. 300
 - 4 400
- 28. The unit digit of 2100 is
 - 1. 2
 - 2 4
 - 3. 6
 - 4. 8
- 29. The dimension of the vector space of all symmetric matrices of order n × n (n ≥ 2) will real entries and trace equal to zero is
 - 1. $(n^2 n)/2 1$
 - 2. $(n^2 + n)/2 1$
 - 3. $(n^2-2n)/2-1$
 - 4. $(n^2 + 2n)/2 1$

11

30 Let
$$I = \{1\} \cup \{2\} \subset \mathbb{R}$$
. For $x \in \mathbb{R}$, let $\varphi(x) = \text{dist } (x, I) = \inf \{|x-y| : y \in I\}$. Then

- 1. φ is discontinuous somewhere on \mathbb{R} .
- φ is continuous on R but not differentiable only at x = 1.
- 3 φ is continuous on \mathbb{R} but not differentiable only at x = 1 and 2.
- 4. φ is continuous on \mathbb{R} but not differentiable only at x = 1, 3/2 and 2.

31. The set
$$\left\{\frac{1}{n}\sin\frac{1}{n}: n \in \mathbb{N}\right\}$$
 has

- 1. one limit point and it is 0
- 2. one limit point and it is 1
- 3. one limit point and it is -1
- three limit points and these are -1, 0 and 1

32. Using the fact that

$$\sum_{1}^{\infty} \frac{(-1)^{n+1}}{n} = \log 2, \sum_{1}^{\infty} \frac{(-1)^{n}}{n(n+1)}$$
 equals

- 1. $1 2 \log 2$
- 2. $1 + \log 2$
- 3. $(log 2)^2$
- 4. $-(log 2)^2$
- 33. Let f: C→C be a complex valued function given by

$$f(z) = u(x,y) + iv(x,y).$$

Suppose that $v(x, y) = 3xy^2$. Then

- f cannot be holomorphic on C for any choice of u.
- 2. f is holomorphic on \mathbb{C} for a suitable choice of u.
- 3 f is holomorphic on C for all choices of u.
- y is not differentiable as a function of x and y.

34. For
$$V = (V_1, V_2) \in \mathbb{R}^2$$
 and $W = (W_1, W_2) \in \mathbb{R}^2$, consider the determinant map

$$\det: \mathbb{R}^2 \times \mathbb{R}^2 \to \mathbb{R}$$
 defined by

$$\det(V,W) = V_1W_2 - V_2W_1$$

Then the derivative of the determinant map at $(V, W) \in \mathbb{R}^2 \times \mathbb{R}^2$ evaluated on $(H, K) \in \mathbb{R}^2 \times \mathbb{R}^2$ is

- 1. $\det(H,W) + \det(V,K)$
- 2. det (H, K)
- 3 $\det(H,V) + \det(W,K)$
- det (V, H) + det (K, W)
- 35. Let W be the vector space of all real polynomials of degree at most 3. Define
 T: W W by (Tp)(x) = p'(x) where p' is the derivative of p. The matrix of T in the basis

derivative of p. The matrix of T in the basis $\{1, x, x^2, x^3\}$, considered as column vectors, is given by

- **36.** The degree of the extension $\mathbb{Q}(\sqrt{2} + \sqrt[3]{2})$ over the field $\mathbb{Q}(\sqrt{2})$ is
 - 1.
 - 2 2
 - 3. 3
 - 4 6

37. The power series
$$\sum_{n=0}^{\infty} 2^{-n} z^{2n}$$
 converges if

- 1. $|z| \leq 2$
- 2. |z| < 2
- 3. $|z| \le \sqrt{2}$
- 4 $|z| < \sqrt{2}$

38. Consider a group G. Let Z(G) be its centre, i.e., Z(G) = {g ∈ G: gh = hg for all h ∈ G}.
For n∈N, the set of positive integers, define

$$J_n = \{(g_1, \dots, g_n) \in Z(G) \times \dots \times Z(G) : g_1 \dots g_n = e\}.$$

As a subset of the direct product group $Gx \cdots xG$ (n times direct product of the group G), J_n is

- 1. not necessarily a subgroup.
- a subgroup but not necessarily a normal subgroup.
- 3. a normal subgroup.
- isomorphic to the direct product Z(G) ×···×Z(G) ((n-1) times).
- 39. Let I_1 be the ideal generated by x^4+3x^2+2 and I_2 be the ideal generated by x^3+1 in $\mathbb{Q}[x]$. If $F_1 = \mathbb{Q}[x]/I_1$ and $F_2 = \mathbb{Q}[x]/I_2$, then
 - 1. F₁ and F₂ are fields.
 - 2. F₁ is a field, but F₂ is not a field.
 - 3. F₁ is not a field while F₂ is a field.
 - 4. neither F₁ nor F₂ is a field.
- 40. Let G be a group of order 77. Then the center of G is isomorphic to
 - 1. Z₍₁₎
 - 2 Z₍₇₎
 - 3. Z(11)
 - 4. Z(77)
- 41. Let P be a polynomial of degree N, with $N \ge 2$. Then the initial value problem u'(t) = P(u(t)), u(0) = 1 has always
 - 1. a unique solution in R.
 - N number of distinct solution in R.
 - no solution in any interval containing 0 for some P.
 - 4. a unique solution in an interval containing 0.

42. Consider the ODE $u''(t) + P(t)u'(t) + Q(t)u(t) = R(t), t \in [0,1]$

There exist continuous functions P, Q and R defined on [0, 1] and two solutions u_1 and u_2 of this ODE such that the Wronskian W of u_1 and u_2 is

- 1. W(t) = 2t 1, $0 \le t \le 1$
- 2. $W(t) = \sin 2\pi t$, $0 \le t \le 1$
- 3. $W(t) = \cos 2\pi t$, $0 \le t \le 1$
- 4. W(t) = 1. $0 \le t \le 1$
- 43. The number of characteristic curves of the PDE

$$(x^2 + 2y) u_{xx} + (y^3 - y + x)u_{yy} + x^2 (y-1)u_{xy} + 3u_x + u = 0$$

passing through the point $x = 1$, $y = 1$ is

- 1. 0
- 2. 1
- 3, 2
- 4. 3
- 44. A general solution of the second order Equation

 $4 u_{xx} - u_{yy} = 0$ is of the form u(x,y) =

- 1. f(x) + g(y)
- 2. f(x + 2y) + g(x 2y)
- 3. f(x + 4y) + g(x-4y)
- 4. f(4x + y) + g(4x y)

where f and g are twice differentiable functions.

- 45 Consider the function $f(x) = e^{-x}$ and its Taylor approximation g(x) of degree 3. For $x = \frac{1}{3}$, g(x) is
 - 1. positive and less than 1
 - 2 negative and less than -2
 - 3. positive and greater than I
 - 4. less than 1 but greater than 0.75

46. The variational problem of extremizing the functional

$$I(y(x)) = \int_0^{2\pi} \left[\left(\frac{d}{dx} y \right)^2 - y^2 \right] dx; \ y(0) = 1, y(2z) = 1$$

has

- 1. a unique solution
- 2 exactly two solutions
- 3. an infinite number of solutions
- 4. no solution
- 47. For the Volterra type linear integral equation

$$\phi(x) = x + 2 \int_{0}^{x} e^{x-\zeta} \phi(\zeta) d\zeta,$$

the resolvent kernel $R(x,\zeta;2)$ of the kernel $e^{x-\zeta}$ is

- 1. $(x-\zeta)^2 e^{2(x-\zeta)}$
- 2. $(x-\zeta)e^{x-\zeta}$
- 3. $e^{3(x-\zeta)}$
- 4. $e^{(x-\zeta)}$
- 48. Which of the following is/are correct
 - A free particle in R³ can have infinite degrees of freedom
 - 2. The number of degree of freedom of N particles is greater than 3N
 - A system of N particles with k constants has 3N + k degrees of freedom
 - A system consisting of three point masses connected by three rigid massless rods has six degrees of freedom.
- 49. A system of 5 identical units consists of two parts A and B which are connected in series. Part A has 2 units connected in parallel and part B has 3 units connected in parallel. All the 5 units function independently with probability of failure $\frac{1}{2}$. Then the reliability of the system is
 - 1. $\frac{31}{32}$
 - 2. $\frac{11}{32}$

- 3. $\frac{1}{32}$
- 4. $\frac{21}{32}$
- **50.** Suppose X_1, X_2, \cdots is an i.i.d. sequence of random variables with common variance

$$\sigma^2 > 0$$
. Let $Y_n = \frac{1}{n} \sum_{i=1}^n X_{2i-1}$ and

$$Z_n = \frac{1}{n} \sum_{i=1}^n X_{2i}$$

Then the asymptotic distribution (as $n \to \infty$) of $\sqrt{n}(Y_n - Z_n)$ is

- 1. N(0,1)
- 2 $N(0, \sigma^2)$
- 3. $N(0, 2\sigma^2)$
- degenerate at 0
- 51. Consider an aperiodic Markov chain with state space S and with stationary transition probability matrix $P = ((p_{ij})), i, j \in S$. Let the n-step transition probability matrix be denoted by $P'' = ((p_{ij})), i, j \in S$. Then which of the following statements is true?
 - 1. $\lim_{n\to\infty} p_{ii}^n = 0$ only if *i* is transient.
 - 2 $\lim_{n \to \infty} p_{ii}^n > 0$ if and only if *i* is recurrent.
 - 3. $\lim_{n\to\infty} p_{ij}^n = \lim_{n\to\infty} p_{jj}^n$ if i and j are in the same communicating class.
 - 4. $\lim_{n\to\infty} p_{ij}^n = \lim_{n\to\infty} p_{ii}^n$ if i and j are in the same communicating class.
- 52. Suppose X is a random variable with E(X) = Var(X). Then the distribution of X
 - 1. is necessarily Poisson.
 - 2 is necessarily Exponential.
 - 3. is necessarily Normal.
 - 4. cannot be identified from the given data.

53. Let x=10 be an observation on the hypergeometric random variable X, namely

$$P(X = x) = \frac{\binom{m}{x}\binom{N-m}{n-x}}{\binom{N}{n}}, x = 0, 1, \dots,$$

 $\min\{m,n\}$ and $n-x \le N-m$

where m=40, n=30 and N is an unknown parameter. The maximum likelihood estimator of N is

- 1. 120
- 2 75
- 3. 60
- 4. not unique
- 54. Let X_1, X_2, \dots, X_n , $n \ge 2$, be i.i.d. observations from $N(0, \sigma^2)$ distribution, where $0 < \sigma^2 < \infty$ is an unknown parameter. Then the uniformly minimum variance unbiased estimate for σ^2 is
 - 1. $\frac{1}{n}\sum_{i=1}^{n}X_{i}^{2}$
- $2 \frac{1}{n-1} \sum_{i=1}^{n} X_i^2$
 - $3. \quad \frac{1}{n} \sum_{i=1}^{n} \left(X_i \overline{X} \right)$
 - 4. $\frac{1}{n-1}\sum_{i=1}^{n}(X_{i}-\bar{X})^{2}$
 - 55. Suppose that we have i.i.d. observations (X₁, Y₁), (X₂, Y₂),···, (Xₙ, Yո), n ≥ 3, where Xᵢ and Yᵢ are independent normal random variables. Consider τ = the sample Kendall's rank correlation coefficient computed from this data. Then which of the following is correct?
 - 1. $P(\tau > 0) > \frac{1}{2}$
 - 2. $P(\tau < 0) > \frac{1}{2}$
 - 3. $E(\tau) = 0$
 - 4. $E(\tau) \neq 0$

56.The reaction time to a stimulus X (in seconds) is distributed normally in

group 1 with mean 2 and variance 8; group 2 with mean 4 and variance 1.

The two groups appear in equal proportions. x is an observable value of X. The best discriminant function (in the sense of minimizing misclassification probabilities) is to classify into group

- 1. 2 if x > 3; otherwise in group 1
- 2 1 if x > 3; otherwise in group 2
- 3. 2 if $0 \le x \le \frac{8}{3}$; otherwise in group 1
- 4. 1 if $0 \le x \le \frac{8}{3}$; otherwise in group 2
- 57. Batteries for torch lights are packed in boxes of 10 and a lot contains 10 boxes. A quality inspector randomly chooses a box and then checks two batteries selected randomly without replacement from that box. The lot will be rejected if any one of the two chosen batteries turns out to be defective. Suppose that 9 of the 10 boxes in the lot contain no defective batteries and only one box contains 2 defective ones. What is the probability that the lot will NOT be passed by the Inspector?
 - 1. $\frac{197}{4950}$
 - 2. $\frac{98}{2475}$
 - 3. $\frac{8}{225}$
 - 4. $\frac{17}{450}$
- 58. To examine whether two different skin creams, A and B, have different effect on the human body *n* randomly chosen persons were enrolled in a clinical trial. Then cream A was applied to one of the randomly chosen arms of each person, cream B to the other. What kind of a design is this?
 - Completely Randomized Design
 - 2. Balanced Incomplete Block Design
 - 3. Randomized Block Design
 - 4. Latin Square Design

Consider the LP problem maximize $x_1 + x_2$

subject to

$$x_1 - 2x_2 \le 10$$

$$x_2 - 2x_1 \le 10$$

$$x_1, x_2 \ge 0$$

Then

- 1. The LP problem admits an optimal
- The LP problem is unbounded
- The LP problem admits no feasible
- 4. The LP problem admits a unique feasible solution
- **60**. Let X(t) be the number of customers in an M/M/1 queueing system with arrival rate 3 and service rate 6. Which of the following is true?
 - 1. $\lim_{t\to\infty} P(X(t) \ge 5) = 0$
 - 2. $\lim_{t \to \infty} P(X(t) \ge 5) = \frac{1}{32}$
 - 3. $\lim_{t\to\infty} P(X(t) \ge 5) = \frac{31}{32}$
 - 4. $\lim P(X(t) \ge 5) = 1$



Unit I

Consider the function

$$f(x) = |\cos x| + |\sin(2-x)|.$$

At which of the following points is f not differentiable?

1.
$$\left\{ (2n+1)\frac{\pi}{2} : n \in \mathbb{Z} \right\}$$

- 2. $\{n\pi: n\in\mathbb{Z}\}$
- 3. $\{n\pi+2: n\in\mathbb{Z}\}$
- $4. \quad \left\{ \frac{n\pi}{2} : n \in \mathbb{Z} \right\}$

- 62. Which of the following subsets of R2 are convex?
 - 1. $\{(x, y) : |x| \le 5 |y| \le 10\}$ 2. $\{(x, y) : x^2 + y^2 = 1\}$

 - 3. $\{(x, y) : y \ge x^2\}$
 - 4. $\{(x, y) : y \le x^2\}$
- 63. Which of the following is/are metrics on R?
 - d(x, y) = min(x, y)
 - d(x, y) = |x y|

 - 3. $d(x, y) = |x^2 y^2|$ 4. $d(x, y) = |x^3 y^3|$
- 64. Let X denote the two-point set {0, 1} and write $X_i = \{0, 1\}$ for every j = 1, 2, 3, ... Let $Y = \prod_{i=1}^{\infty} X_i$. Which of the following is/are true?
 - Y is a countable set.
 - Card Y = card [0,1].
 - $\bigcup_{i=1}^{n} X_{i}$ is uncountable.
 - Y is uncountable.
- 65. Which of the following is/are correct?
 - 1. $n\log\left(1+\frac{1}{n+1}\right) \to 1 \text{ as } n\to\infty$
 - 2. $(n+1)\log\left(1+\frac{1}{n}\right) \to 1 \text{ as } n\to\infty$
 - 3. $n^2 \log \left(1 + \frac{1}{n}\right) \to 1 \text{ as } n \to \infty$
 - 4. $n\log\left(1+\frac{1}{n^2}\right) \to 1 \text{ as } n\to\infty$
- **66.** If $\{x_n\}$ and $\{y_n\}$ are sequences of real numbers, which of the following is/are true?
 - $\limsup (x_n + y_n) \le \limsup x_n + \limsup y_n$
 - 2. $\limsup_{n \to \infty} (x_n + y_n) \ge \limsup_{n \to \infty} x_n + \limsup_{n \to \infty} y_n$
 - 3. $\liminf_{x_n+y_n} \sup \lim \inf_{x_n+1} \lim \inf y_n$
 - 4. $\liminf_{x_n + y_n \ge \lim \inf x_n + \lim \inf y_n}$

- 67. Let {f_n}be a sequence of integrable functions defined on an interval [a, b]. Then
 - 1. If $f_n(x) \to 0$ a.e., then $\int_a^b f_n(x) dx \to 0$
 - 2.If $\int_{a}^{b} f_n(x) dx \rightarrow 0$, then $f_n(x) \rightarrow 0$ a.e.
 - 3.If $f_n(x) \to 0$ a.e. and each f_n is a bounded function, then $\int_a^b f_n(x) dx \to 0$
 - 4.If $f_n(x) \to 0$ a.e. and the f_n 's are uniformly bounded, then $\int_a^b f_n(x) dx \to 0$
- **68.** For $x = (x_1, x_2,...,x_d) \in \mathbb{R}^d$, and $p \ge 1$, define

$$||x||_p = \left(\sum_{j=1}^{n} |x_j|^p\right)^{1/p}$$
 and

 $||x||_{\infty} = \max\{|x_j|: j=1,2,\ldots d\}$. Which of the

following inequalities hold for all $x \in \mathbb{R}^d$?

- 1. $||x|| \ge ||x|| \ge ||x||$
- $2. \quad \|x\| \le d \|x\|$
- 3. $||x|| \le \sqrt{d} ||x||_{\infty}$
- 4. $||x|| \le \sqrt{d} ||x||_2$
- 69. Consider the map $f: \mathbb{R}^2 \to \mathbb{R}^2$ defined by $f(x,y) = (3x 2y + x^2, 4x + 5y + y^2)$. Then
 - 1. f is discontinuous at (0, 0).
 - f is continuous at (0, 0) and all directional derivatives exist at (0, 0).
 - 3 f is differentiable at (0, 0) but the derivative Df(0,0) is **not** invertible.
 - f is differentiable at (0, 0) and the derivative Df (0, 0) is invertible

- 70. Which of the following sets are dense in \mathbb{R} with respect to the usual topology.
 - 1. $\{(x,y)\in\mathbb{R}^2:x\in\mathbb{N}\}$
 - 2. $\{(x, y) \in \mathbb{R}^2 : x + y \text{ is a rational number}\}$
 - 3. $\{(x, y) \in \mathbb{R}^2 : x + y^2 = 5\}$
 - 4. $\{(x, y) \in \mathbb{R}^2 : xy \neq 0\}$
- 71. Let

$$F = \{ f : \mathbb{R} \to \mathbb{R} : |f(x) - f(y)| \le K |(x - y)|^{\alpha} \}.$$

for all $x, y \in \mathbb{R}$ and for some $\alpha > 0$ and some K > 0.

Which of the following 1s/are true?

- 1. every $f \in F$ is continuous
- every f∈F is uniformly continuous
- 3. every differentiable function f is in F
- 4. every $f \in F$ is differentiable.
- 72. Let $a_{ij} = a_i a_j$, $1 \le i, j \le b$, where $a_1, ..., a_n$ are real numbers. Let $A = ((a_{ij}))$ be the $n \times n$ matrix $((a_{ij}))$. Then
 - It is possible to choose a₁,...,a_n so as to make the matrix A non-singular.
 - 2. The matrix A is positive definite if $(a_1,...,a_n)$ is a nonzero vector
 - 3. The matrix A is positive semidefinite for all $(a_1, ..., a_n)$.
 - For all (a₁,...,a_n), zero is an eigenvalue of A.
- 73. Suppose A, B are n × n positive definite matrices and I be the n × n identity matrix. Then which of the following are positive definite.
 - 1. A+B
 - 2. ABA
 - A²+I
 - AB

- 74. Let T be a linear transformation on the real vector space \mathbb{R}^n over \mathbb{R} such that $T^2 = \lambda T$ for some $\lambda \in \mathbb{R}$. Then
 - 1. $|| Tx || = |\lambda| || x ||$ for all $x \in \mathbb{R}^n$.
 - 2. If ||Tx|| = ||x|| for some non-zero vector $x \in \mathbb{R}^n$, then $\lambda = \pm 1$
 - 3. $T = \lambda I$ where I is the identity transformation on \mathbb{R}^n .
 - 4. If ||Tx|| > ||x|| for a nonzero vector $x \in \mathbb{R}^n$, then T is necessarily singular.
 - 75. Let M be the vector space of all 3 × 3 real matrices and let

$$A = \begin{pmatrix} 2 & 1 & 0 \\ 0 & 2 & 0 \\ 0 & 0 & 3 \end{pmatrix}$$

Which of the following are subspaces of M?

- 1. $\{X \in M : XA = AX\}$
- 2. $\{X \in M : X + A = A + X\}$
- 3. $\{X \in M : \text{trace } (AX) = 0\}$
- 4. $\{X \in M : \det(AX) = 0\}$
- 76. Let $W = \{p(B) : p \text{ is a polynomial with real } 0 = 1 = 0 = 0 = 0$ coefficients, where $B = \begin{bmatrix} 0 & 1 & 0 \\ 0 & 0 & 1 \\ 1 & 0 & 0 \end{bmatrix}$

The dimension d of the vector space W satisfies

- 1. $4 \le d \le 6$
- 2. $6 \le d \le 9$
- 3. $3 \le d \le 8$
- 4. $3 \le d \le 4$
- 77. Let N be a 3×3 nonzero matrix with the property N³ = 0. Which of the following is/are true?
 - 1. N is not similar to a diagonal matrix.
 - 2. N is similar to a diagonal matrix.
 - N has one non-zero eigenvector.
 - N has three linearly independent eigenvector.

78. Let $x, y \in \mathbb{C}^n$. Consider

$$f(x,y) = \sup_{\theta, \omega} \left\| e^{i\theta} x - e^{i\varphi} y \right\|_{2}, \ \theta, \phi \in \mathbb{R}.$$

Which of the following is/are correct?

1.
$$f(x, y) \le ||x||^2 + ||y||^2 - 2Re|\langle x, y \rangle|$$

2.
$$f(x, y) \le ||x||^2 + ||y||^2 + 2Re|\langle x, y \rangle|$$

3.
$$f(x, y) = ||x||^2 + ||y||^2 + 2|\langle x, y \rangle|$$

4.
$$f(x, y) \ge ||x||^2 + ||y||^2 - 2Re\langle x, y \rangle$$

Unit II

- 79. Let $\mathbb{D} = \{z \in \mathbb{C} : |z| < 1\}$ be the unit disc. Let
 - $f: \mathbb{D} \to \mathbb{C}$ be an analytic function

satisfying
$$f\left(\frac{1}{n}\right) = \frac{2n}{3n+1}$$
 for $n \ge 1$. Then

- 1. f(0) = 2/3
- 2. f has a simple pole at z = -3
- 3. f(3) = 1/3
- 4. no such f exists
- **80.** Let f be an entire function. If Re f is bounded then
 - 1. Im f is constant
 - 2. f is constant
 - 3. $f \equiv 0$
 - 4. f' is non zero constant
- 81. Let $f: \mathbb{D} \to \mathbb{D}$ be holomorphic with $f(0) = \frac{1}{2}$ and f(1/2) = 0, where $\mathbb{D} = \{z : |z| \le 1\}$. Which of the following is correct?
 - 1. $|f'(0)| \le 3/4$
 - 2. $|f'(1/2)| \le 4/3$
 - 3. $|f'(0)| \le 3/4$ and $|f'(1/2)| \le 4/3$
 - 4. $f(z) = z, z \in \mathbb{D}$

82. Define
$$H^+ = \{z \in \mathbb{C} : y > 0\}$$

 $H^- = \{z \in \mathbb{C} : y < 0\}$
 $L^+ = \{z \in \mathbb{C} : x > 0\}$
 $L^- = \{z \in \mathbb{C} : x < 0\}$

The function $f(z) = \frac{z}{3z+1}$

- 1. maps H onto H and H onto H
- 2. maps H onto H and H onto H
- 3. maps H+ onto L+ and H- onto L-
- 4. maps H onto L and H onto L

83. At
$$z = 0$$
 the function $f(z) = \frac{e^z + 1}{e^z - 1}$ has

- 1. a removable singularity.
- 2. a pole.
- 3. an essential singularity.
- 4. the residue of f(z) at z = 0 is 2.
- **84.** Let $H = \{e, (1,2) (3, 4)\}$ and $K = \{e, (1, 2) (3, 4), (1,3) (2, 4), (1, 4) (2, 3)\}$ be subgroups of S_4 , where e denotes the identify element of S_4 . Then
 - 1. H and K are normal subgroups of S_4
 - 2. H is normal in K and K is normal in A_4
 - H is normal in A₄ but not normal in S₄
 - K is normal in S₄ but H is not.
- **85.** Let $\langle p(x) \rangle$ denote the ideal generated by the polynomial p(x) in $\mathbb{Q}[x]$. If $f(x) = x^3 + x^2 + x + 1$ and $g(x) = x^3 x^2 + x 1$, then
 - 1. $\langle f(x) \rangle + \langle g(x) \rangle = \langle x^3 + x \rangle$
 - 2. $\langle f(x) \rangle + \langle g(x) \rangle = \langle f(x) \cdot g(x) \rangle$
 - 3. $\langle f(x) \rangle + \langle g(x) \rangle = \langle x^2 + 1 \rangle$
 - 4. $\langle f(x) \rangle + \langle g(x) \rangle = \langle x^4 1 \rangle$
- **86.** Let I_1 be the ideal generated by $x^2 + 1$ and I_2 be the ideal generated by $x^3 x^2 + x 1$ in $\mathbb{Q}[x]$. If $R_1 = \mathbb{Q}[x]/I_1$ and $R_2 = \mathbb{Q}[x]/I_2$, then
 - 1. R₁ and R₂ are fields.
 - 2. R₁ is a field and R₂ is not a field.
 - R₁ is an integral domain, but R₂ is not an integral domain.
 - R₁ and R₂ are not integral domains.

87. Let
$$G = \mathbb{Z}_{10} \times \mathbb{Z}_{15}$$
. Then

- G contains exactly one element of order
- 2. G contains exactly 5 elements of order 3
- 3. G contains exactly 24 elements of order 5
- 4. G contains exactly 24 elements of order 10
- 88. The space C [0, 1] of continuous functions on [0, 1] is complete with respect to which of the following
 - $||f||_{\infty} = \sup\{|f(x)| : x \in [0, 1]\}$

2.
$$||\mathbf{f}||_2 = \left(\int_0^1 |f(x)|^2 dx\right)^{1/2}$$

- 3. $||f||_{\infty}$, $\frac{1}{2} = ||f||_{\infty} + |f(1/2)|$
- 4. $||f||_{\infty}$ and $||f||_{\infty}$ $\frac{1}{2}$.
- 89. Consider the set

$$X = (-\infty, 0] \cup \left\{ \frac{1}{n} : n \in \mathbb{N} \right\} \subseteq \mathbb{R}$$
 with the subspace topology. Then

- 1. 0 is an isolated point.
- 2. (-2, 0] is an open set.
- 3 0 is a limit point of the subset

$$\left\{\frac{1}{n}: n \in \mathbb{N}\right\}$$

- (-2,0) is an open set.
- **90.** Consider three subsets of \mathbb{R}^2 , namely

$$A_1 = \{(x, y) : x^2 + y^2 \le 1\}$$

$$A_2 = \{(1, y) : y \in \mathbb{R}\}$$

$$A_3 = \{(0, 2)\}.$$

Then there always exists a continuous realvalued function f on \mathbb{R}^2 such that

$$f(x) = a_i \text{ for } x \in A_i, j = 1, 2, 3$$

- if and only if at least two of the numbers
 a₁, a₂, a₃ are equal
- 2. if $a_1 = a_2 = a_3$
- 3. for all real values of a₁, a₂, a₃
- 4. if and only if $a_1 = a_2$

Unit III

91. The Green's function $G(x, \zeta)$, $0 \le x$, $\zeta \le 1$ of the boundary value problem

$$y'' + \lambda y = 0$$
, $y(0) = 0 = y(1)$

is

- symmetric in x and ζ
- 2. continuous at $x = \zeta$

3.
$$\frac{\partial G(x,\zeta)}{\partial x}\Big|_{x=\zeta^{-}} - \frac{\partial G(x,\zeta)}{\partial x}\Big|_{x=\zeta^{+}} = -1$$

4.
$$\frac{\partial G(x,\zeta)}{\partial x}\Big|_{x=\zeta^{-}} - \frac{\partial G(x,\zeta)}{\partial x}\Big|_{x=\zeta^{+}} = 1$$

92. For the boundary value problem,

$$y'' + \lambda y = 0,$$
 $y(-\pi) = y(\pi),$ $y'(-\pi) = y'(\pi),$

to each eigenvalue \(\lambda\), there corresponds

- 1. only one eigenfunction
- 2. two eigenfunctions
- 3. two linearly independent eigenfunctions
- 4. two orthogonal eigenfunctions
- 93. Let y₁(x) and y₂(x) form a fundamental set of solutions to the differential equation

$$\frac{d^2y}{dx^2} + p(x)\frac{dy}{dx} + q(x)y = 0, \quad a \le x \le b,$$

where p(x) and q(x) are continuous in [a, b], and x_0 is a point in (a, b). Then

- both y₁(x) and y₂(x) cannot have a local maximum at x₀.
- both y₁(x) and y₂(x) cannot have a local minimum at x₀.
- y₁(x) cannot have a local maximum at x₀ and y₂(x) cannot have local minimum at x₀ simultaneously.
- both y₁(x) and y₂(x) cannot vanish at x₀ simultaneously.

94. A general solution of the PDE

$$uu_x + yu_y = x$$

is of the form

1.
$$f\left(u^2 - x^2, \frac{y}{x+u}\right) = 0$$
, where $f: \mathbb{R}^2 \to$

 \mathbb{R} is C^1 and $\nabla f \neq (0,0)$ at every point

2.
$$u^2 = g\left(\frac{y}{x+u}\right) + x^2$$
, $g \in C^1(\mathbb{R})$

- 3. $f(u^2 + x^2) = 0$, $f \in C^1(\mathbb{R})$
- 4. f(x+y)=0, $f\in C^1(\mathbb{R})$
- 95. The PDE

$$u_{xx} + u_{yy} + \lambda u = 0, \quad 0 < x, y < 1$$

 $u(x, 0) = u(x, 1) = 0, \quad 0 \le x \le 1$
 $u(0, y) = u(1, y) = 0, \quad 0 \le y \le 1$

has

- 1. a unique solution u for any $\lambda \in \mathbb{R}$.
- 2. infinitely many solutions for some $\lambda \in \mathbb{R}$.
- 3. a solution for countably many values of λ .
- infinitely many solutions for all λ∈ ℝ.
- 96. The Cauchy problem

$$u_x(x,y) + u_y(x,y) = 0$$
 for $(x,y) \in \mathbb{R}^2$
 $u(x,x) =$ for all $x \in \mathbb{R}$

has

- 1. a unique solution.
- a family of straight lines as characteristics.
- solution which vanishes at (2, 1).
- infinitely many solutions.
- 97. Consider a linear system Ax = b with a computed solution x_C; the error and the residue are defined, respectively by

$$e = x - x_c$$
$$r = Ax - Ax_c$$

Then

- A small error necessarily implies a small residue.
- The error can be large with relatively small residue.
- The error can be small with relatively large residue.
- The error and the residue are always equal.

98. Consider the iteration function for Newton's method

$$g(x) = x - \frac{f(x)}{f'(x)}$$

and its application to find (approximate) square root of 2, starting with $x_0 = 2$. Consider the first and the second iterates x_1 and x_2 , respectively; then

- 1. $1.5 \le x_1 \le 2$
- 2. $1.5 \le x_1 \le 2$
- 3. $x_1 \le 1.5$; $x_2 \le 1.5$
- 4. $x_1 = 1.5$; $x_2 < 1$

99. In the Ritz method, seeking an extremum of the functional

$$I(y) = \int_{x_0}^{x_1} F\left(x, y, \frac{dy}{dx}\right) dx$$
; $y(x_0) = a, y(x_1) = b$,

The coordinate function/or the admissible function $\phi_i(x)$, i = 1, 2,... defined on $[x_0, x_1]$ must be

- linearly independent
- 2. continuous
- smooth
- 4. linearly independent, smooth and the functional be considered not along admissible curves y = y(x) but only along all possible linear combinations admissible functions

100. The integral equation, involving a parameter λ ,

$$\phi(x) = \cos zx + \lambda \int_0^{\pi} \cos(x + \zeta) d\zeta$$
has

- 1. a unique solution if $\lambda = 1$, and an infinite number of solution if $\lambda = \frac{2}{3}$
- 2. a unique solution if $\lambda = -1$, and an infinite number of solution if $\lambda = -\frac{2}{\pi}$
- 3. a unique solution if $\lambda \neq \frac{2}{\pi}$
- 4. no solution if $\lambda = \pm \frac{2}{\pi}$

101. Consider the force free motion of a rigid body about a fixed point 0. Suppose 3A, 5A and 6A are the principal moments of inertia at 0, and initially the angular velocity has components $\omega_1 = \sqrt{5}$, $\omega_2 = 0$,

> $\omega_3 = \sqrt{5}$ about the corresponding principal axes; if the body ultimately rotates about the mean axis, then

- 1. $\omega_1^2 + \omega_2^2 = 5$
- 2. $5\omega_2^2 + g\omega_1^2 = 45$
- 3. $\omega_3^2 = \omega_1^2$
- 4. $\omega_2^2 \neq \omega_1^2$
- 102. Using Euler's dynamical equation for forcefree motion of a rigid body, symmetrical about the Z-principal axis, with angular velocity $\overline{\omega} = (\omega_1, \omega_2, \omega_3)$, where ω_i , i = 1, 2,3, are the components along the three principal axes, it follows that
 - $1. \omega_i = constant$
 - 2. $\omega_2 = a \sin(\lambda t + b)$ with a, λ , and b as constant
 - 3. $\omega_3 = constant$
 - 4. $\omega_1^2 + \omega_2^2$ constant

Unit IV

- 103. Which of the following is/are cumulative distribution function(s) (c.d.f.) of random variable(s)?
 - 1. $F_1(x) = \begin{cases} 0, & x \le 0 \\ e^{-x}, & x > 0 \end{cases}$
 - 2. $F_2(x) = \begin{cases} 0, & x \le 0 \\ 1 e^{-x}, & x > 0 \end{cases}$

 - 3. $F_3(x) = \begin{cases} 0, & x \le 0 \\ 1, & x > 0 \end{cases}$ 4. $F_4(x) = \begin{cases} 0, & x < 0 \\ 1/2, & 0 \le x < 1 \\ 1, & x \ge 0 \end{cases}$

104. Let X be a random variable taking values in a set E. Let

P(X > a + b | X > a) = P(X > b) for all $a, b \in E$. Then which of the following is a possible distribution of X?

- 1. Poisson
- 2. Geometric
- 3. Log-normal
- 4. Exponential
- 105. Let {X_n} be a stationary Markov chain such that

$$P(X_{i+1} = 1 \mid X_i = 1) = p_1 = 1 - P(X_{i+1} = 0 \mid X_i = 1),$$

$$P(X_{i+1} = 1 \mid X_i = 0) = p_o = 1 - P(X_{i+1} = 0 \mid X_i = 0),$$

and
$$P(X_1 = 1) = \pi_1 = 1 - P(X_1 = 0)$$
.
Then

- 1. $\pi_1 = p_1$
- 2. $\pi_1 = p_0$

$$3. \ \pi_1 = \frac{p_0}{1 - p_1 + p_0}$$

- 4. $\pi_1 = \frac{1}{2}$
- 106. Suppose X and Y are independent N (0, 1) random variables.

Let
$$U = \frac{X}{Y}$$
 and $V = \frac{X}{|Y|}$. Then

- 1.U and V are independent
- 2.U and V have the same distribution
- 3.P(U = V) = 1/2
- 4.P(U < V) = 1/2
- 107. Suppose $X_1, X_2, ...$ is a sequence of i.i.d. random variables where $P(X_i = 1) = p = 1 P(X_i = 0), i = 1, 2...$

Let
$$Z = \frac{1}{500} \sum_{i=1}^{500} X_i$$
 and $\alpha = P(|Z-p| > 0.1)$.

Then for all p

- 1. $\alpha \leq .1$
- $2. \alpha \leq .05$
- 3. $\alpha > .01$
- 4. $\alpha = 0$

- 108. Suppose $X_1 \sim U(0, \theta)$, $X_2 \sim U(0, 1 + \theta)$ and X_1 and X_2 are independent. Then
 - 1. min $\{X_1, X_2\}$ is sufficient for θ
 - 2. max {X₁, X₂} is sufficient for θ
 - 3. max $\{X_1, X_2-1\}$ is sufficient for θ
 - 4. max $\{X_1+1, X_2\}$ is sufficient for θ
- **109.** Suppose that we have $n \ge 1$ i.i.d. observations $X_1, X_2,..., X_n$ each with a common $N(\mu,1)$ distribution where $\mu \ge 0$ is unknown parameter. Then
 - the maximum likelihood estimate and the uniformly minimum variance unbiased estimate for μ are the same.
 - 2. the minimum variance unbiased estimate for μ is a consistent estimate.
 - for any unbiased estimate for μ, there
 is another estimate for μ with a smaller
 mean squared error
 - the maximum likelihood estimate for μ
 has smaller mean squared error than
 the estimate obtained by the method of
 moments.
- 110. Let $X_1, X_2,...$ be i.i.d. observations from $N(\mu, \sigma^2)$ distribution with $-\infty < \mu < +\infty$ and $0 < \sigma^2 < \infty$ as unknown parameters. Then
 - sample mean is an unbiased estimate for μ but sample median is not an unbiased estimate for μ.
 - both sample mean and sample median are unbiased estimates for μ.
 - sample mean has smaller variance than sample median.
 - sample mean has smaller mean squared error than sample median.
- 111. Suppose X~ N(0, σ²), Y has the exponential distribution with mean 2σ² and, X and Y are independent. We want to test at level α H₀: σ²≤1 versus H₁: σ²>1. Then
 - UMP test does not exist
 - UMP test rejects H₀ when X² + Y is large
 - UMP test is a chi-square test
 - UMP test is a t-test

112. Suppose that the probability distribution of a discrete random variable X under two possible parameter values is as follows.

Parameter	1	2	3	4
θι	.01	.04	.05	.90
θ_2	.80	.10	.05	.05

Test H_0 : $\theta = \theta_1$ versus H_1 : $\theta = \theta_2$ at level α =0.05. Then the most powerful test

- 1. rejects H_0 if x = 1 or x = 2
- 2. rejects H_0 if x = 3
- 3. has power larger than 0.85
- 4. has power .05
- 113. In a Bayesian estimation problem of the Poisson mean λ , a gamma prior (with density proportional to $e^{-\beta\lambda}$ λ^{α} -1) is formulated. There is a sample of size n from the Poisson and the sample mean is \overline{x} . The posterior distribution of λ is
 - 1. a gamma distribution
 - 2. a Poisson distribution
 - 3. has mean = $\frac{n\overline{x} + \alpha}{n + \beta}$
 - 4. has mean = $(n\overline{x} + \alpha)(n + \beta)$
 - 114. Random variables X_1 , X_2 , X_3 are such that correlation $(X_1, X_2) = \text{correlation } (X_2, X_3) = \text{correlation } (X_3, X_1) = \rho$.
 - 1. ρ cannot be negative
 - 2. p can take any value between -1 and + 1
 - 3. $\rho \ge -0.5$
 - 4. ρ is either +1 or -1
 - observations X_1, X_2, X_3, X_4 such that $E(X_1) = A+B+C$; $E(X_2) = A$; $E(X_3) = B$; $E(X_4) = A-B-C$ [where A, B, C, D are parameters]. Then
 - 1. B + C is not estimable
 - 2. A, B, C are all estimable
 - 3. A+B+C is estimable
 - X₂ is the Best Linear unbiased estimate of A

- 116. In a survey of a population of N = nk units, a sample of n units is to be drawn by systematic sampling with a random start between 1 and k and selecting every k^{th} unit. Then
 - the sample mean is an unbiased estimate of the population mean.
 - the variance of the sample mean cannot be estimated under this design.
 - if the N population units have been arranged at random, then the sample is equivalent to a simple random sample with replacement.
 - if the N population units have been arranged at random, then the sample is equivalent to a simple random sample without replacement.
- 117. Let \mathbb{D} be a balanced incomplete block design with usual parameters v, b, r, k, λ . Which of the following statements is true?
 - 1. \mathbb{D} is connected if $k \ge 2$.
 - The variance of the best linear unbiased estimator of an elementary treatment contrast under D is proportional to 2/r
 - The covariance between the best linear unbiased estimators of a pair of orthogonal treatment contrasts under D is zero.
 - The efficiency factor of D relative to a randomized (complete) block design with replication r is strictly smaller than unity.
- 118. Suppose that we have a data set consisting of 25 observations, where each value is either 5 or 10.
 - The mean of the data cannot be larger than the median.
 - 2. The mean of the data cannot be smaller than the median.
 - The mean and the median for the data will be the same only if the variance of the data is zero.
 - The mean and the median for the data will be different only if the range is 5.

119. Suppose that the LP problem maximise $\mathbf{c}^{\mathsf{T}}\mathbf{x}$

subject to

 $Ax \leq b$

 $x \ge 0$

admits a feasible solution and the dual minimise b^Ty

subject to $A^Ty \ge c$

$$y \ge 0$$

admits a feasible solution yo Chen

- 1. the dual admits an optimal solution.
- 2. any feasible solution x_0 of the primal and y_0 of the dual satisfies $b^T y_0 \le c^T x_0$.
- 3. the dual problem is unbounded.
- 4. the primal problem admits an optimal solution.
- 120. Let X(t) be the number of customers in an M/M/1 queuing system with arrival rate $\lambda > 0$ and service rate $\mu > 0$.

It is known that $\lim_{t\to\infty} P(X(t)=1) = \frac{1}{4}$.

Which of the following is true?

1.
$$\lim_{t\to\infty} E(X(t)=1) = \frac{1}{3}$$

$$2. \lim_{t\to\infty} E(X(t)=1) = \frac{\lambda}{\mu}$$

3.
$$\lim_{t \to \infty} Var(X(t)=1) = \frac{1}{9}$$

4.
$$\lim_{t\to\infty} Var(X(t)=1) = \left(\frac{\lambda}{\mu}\right)^2$$