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## **MATHEMATICS PAPER IA.- MARCH 2010.**

## ALGEBRA, VECTOR ALGEBRA AND TRIGONOMETRY

TIME	: 3hrs	Max. Marks.75
SECTION A		
VERY	SHORT ANSWER TYPE QUESTIONS.	10X2 =20
Noe : Attempt all questions. Each question carries 2 marks.		
1.	If $f: Q \to Q$ is defined by $f(x) = 5x + 4$ for all $x \in Q$ , find $f^{-1}$	
2.	Find the domain of the function $f(x) = log(x^2 - 4x + 3)$	
3.	Let $\mathbf{a} = 2\mathbf{i} + 4\mathbf{j} - 5\mathbf{k}$ , $\mathbf{b} = \mathbf{i} + \mathbf{j} + \mathbf{k}$ and $\mathbf{c} = \mathbf{j} + 2\mathbf{k}$ . Find unit vector in the op $\mathbf{a} + \mathbf{b} + \mathbf{c}$ .	posite direction of
4.	Find the vector equation to the line passing through the points $i+j+k$ , $i-j+k$	+k
5.	Find the value of $\cos^2 45^\circ - \sin^2 15^\circ$	
6.	Find the value of $\tan 10^{0} + \tan 35^{0} + \tan 10^{0} \cdot \tan 35^{0}$	
7.	If $\cosh x = \frac{5}{2}$ , find the values of i) $\cosh (2x)$ and ii) $\sinh (2x)$	
8.	Ina $\triangle ABC$ , find $b\cos^2\frac{\pi}{2} + c\cos^2\frac{\pi}{2}$	
9.	Write the polar form of -1+i	
10.	Find the angle between the vectors $i+2j+3k$ and $3i-j+2k$	

### **SECTION B**

### SHORT ANSWER TYPE QUESTIONS.

#### 5X4 =20

Note: Answer any FIVE questions. Each question carries 4 marks.

- 11. If  $\overline{a}, \overline{b}, \overline{c}$  are linearly independent vectors, then show that  $\overline{a} 2\overline{b} + 3\overline{c}, -2\overline{a} + 3\overline{b} 4\overline{c}, -\overline{b} + 2\overline{c}$  are linearly dependent
- 12. Prove that the angle between any two diagonals of a cube is given by  $\cos^{-1}\frac{1}{3}$ .
- 13. If  $\tan \theta = \frac{b}{a}$ , then prove that  $a \cos 2\theta + b \sin 2\theta = a$

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14. Solve the 
$$\sin x + \sqrt{3}\cos x = \sqrt{2}$$

15. Prove that  $Sin^{-1}\frac{4}{5} + 2Tan^{-1}\frac{1}{3} = \frac{\pi}{2}$ 

16. In 
$$\triangle ABC$$
, prove that  $\cot A + \cot B + \cot C = \frac{a^2 + b^2 + c^2}{4\Delta}$ 

17. Show that  $8\sin^4\theta = \cos 4\theta - 4\cos 2\theta + 3$ 

### SECTION C

### LONG ANSWER TYPE QUESTIONS.

 $5 \times 7 = 35$ 

Note: Answer any Five of the following. Each question carries 7 marks.

18. If  $f: A \to B$ ,  $g: B \to C$  be bijections. Then prove that  $(gof)^{-1} = f^{-1}og^{-1}$ .

19. Prove by induction 
$$a + (a+d) + (a+2d) + \dots \text{ to } n \text{ terms} = \frac{n}{2} [2a + (n-1)d]$$

20. Find the cartesian equation of the plane passing through the points (2, 3, 1), (4, 5, 2), and (3, 6, 5).

21. In triangle ABC, prove that 
$$\cos\frac{A}{2} + \cos\frac{B}{2} + \cos\frac{C}{2} = 4\cos\frac{\pi - A}{4}\cos\frac{\pi - B}{4}\cos\frac{\pi - C}{4}$$

22. If  $P_1, P_2, P_3$  are altitudes drawn from vertices A,B,C to the opposite sides of a triangle respectively, then show that

(i) 
$$\frac{1}{P_1} + \frac{1}{P_2} + \frac{1}{P_3} = \frac{1}{r}$$
 (ii)  $P_1 P_2 P_3 = \frac{(abc)^2}{8R^3}$ 

- 23. On a tower AB of height h, there is a flag staff BC. At a point d meters away from the foot of the tower, AB and BC are making equal angles. Show that the height of the flag staff if  $h\left(\frac{d^2 + h^2}{d^2 h^2}\right)$  meters.
- 24. If n is an integer then show that  $(1 + \cos \theta + i \sin \theta)^n + (1 + \cos \theta i \sin \theta)^n = 2^{n+1} \cos^n \left(\frac{\theta}{2}\right) \cos\left(\frac{n\theta}{2}\right)$

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